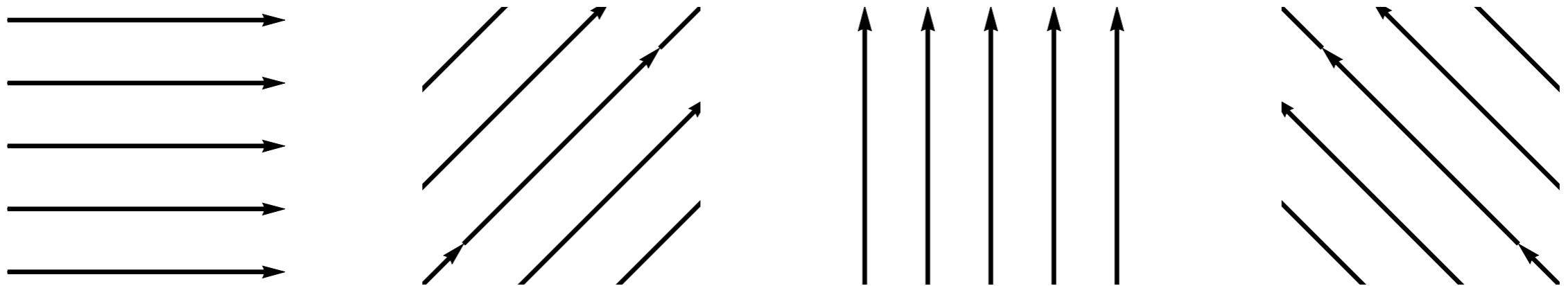


Floquet Superconductor in Holography



Takaaki Ishii (Utrecht)

arXiv:1804.06785 [hep-th] w/ Keiju Murata

Motivations

Holography in time dependent systems

Nonequilibrium phenomena, nonlinear dynamics

e.g.) QGP, quench, thermalization

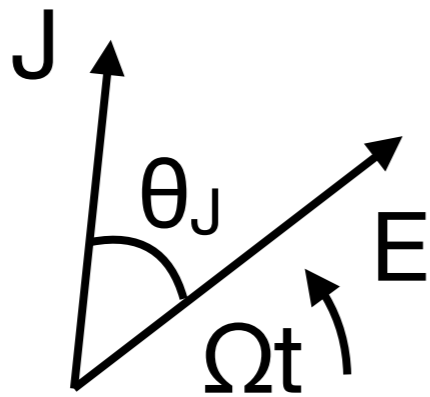
Condensed matter in real world

Driving, laser-pulse, nonequilibrium states

e.g.) ARPES, superconductivity enhancement

Rotating electric field

We apply a circularly polarized electric field



$$E_x + iE_y = E e^{i\Omega t}$$

$$J_x + iJ_y = J e^{i\Omega t + i\theta_J}$$

$$A_x + iA_y = A e^{i\Omega t} \quad (A \equiv iE/\Omega)$$

Amplitude is fixed, only direction changes: $|\vec{E}| = |E|$

c.f.) Linear polarization: $E_x = E \cos(\Omega t)$, $E_y = 0$

Rotating holography

Complex scalar with phase rotation $\phi \sim \phi_0 e^{i\Omega t} + \dots$

[Biasi-Carrecedi-Mas-Musso-Serantes]

c.f.) Spontaneous rotation: Boson star

[Astefanesei-Radu, Buchel-Liebling-Lehner]

D3/D7+rotating cpx scalar for CME

[Hoyos-O'Bannon-Nishioka]

D3/D7+rotating electric field $A_x + iA_y = A(z)e^{i\Omega t}$

[Hashimoto-Kinoshita-Murata-Oka]

↑ **Murata's talk**

Review: holographic superconductor

The simplest probe model in Sch-AdS4 BH:

[Hartnoll-Herzog-Horowitz]

$$S = \int d^4x \sqrt{-g} \left(-\frac{1}{4} F_{\mu\nu} F^{\mu\nu} - |D_\mu \Psi|^2 + 2|\Psi|^2 \right)$$

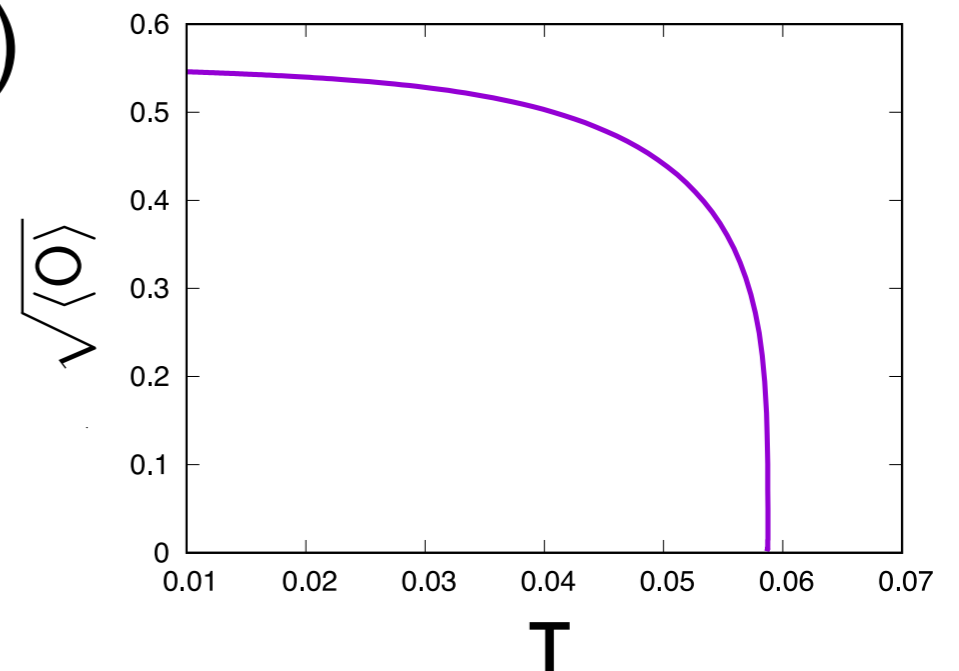
$$ds^2 = \frac{1}{z^2} \left(-f(z) dt^2 + \frac{dz^2}{f(z)} + dx^2 + dy^2 \right)$$

U(1) charge (we use $\mu=1$ today)

$$A_t(z) = \mu - \rho z + \dots$$

Spontaneous condensation

$$\Psi(z) = \psi_2 z^2 + \dots \neq 0$$



We add the rotating gauge field

$$S = \int d^4x \sqrt{-g} \left(-\frac{1}{4} F_{\mu\nu} F^{\mu\nu} - |D_\mu \Psi|^2 + 2|\Psi|^2 \right)$$

Ansatz: $A_t(z), \Psi(z), A_x + iA_y = b(z)e^{i\Omega t}$

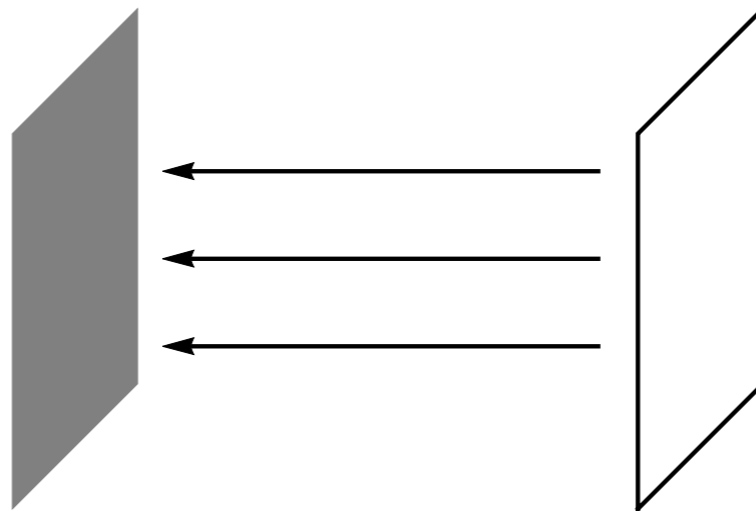
Then time dependence disappears: we get ODEs.

$$\mathcal{L} = -\frac{1}{2} A_t'^2 + \frac{f}{2} |b'|^2 - \frac{\Omega^2}{2f} |b|^2 + \frac{1}{z^2} \left[f \psi'^2 + \left(|b|^2 - \frac{2}{z^2} - \frac{A_t^2}{f} \right) \psi^2 \right]$$

Source and current in $A_{x,y}$: $b(z) = A + Jz + \dots$

Holographic steady state

BH is like heat bath in probe models



Conserved flux (in the holographic direction)

$$b \rightarrow be^{i\theta} : J_\theta = \frac{if}{2}(b^*b' - b^{*'}b), \quad \partial_z J_\theta = 0$$

This gives Joule heating for normal conductor

$$q = \Omega J_\theta = \vec{E} \cdot \vec{J}$$

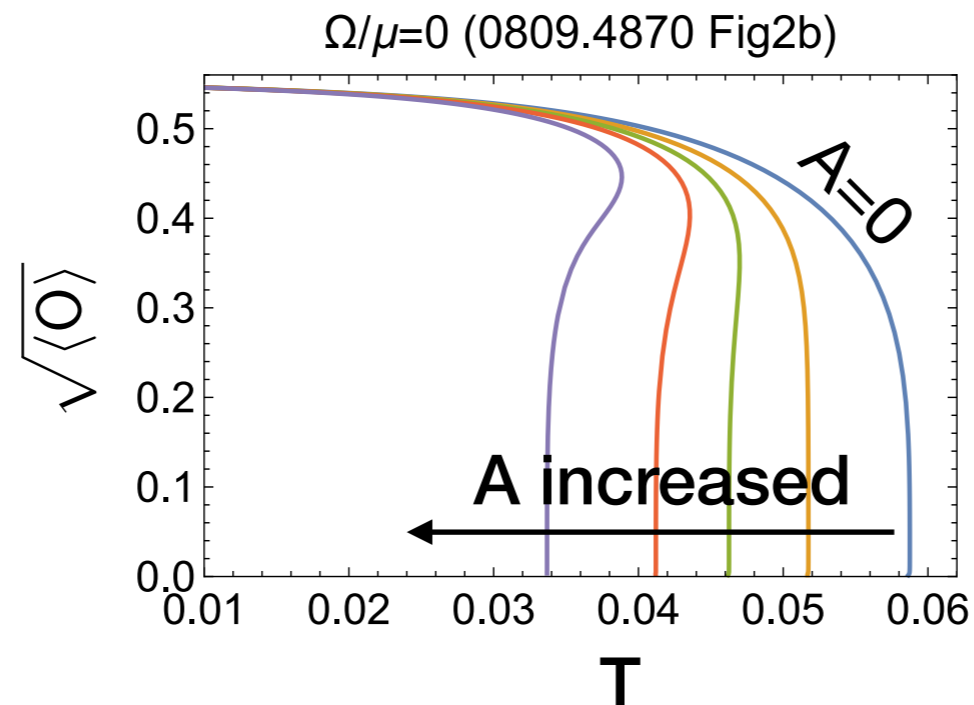
Review: $\Omega=0$

This is constant gauge potential for superfluid velocity.

[Basu-Mukherjee-Shieh, Herzog-Kovtun-Son]

In our setup: $(E, \Omega) \rightarrow 0$ with $A=E/\Omega$ fixed

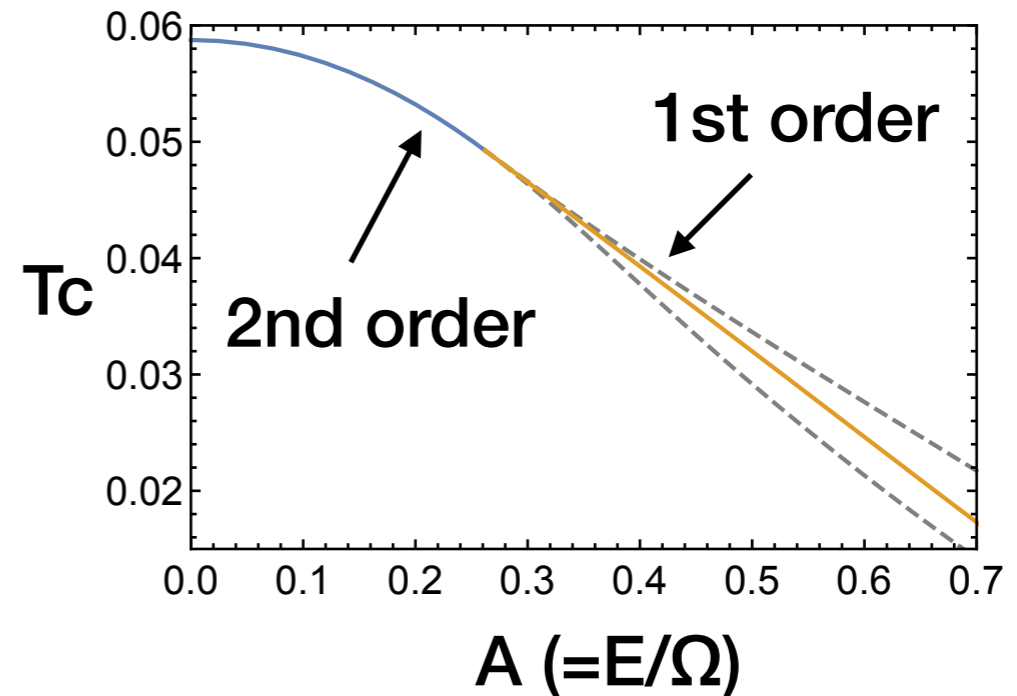
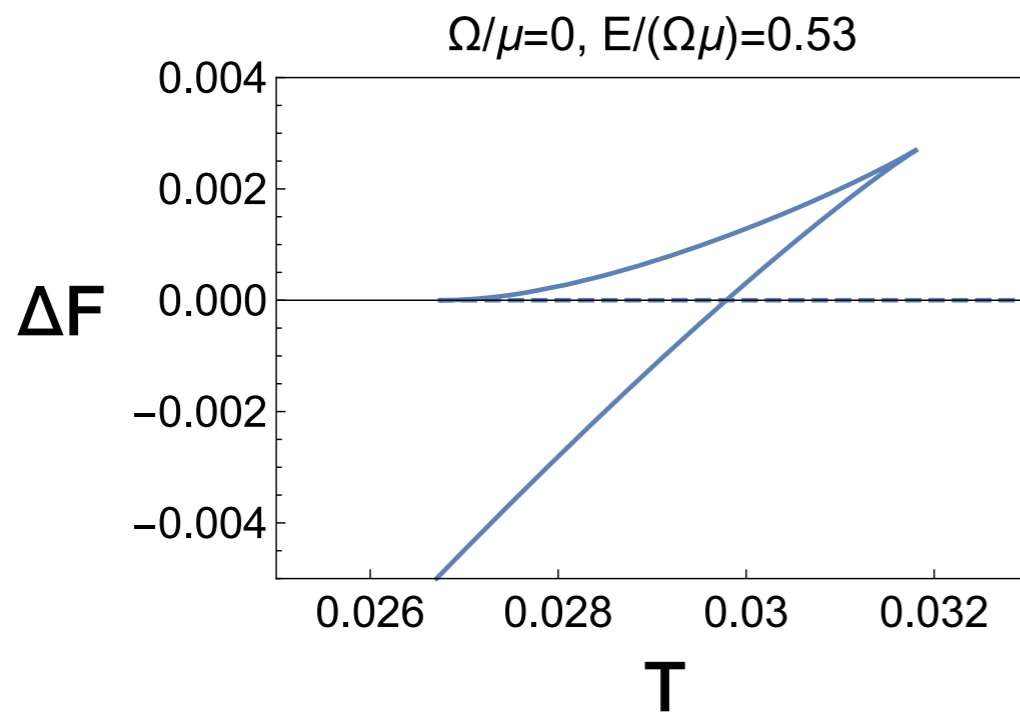
Phase transition changes from 2nd to 1st order.



Free energy for $\Omega=0$

"Free energy is the minus of on-shell action."

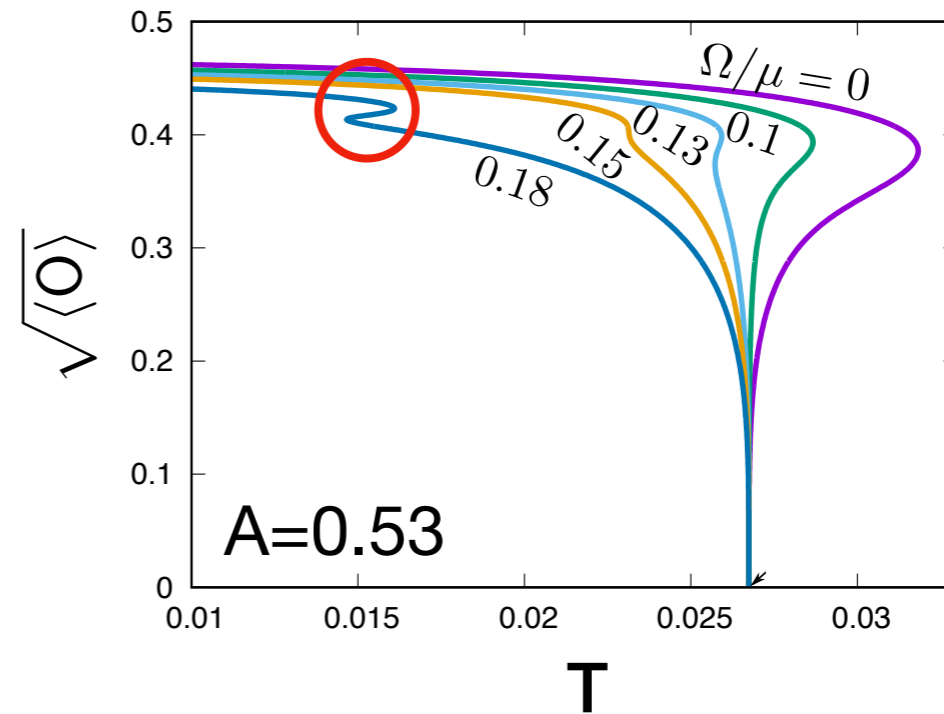
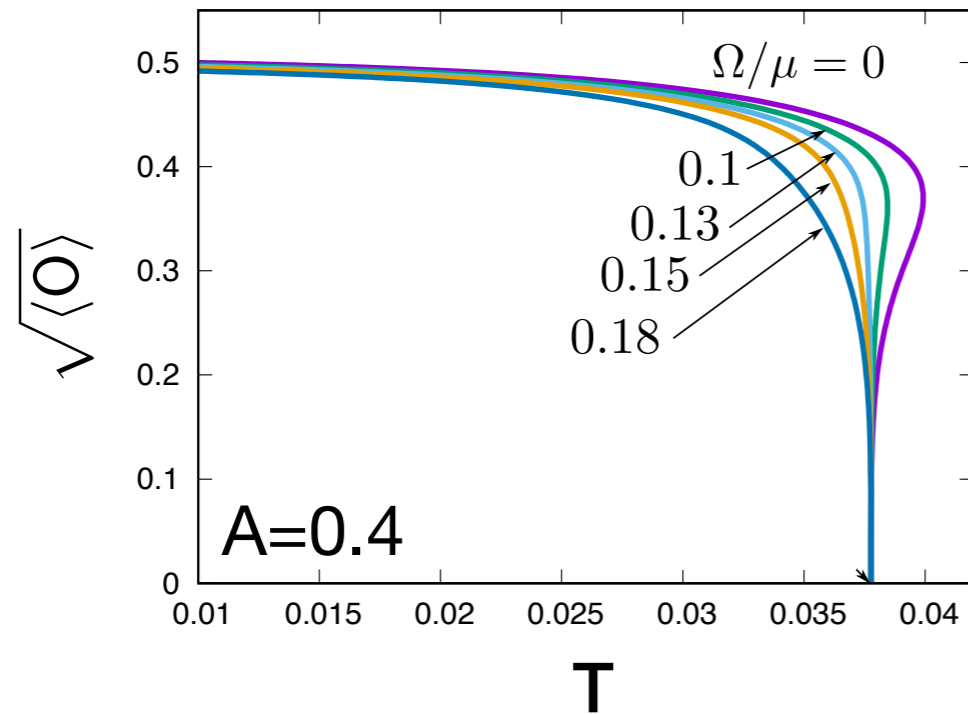
$$F_{\Omega=0} = -\frac{S_{\text{on-shell}}}{V} = -\frac{1}{2} \left(\mu\rho + \vec{A} \cdot \vec{J} \right) - \int \frac{dz}{z^2} \left(|b|^2 - \frac{A_t^2}{f} \right) \Psi^2$$



"Swallow tail" for 1st order PT

T_c always decreases

When $\Omega \neq 0$

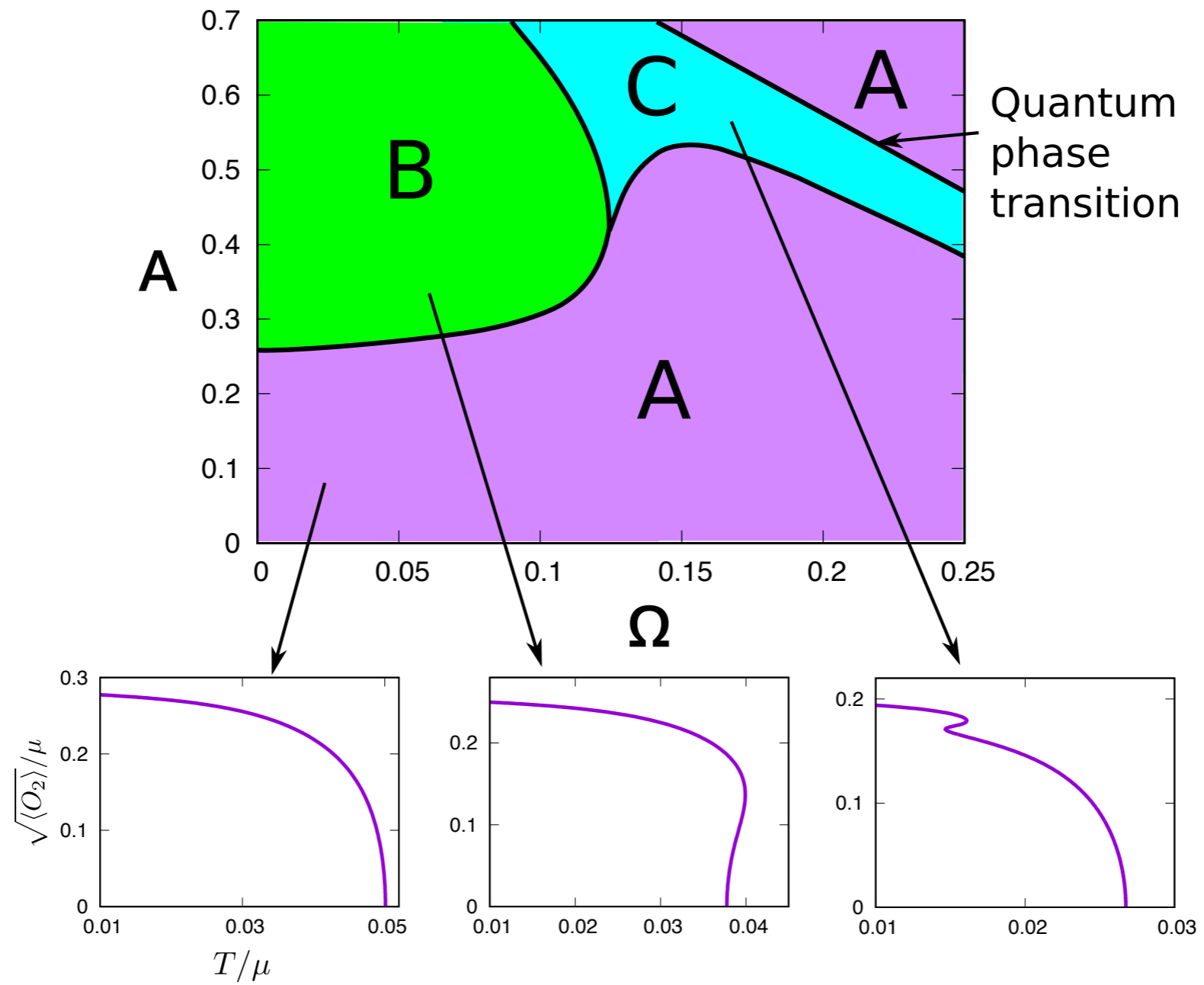


Normal-to-SC transition is pushed back to 2nd order.

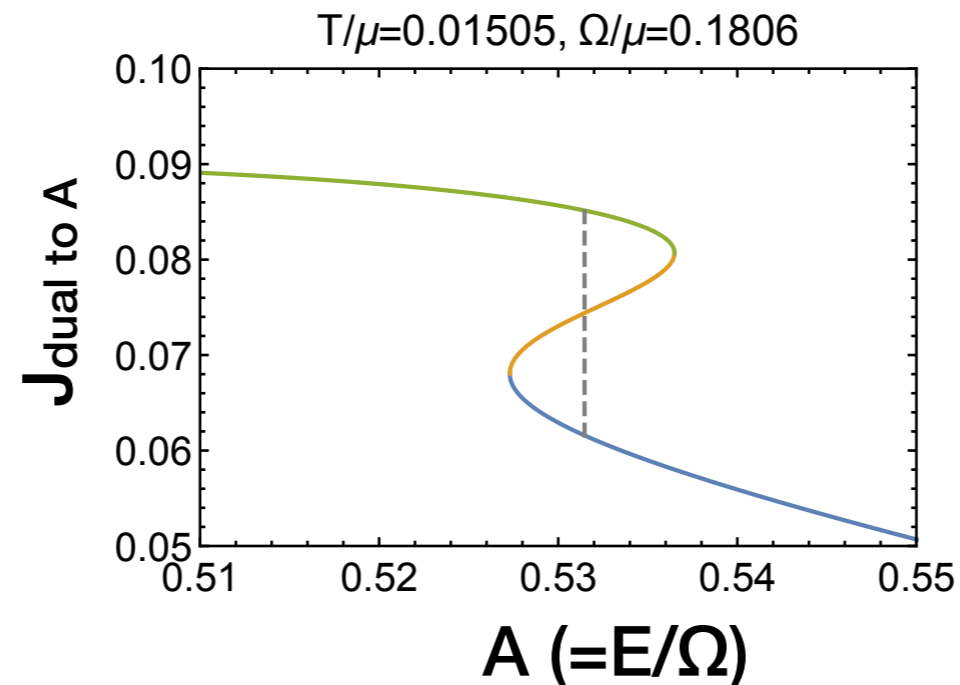
There appears spinodal structure inside the SC phase.

This indicates 1st order (phase) transition.

Phase diagram



Evaluate phase transition when $\Omega \neq 0$?



Order parameters will "jump" in the spinodal region.

Where do they actually jump?

Can I use Maxwell construction (aka "equal area law")?

$\Omega=0$ revisited

Free energy can be given in the variational form

$$\delta S_{\text{on-shell}} = \int_{\partial} d^3x \left(\rho \delta\mu + \vec{J} \cdot \delta \vec{A} \right)$$

$$\Rightarrow dF_{\Omega=0} = -\rho d\mu - \vec{J} \cdot d\vec{A}$$

Integrability is satisfied: $\frac{\partial \rho}{\partial \vec{A}} = \frac{\partial \vec{J}}{\partial \mu}, \quad \frac{\partial}{\partial \vec{A}} \times \vec{J} = 0$

Maxwell construction: $F_{\Omega=0} = - \int \rho d\mu = - \int \vec{J} \cdot d\vec{A}$

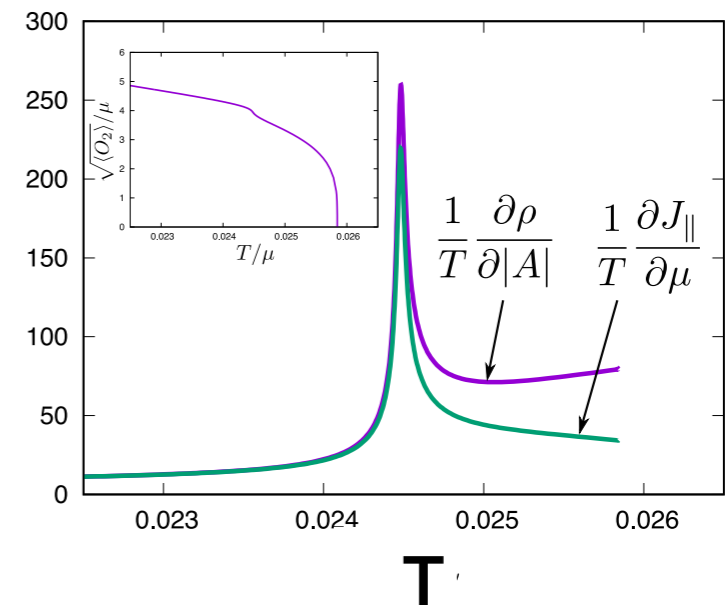
Free energy for $\Omega \neq 0$?

Do we have nonequilibrium thermodynamics in which there is dF satisfying $dF = -\rho d\mu - \vec{J} \cdot d\vec{A} + \dots$?

A: No

Integrability is violated:

$$\frac{\partial \rho}{\partial \vec{A}} \neq \frac{\partial \vec{J}}{\partial \mu}, \quad \frac{\partial}{\partial \vec{A}} \times \vec{J} \neq 0$$



The violation is small when the Joule heating q is small.

Is anything wrong with our sources/vevs?

AdS/CFT dictionary revisited

$$\delta S_{\text{on-shell}} = \delta s_b + \delta s_h$$

$$\delta s_b = \int d^3x \left[\rho \delta \mu + \vec{J} \cdot \delta \vec{A} - (q/\Omega) \delta(\Omega t) \right]$$

$$\delta s_h = \int d^3x \left[\Omega \text{Im}(b^* \delta b)_{\text{horizon}} + (q/\Omega) \delta(\Omega t) \right]$$

Real-time AdS/CFT dictionary

Field theory quantities are derived from δs_b .

We have $A_t(z) = \mu - \rho z + \dots$ $b(z) = A + Jz + \dots$

Then δs_b is not an integrable dF because of δs_h .

So there is difficulty

AdS/CFT dictionary gives how to calculate VEVs (ρ, J, \dots) in nonequilibrium ...from δs_b . We believe it.

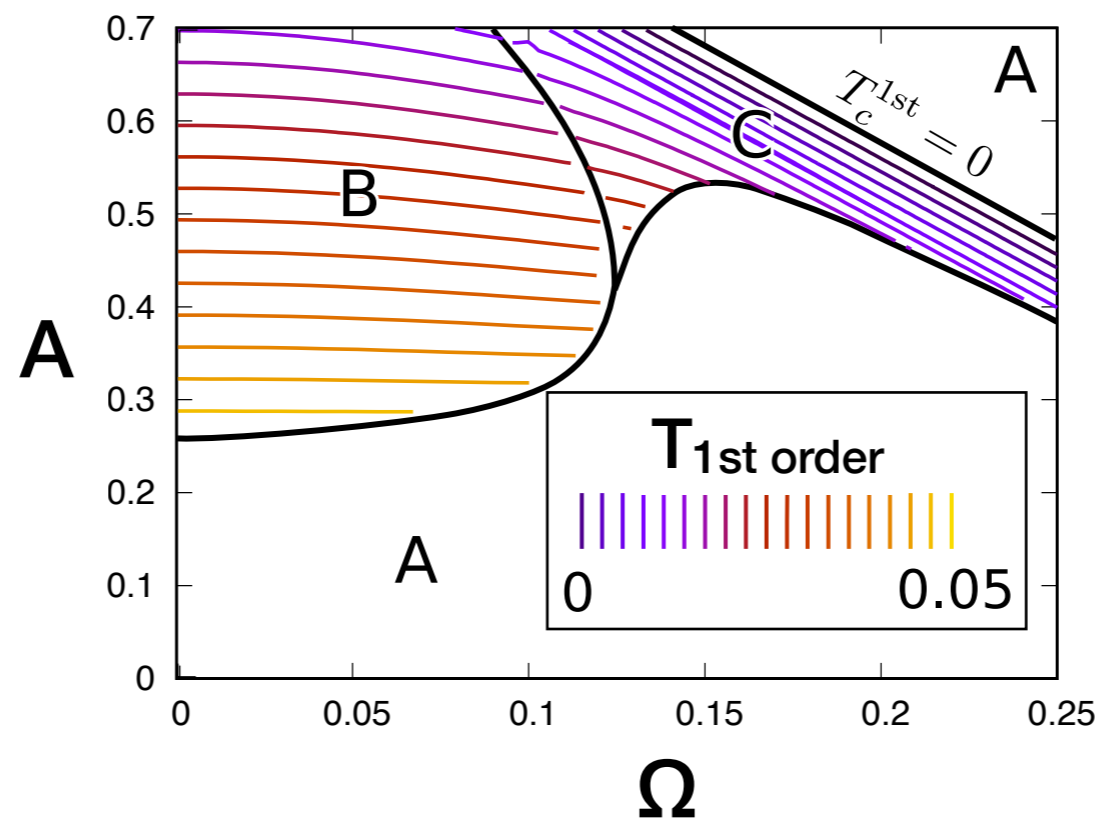
Then we do not have integrable dF for nonequilibrium steady solutions.

Should we have defined (ρ, J, \dots) such that we had $dF = -\rho d\mu - \vec{J} \cdot d\vec{A} + \dots$? Probably No.

But anyway we can estimate T_{1st} order

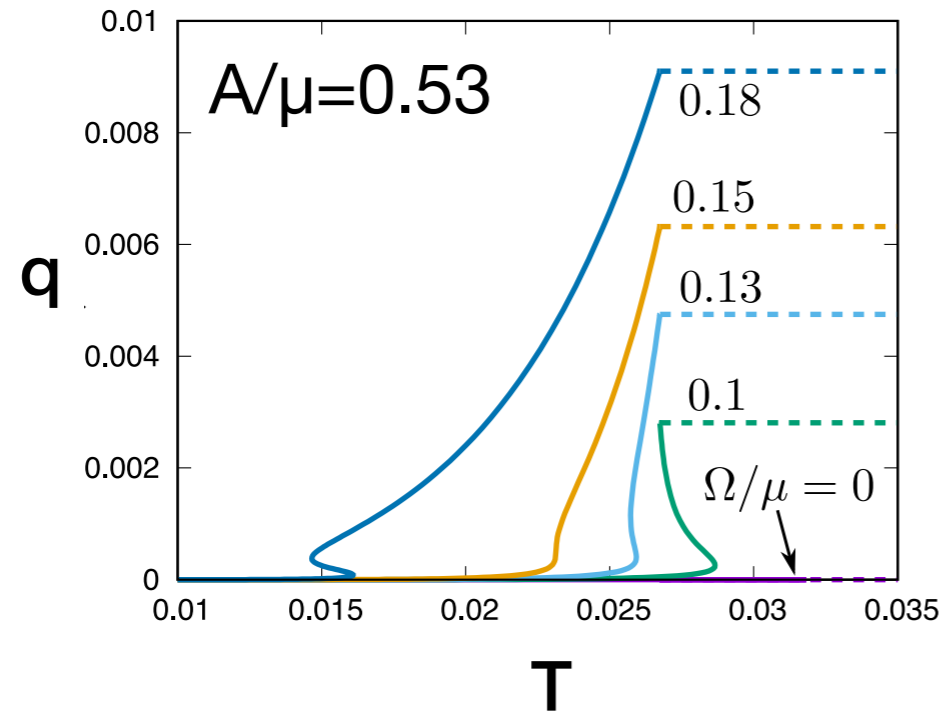
We employ a reasonable choice realizing the "swallow tail" for 1st order phase transition

$$F := \int \rho d\mu$$

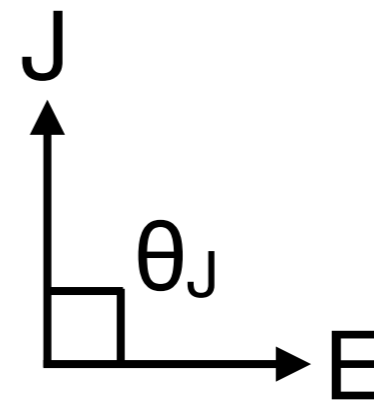


(2nd order T_c in region A is not shown)

Current: E and J get out of phase



$$q = \vec{E} \cdot \vec{J} \rightarrow 0$$



Joule heating is suppressed: no Ohm's law

Instead we have $E \perp J$: London equation

Discussion

Superconductivity enhancement is one of our motivations.

But in our results T_c for superconducting phase transition is always lowered by the electric field.

This might be due to our model being too simple.

What will/can/need to be done?

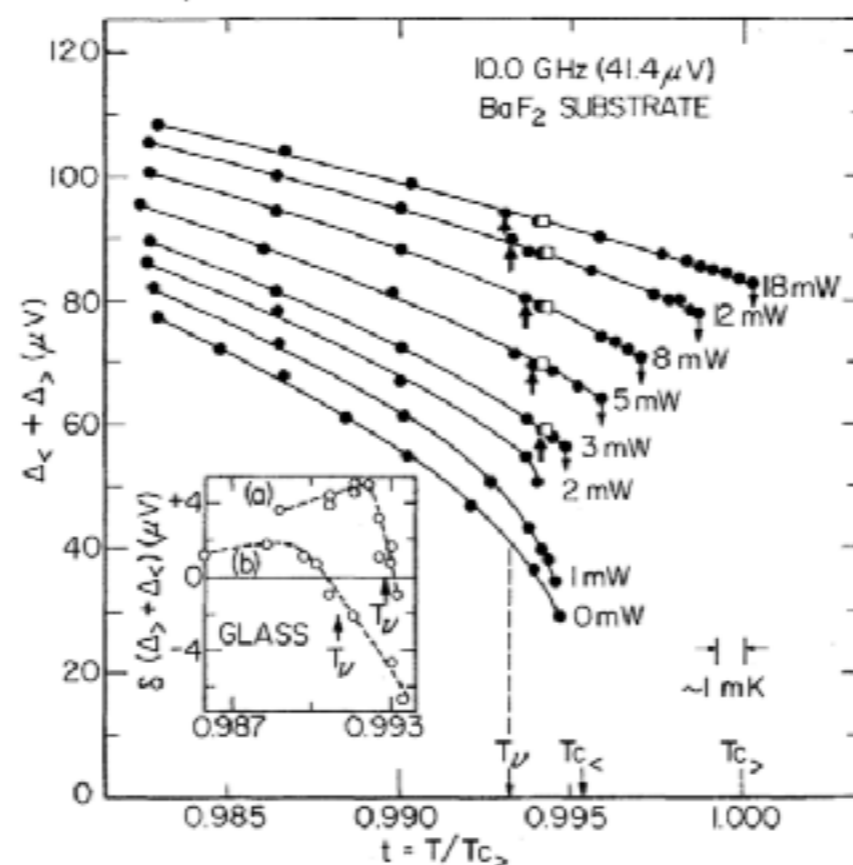
Measurement of Microwave-Enhanced Energy Gap in Superconducting Aluminum by Tunneling*

Tom Kommers and John Clarke

Department of Physics, University of California, and Materials and Molecular Research Division, Lawrence Berkeley Laboratory, Berkeley, California 94720

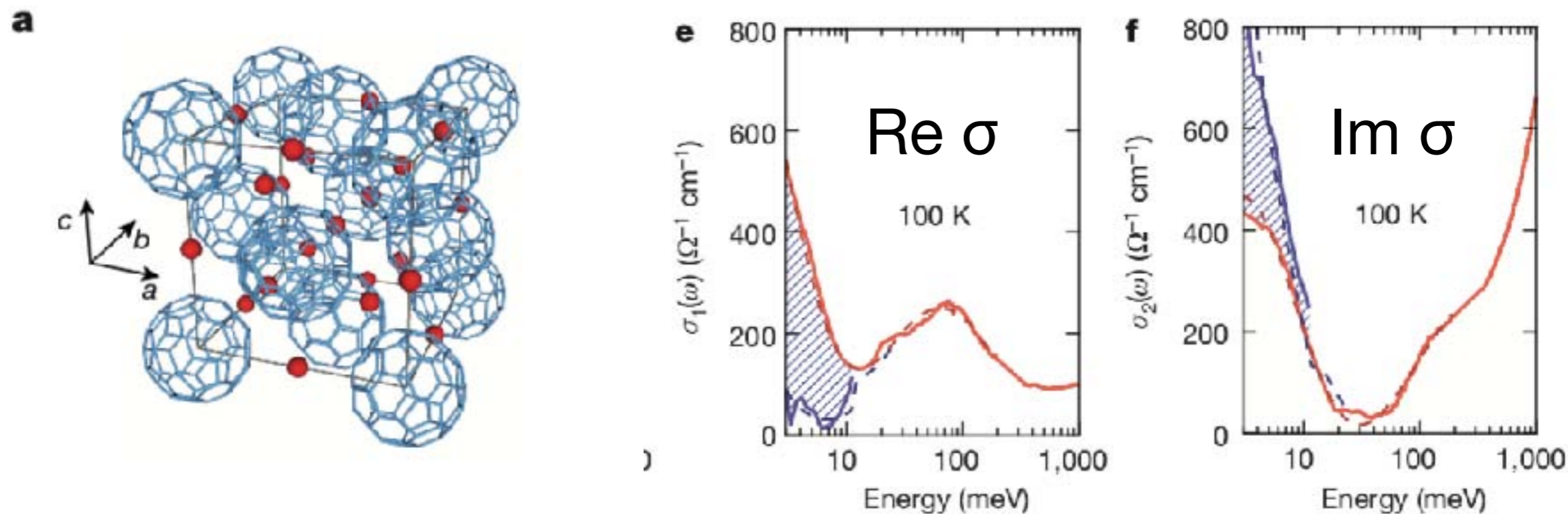
(Received 7 February 1977)

Al-Al₂O₃-Al tunnel junctions were used to measure large increases in the energy gap of superconducting aluminum films in the presence of 10-GHz microwave radiation. When



Possible light-induced superconductivity in K_3C_{60} at high temperature

M. Mitrano¹, A. Cantaluppi^{1,2}, D. Nicoletti^{1,2}, S. Kaiser¹, A. Perucchi³, S. Lupi⁴, P. Di Pietro³, D. Pontiroli⁵, M. Riccò⁵, S. R. Clark^{1,6,7}, D. Jaksch^{7,8} & A. Cavalleri^{1,2,7}



Nonlinear lattice dynamics as a basis for enhanced superconductivity in $\text{YBa}_2\text{Cu}_3\text{O}_{6.5}$

R. Mankowsky^{1,2,3*}, A. Subedi^{4*}, M. Först^{1,3}, S. O. Mariager⁵, M. Chollet⁶, H. T. Lemke⁶, J. S. Robinson⁶, J. M. Glownia⁶, M. P. Minitti⁶, A. Frano⁷, M. Fechner⁸, N. A. Spaldin⁸, T. Loew⁷, B. Keimer⁷, A. Georges^{4,9,10} & A. Cavalleri^{1,2,3,11}

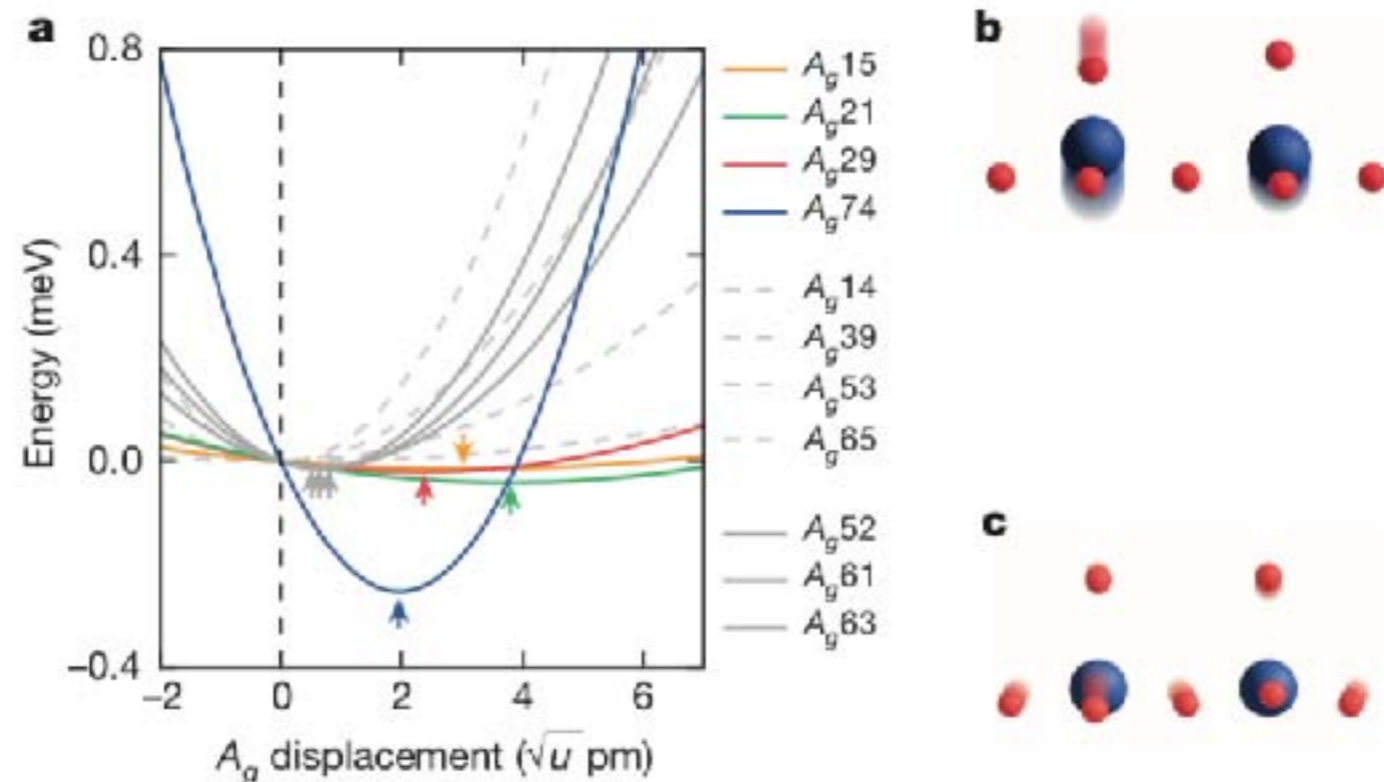


Figure 3 | First-principles calculations of cubic coupling between 11 A_g modes and the driven B_{1u} mode. **a**, Energy potentials of all A_g modes for a

Summary

We applied a rotating electric field to holographic superconductors.

We obtained steady state solutions.

We discussed nonequilibrium "thermodynamics."

Many things to do before HoloQuark2020

backreaction, photon stars; vortex formation, turbulence; SC enhancement, lattices, ...