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# Initial stages in heavy-ion collisions - from small to large systems

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# Contents:

1. Introduction.

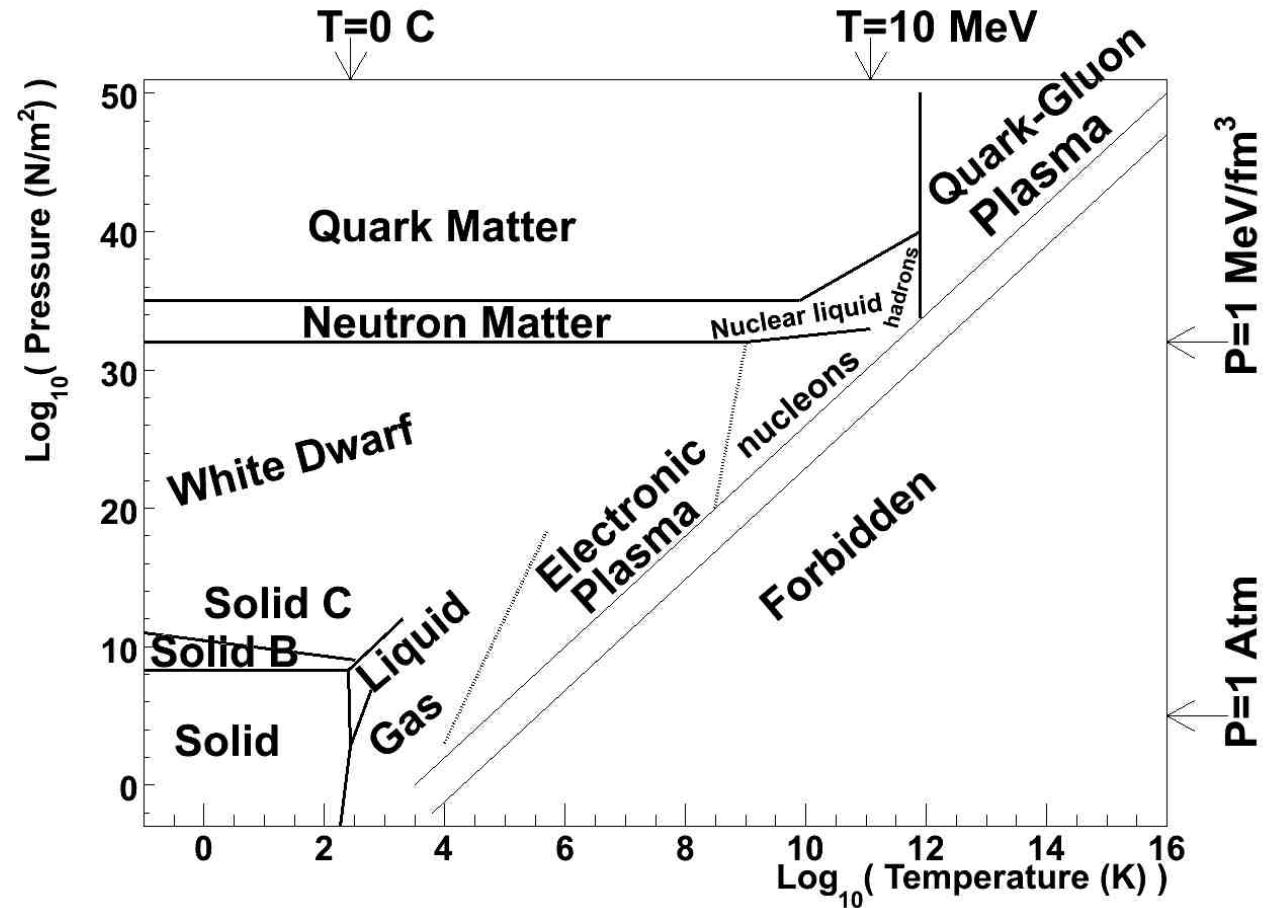
2. Experimental findings.

3. Non-hydrodynamical approaches to collectivity.

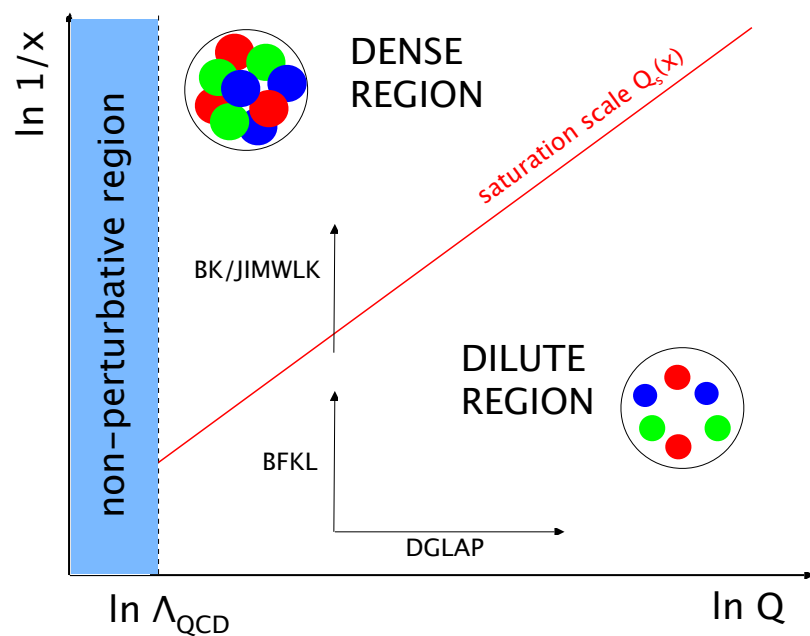
4. Summary.

# Heavy-ion collisions:

- Behaviour of matter at **high temperature and baryon number**: confinement and chiral symmetry breaking.



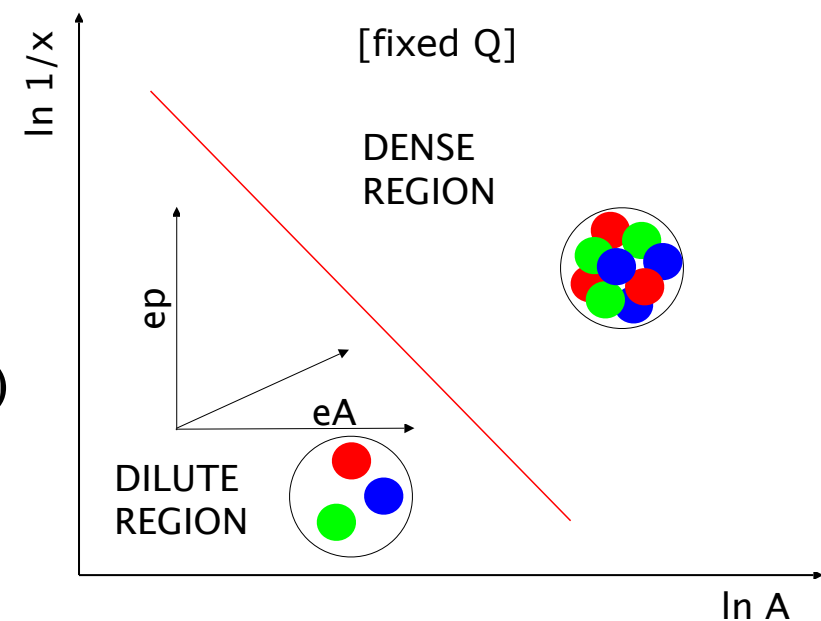
- Behaviour of QCD at **high energies/A**  $\equiv$  high partonic densities.



$$\frac{xG_A(x, Q_{s,A}^2)}{\pi R_A^2 Q_{s,A}^2} \sim 1$$

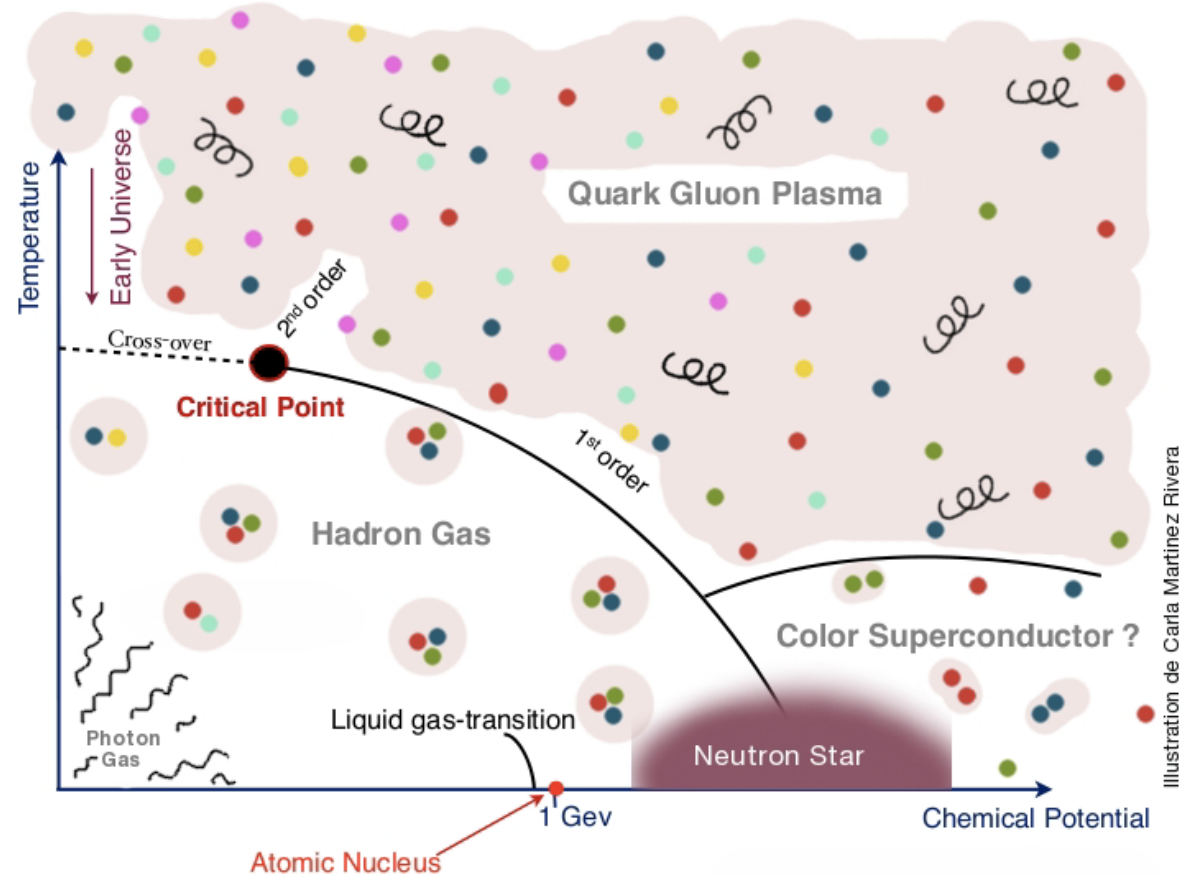
$$\Rightarrow Q_{s,A}^2 \propto A^{1/3} xG_p(x, Q_{s,A}^2)$$

$$\propto A^{1/3} \frac{1}{x^{1/3}}$$

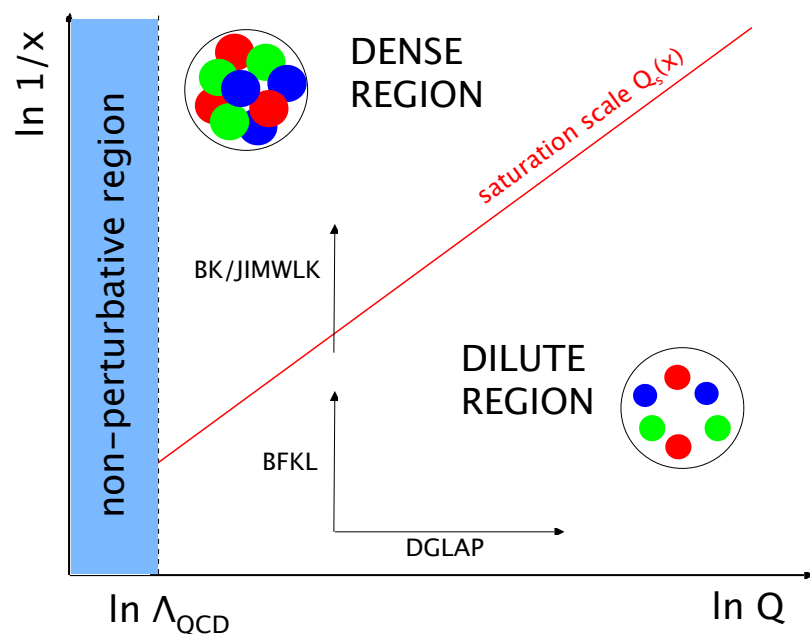


# Heavy-ion collisions:

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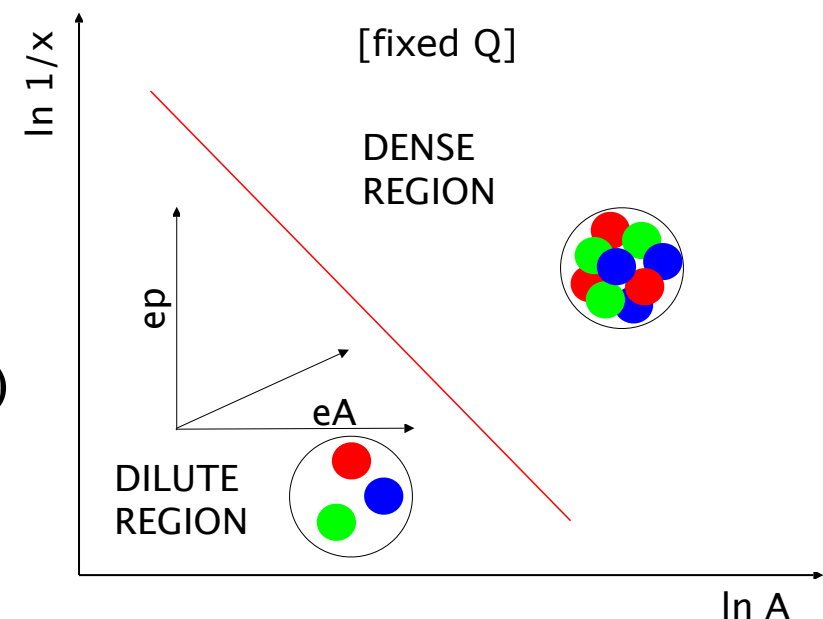
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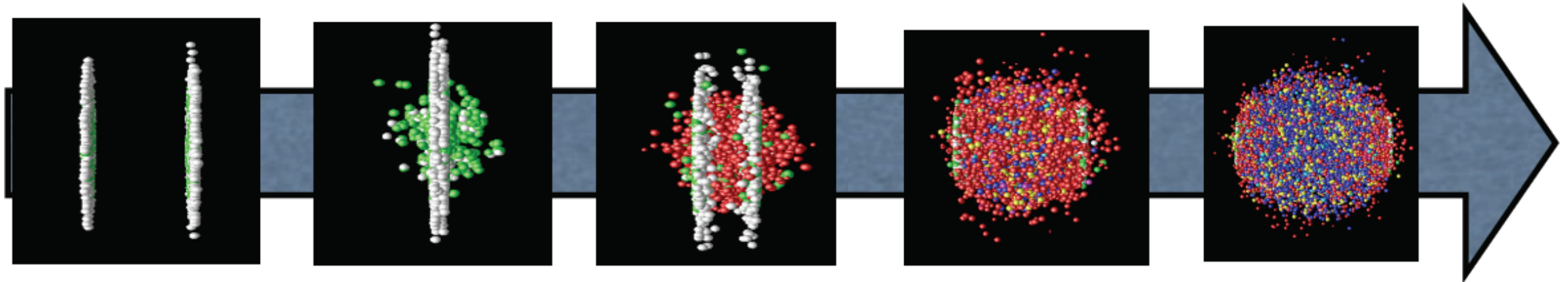
# The yet unsolved questions:

- Nucleus  $\neq Zp+(A-Z)n$ .
- Particle production at large scales similar to pp (dilute regime).

- Medium behaves very early like a low viscosity liquid: macroscopic description.

- Medium is very opaque to colour.

[B. Cole]



Gluons from saturated nuclei → Glasma? → QGP → Reconfinement

- Lack of information about small- $x$  partons, correlations and transverse structure.
- We do not understand the dense regime.

- How isotropised the system becomes?
- Why is hydro effective so fast, which dynamics?
- Why does this happen in pp/pA?

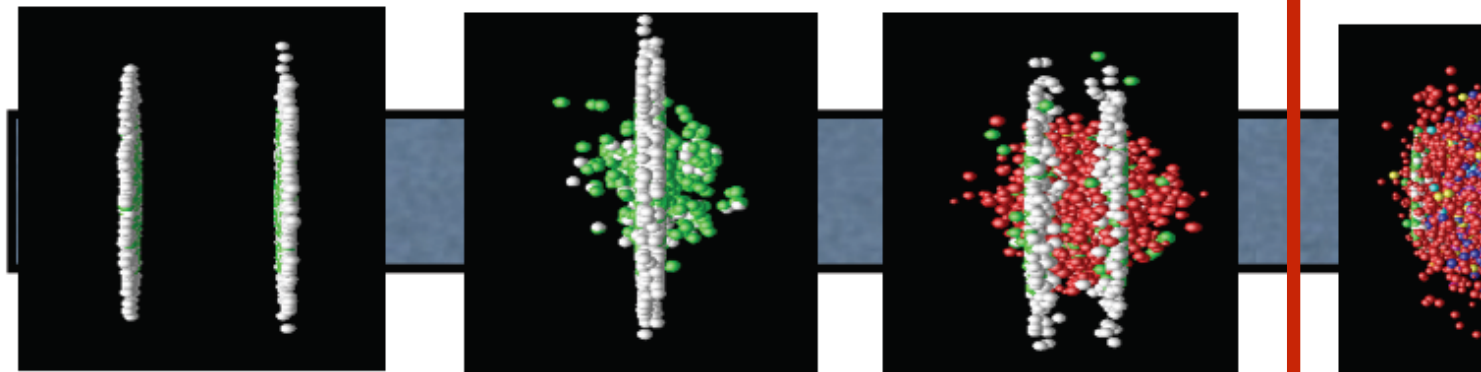
- What are the dynamical mechanisms for such opacity? Weak or strong coupling?
- How to extract accurately medium parameters?

# The yet unsolved questions:

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Gluons from saturated nuclei → Glasma? → QGP →

- I will focus on the physics that, observed in both small (pp, pA) and in large (AA) systems, seems to originate in the initial stages of the collisions.

- Lack of information about small-x partons, correlations and transverse structure.
- We do not understand the dense regime.

- How isotropised the system becomes?
- Why is hydro effective so fast, which dynamics?
- Why does this happen in pp/pA?

- I will concentrate on non-hydrodynamical approaches, taking for granted that everybody knows hydro... parameters?

# The context:

- **Macroscopic techniques** to describe nuclear matter and nuclear collisions can be traced back to the first studies of nuclear structure.
- **60's - Glauber model, Regge-Gribov theory: pre-QCD microscopic approaches to hadronic and nuclear collisions, unified approach.**
- Right after QCD proposal: Collins-Perry, Cabbibo-Parisi, Bear Mountain proceedings, ... deconfined matter could be created in heavy-ion collisions, later called **QGP**, formed by free partons (**gas**).
- **2001: azimuthal asymmetries as a signature of collective behaviour describable by relativistic hydrodynamics, later found at RHIC with little viscosity: perfect liquid in heavy-ion collisions, macroscopic description.**
- **2008-2009: ridge discovered in AuA collisions at RHIC.**
- **2010: ridge discovered in high multiplicity pp collisions at the LHC, later in pPb, hydrodynamic description working.**
- **Note: that pp could be described like AA was predicted both from the hydro and from the microscopic point of view (~2008).**

# The context:

- **Macroscopic techniques** to describe nuclear matter and nuclear collisions can be traced back to the first studies of nuclear structure.

## **From an old paradigm to a new one?**

**Old:** QGP produced in AA, pp as reference (vacuum), pA to separate (uninteresting) “cold nuclear matter” effects.

**New:** Smooth transition from pp to AA whose implications are still under debate:

- QGP is formed in small systems?
- Hydro-like collective behaviour, strangeness enhancement, ... are general features of high energy hadronic collisions?

later in pPb, hydrodynamic description working.

- **Note:** that pp could be described like AA was predicted both from the hydro and from the microscopic point of view (~2008).

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# Summary:

Observable or effect	PbPb	pPb (high mult.)	pp (high mult.)	Refs.
Low $p_T$ spectra (“radial flow”)	yes	yes	yes	[1–10]
Intermed. $p_T$ (“recombination”)	yes	yes	yes	[5, 6, 10–15]
Particle ratios	GC level	GC level except $\Omega$	GC level except $\Omega$	[8, 9, 16, 17]
Statistical model	$\gamma_s^{GC} = 1, 10\text{--}30\%$	$\gamma_s^{GC} \approx 1, 20\text{--}40\%$	$\gamma_s^C < 1, 20\text{--}40\%$	[9, 18, 19]
HBT radii ( $R(k_T), R(\sqrt[3]{N_{ch}})$ )	$R_{out}/R_{side} \approx 1$	$R_{out}/R_{side} \lesssim 1$	$R_{out}/R_{side} \lesssim 1$	[20–28]
Azimuthal anisotropy ( $v_n$ ) (from two part. correlations)	$v_1 - v_7$	$v_1 - v_5$	$v_2, v_3$	[29–31] [32–39, 39–43]
Characteristic mass dependence	$v_2 - v_5$	$v_2, v_3$	$v_2$	[39, 42–48]
Directed flow (from spectators)	yes	no	no	[49]
Charge dependent flow (CME, CMW)	yes	yes	not observed	[50–54]
Higher order cumulants (mainly $v_2\{n\}, n \geq 4$ )	“ $4 \approx 6 \approx 8 \approx \text{LYZ}$ ” +higher harmonics	“ $4 \approx 6 \approx 8 \approx \text{LYZ}$ ” +higher harmonics	“ $4 \approx 6 \approx 8 \approx \text{LYZ}$ ”	[39, 55–64, 64–69]
Weak $\eta$ dependence	yes	yes	not measured	[41, 65, 67, 70–76]
Factorization breaking	yes ( $n = 2, 3$ )	yes ( $n = 2, 3$ )	not measured	[40, 77, 78]
Event-by-event $v_n$ distributions	$n = 2 - 4$	not measured	not measured	[79, 80]
Event plane and $v_n$ correlations	yes	yes	yes	[81–84]
Direct photons at low $p_T$	yes	not measured	yes	[85, 86]
Jet quenching	yes	not observed	not observed	[87–107]
Heavy flavor anisotropy	yes	yes [108]	not measured	[108–118]
Quarkonia	$J/\psi \uparrow, \Upsilon \downarrow$	suppressed	not measured	[108, 118–125, 125–138]

Collective hadronisation

Collective expansion (hydro-like)

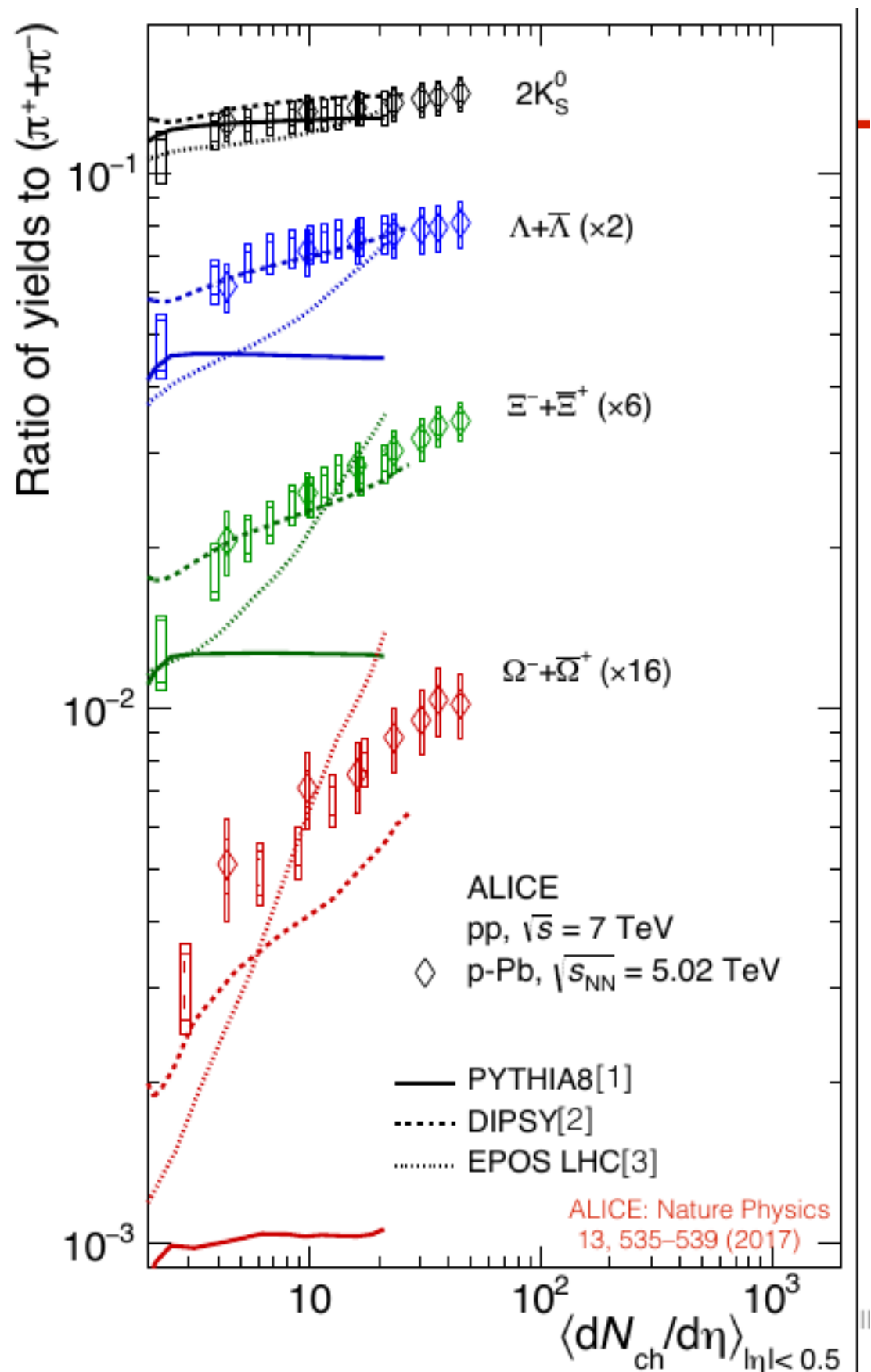
Direct photons

Final state interactions (non-hydro)

HL/HE-LHC workshops, preliminary, to be published



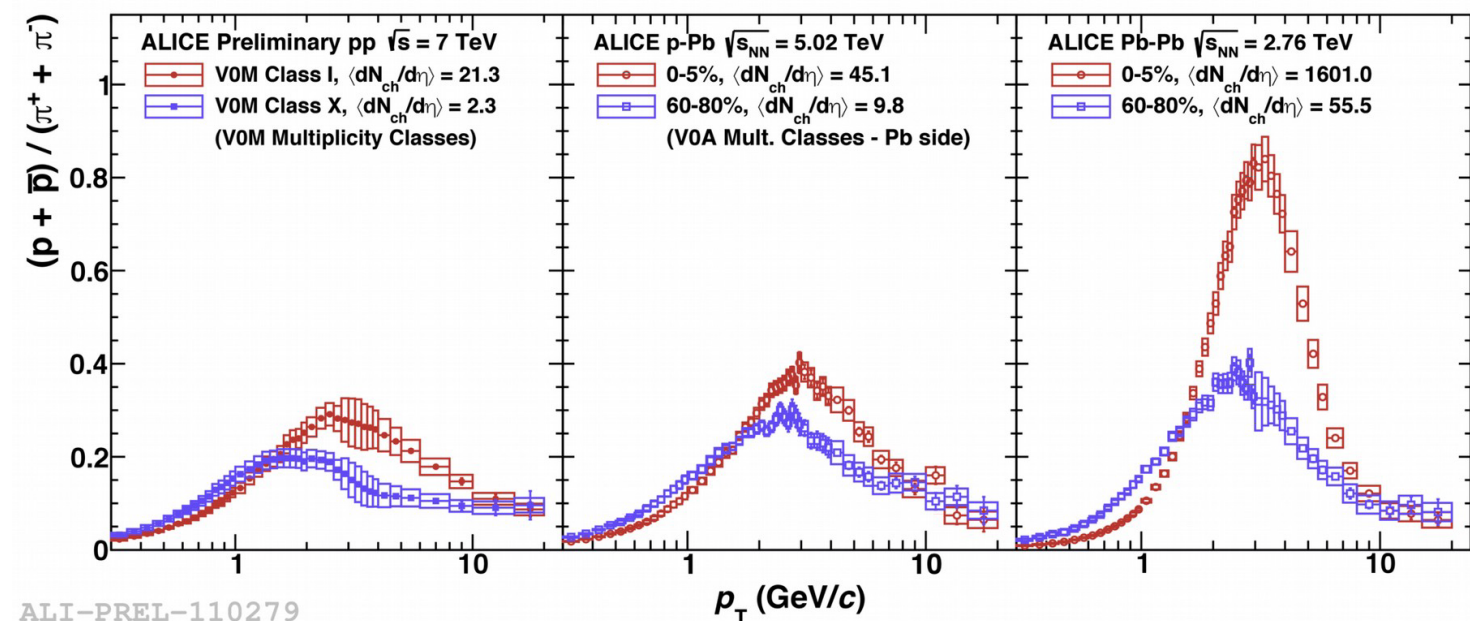
# Collective hadronisation:



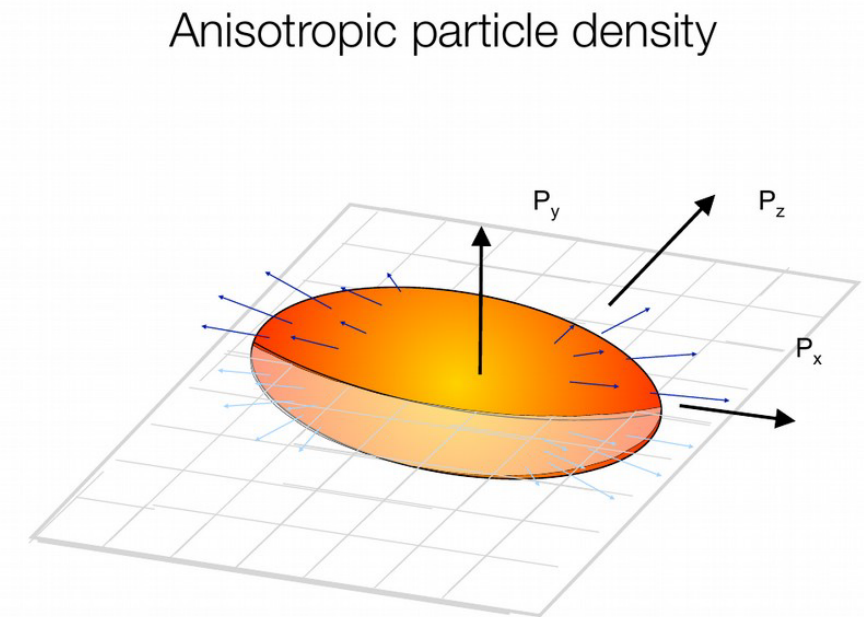
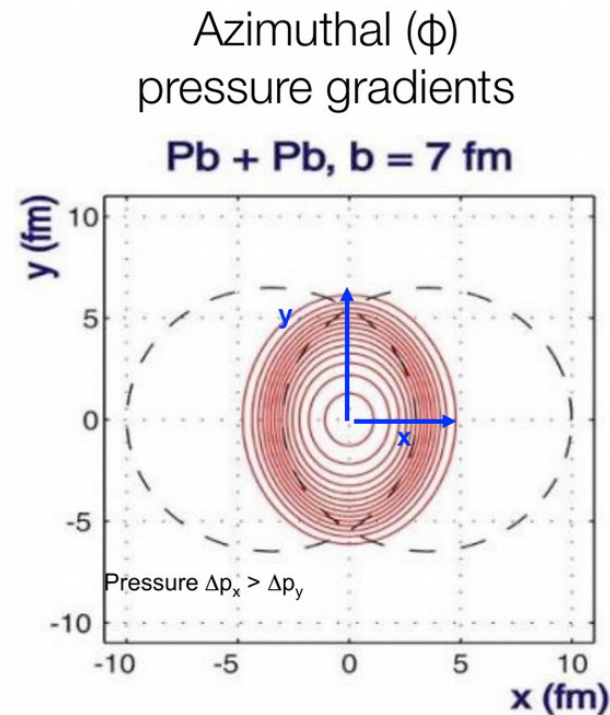
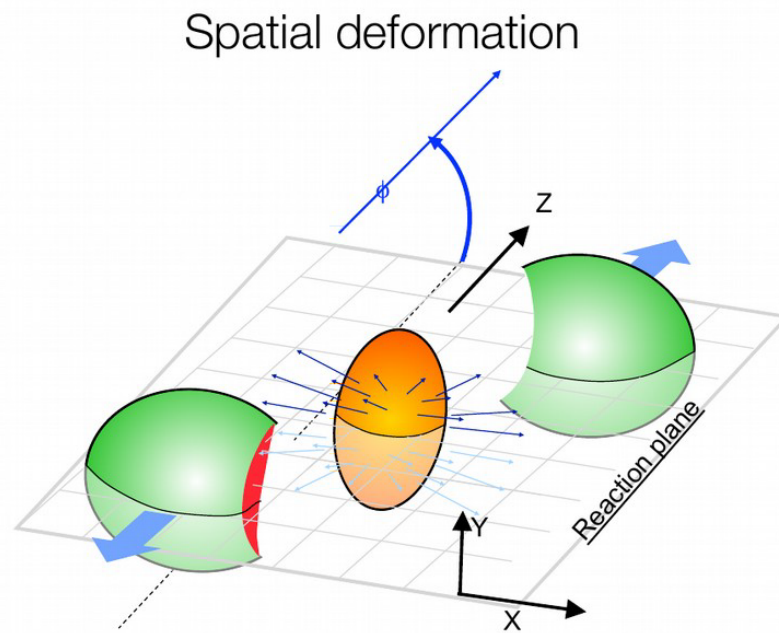
- Smooth increase of strange particles with respect to pions from pp to PbPb, when plotted as a function of multiplicity.
- Baryon/meson enhancement at intermediate  $p_T$ , from pp to PbPb.



Non-perturbative fragmentation: statistical, recombination, coalescence?



# Collective expansion:



$$\frac{dN}{d\phi} \propto 1 + 2v_1 \cos[\phi - \Psi_1] + 2v_2 \cos[2(\phi - \Psi_2)] + 2v_3 \cos[3(\phi - \Psi_3)] + \dots$$

- Fourier coefficients now measured via n-particle correlations:

$$\begin{aligned} \langle\langle e^{in(\phi_1 + \phi_2 - \phi_3 - \phi_4)} \rangle\rangle &\equiv \langle e^{in(\phi_1 + \phi_2 - \phi_3 - \phi_4)} \rangle - \langle e^{in(\phi_1 - \phi_3)} \rangle \langle e^{in(\phi_2 - \phi_4)} \rangle - \langle e^{in(\phi_1 - \phi_4)} \rangle \langle e^{in(\phi_2 - \phi_3)} \rangle \\ c_2\{4\} &= \langle\langle e^{in(\phi_1 + \phi_2 - \phi_3 - \phi_4)} \rangle\rangle = -v_n^4 + O\left(\frac{1}{N^3} + \frac{v_{2n}^2}{N^2}\right) \end{aligned}$$

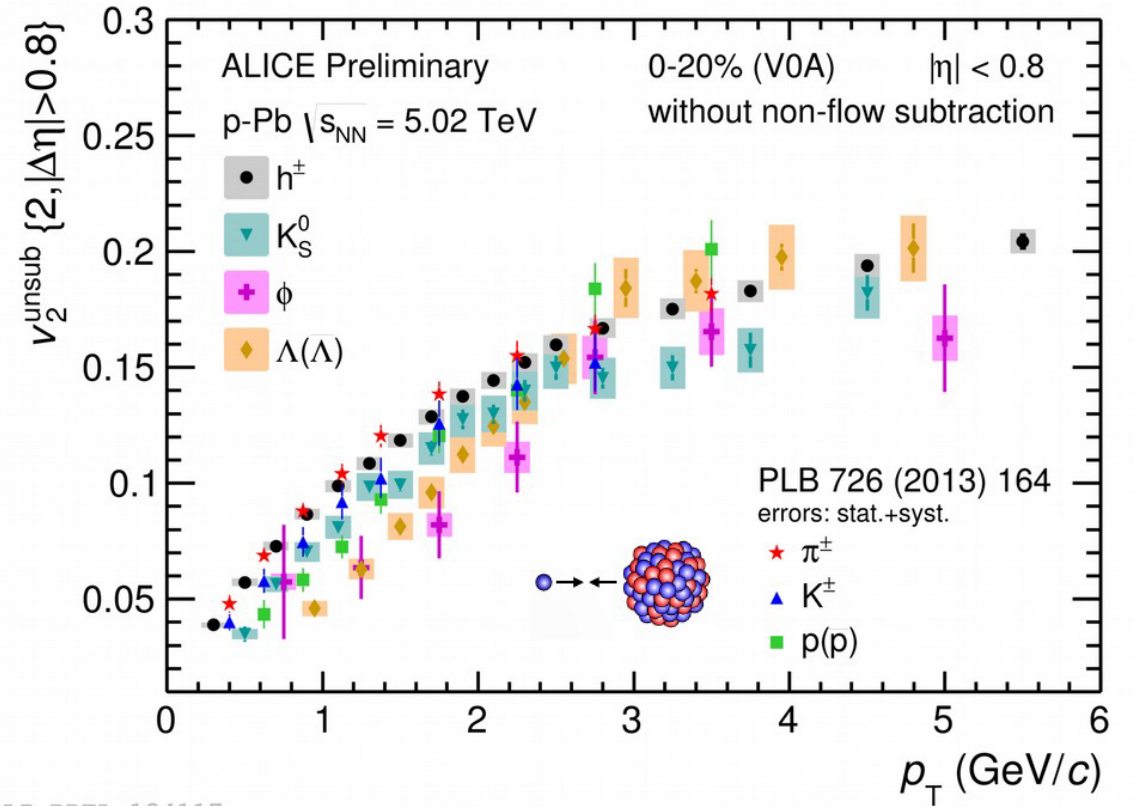
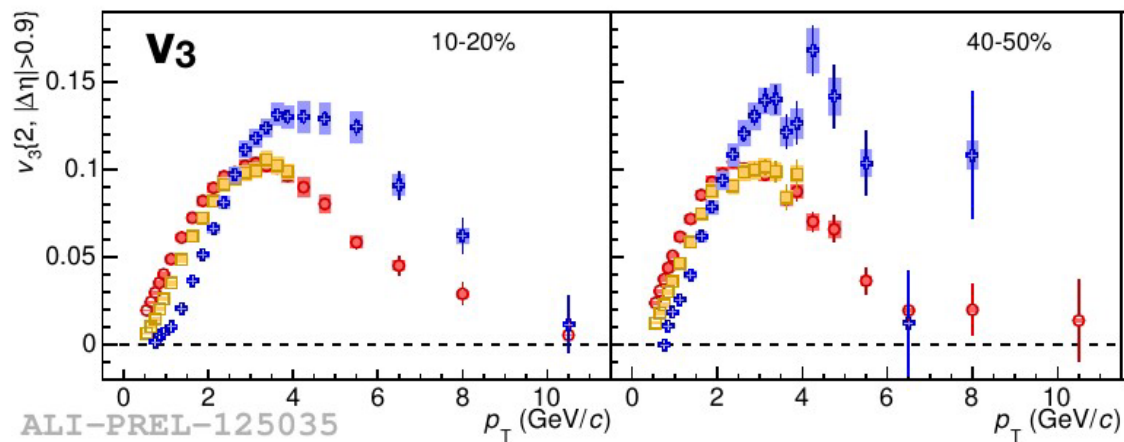
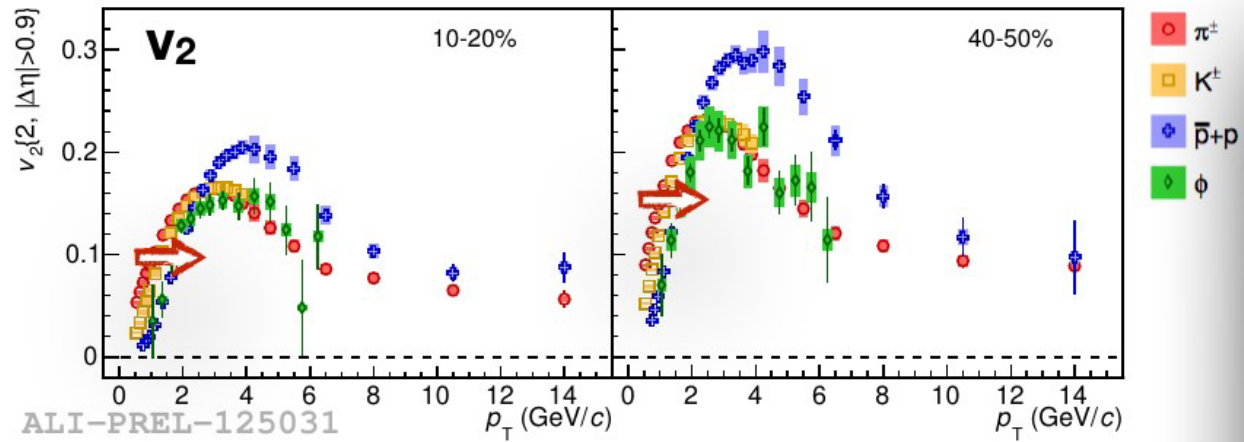
$$V_{n\Delta}(p_T^a, p_T^b) \equiv \langle \cos n(\phi^a - \phi^b) \rangle \stackrel{?}{=} v_n(p_T^a) \times v_n(p_T^b)$$

- Factorisation in ideal hydro, broken by ebe fluctuations (damped by viscosity).

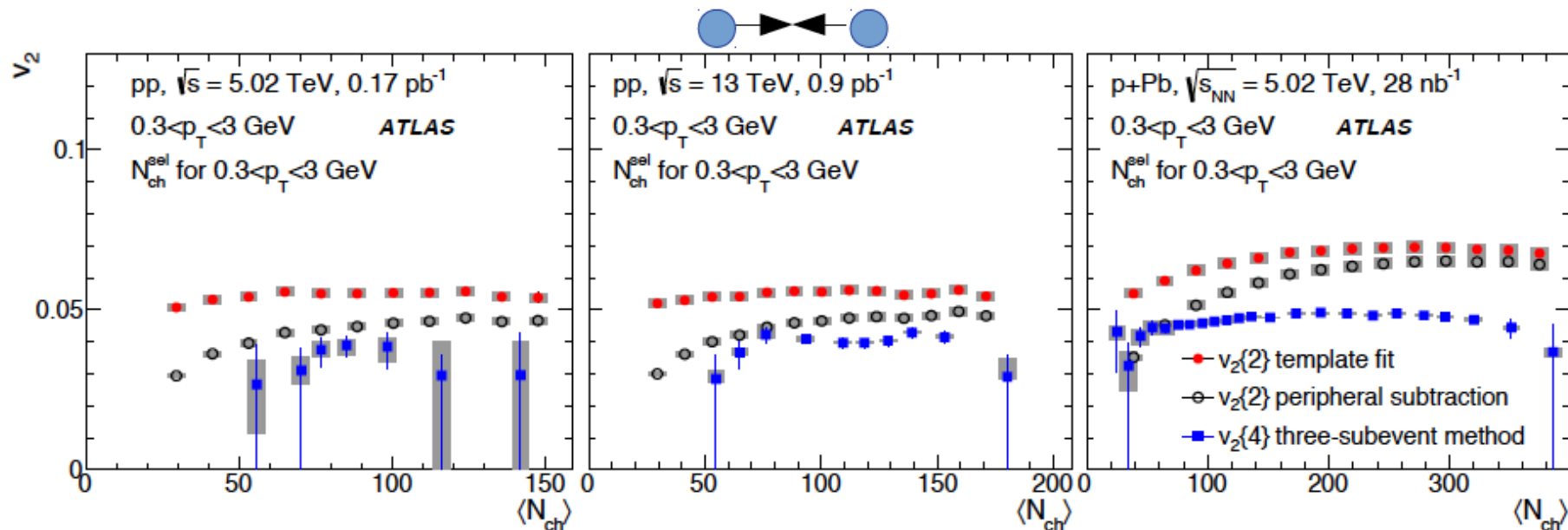


# Collective expansion:

ALICE Preliminary  
Pb-Pb  $\sqrt{s_{NN}} = 5.02$  TeV  
 $|\eta| < 0.5$

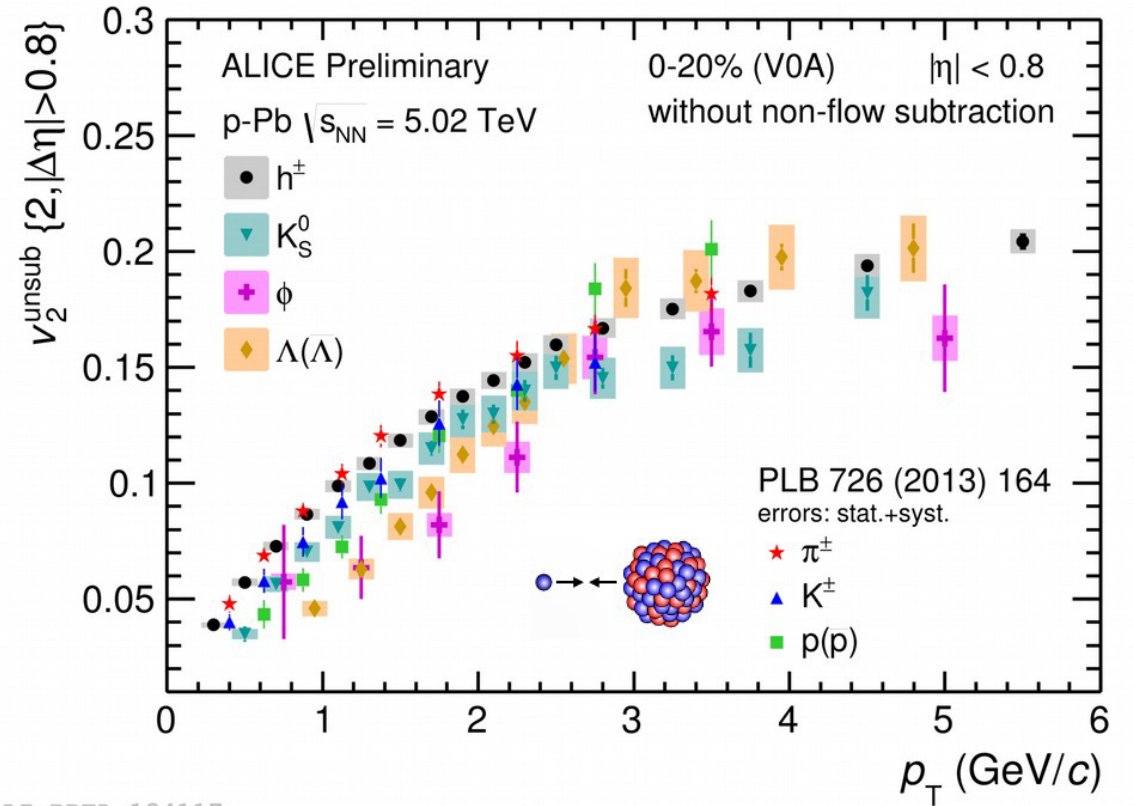
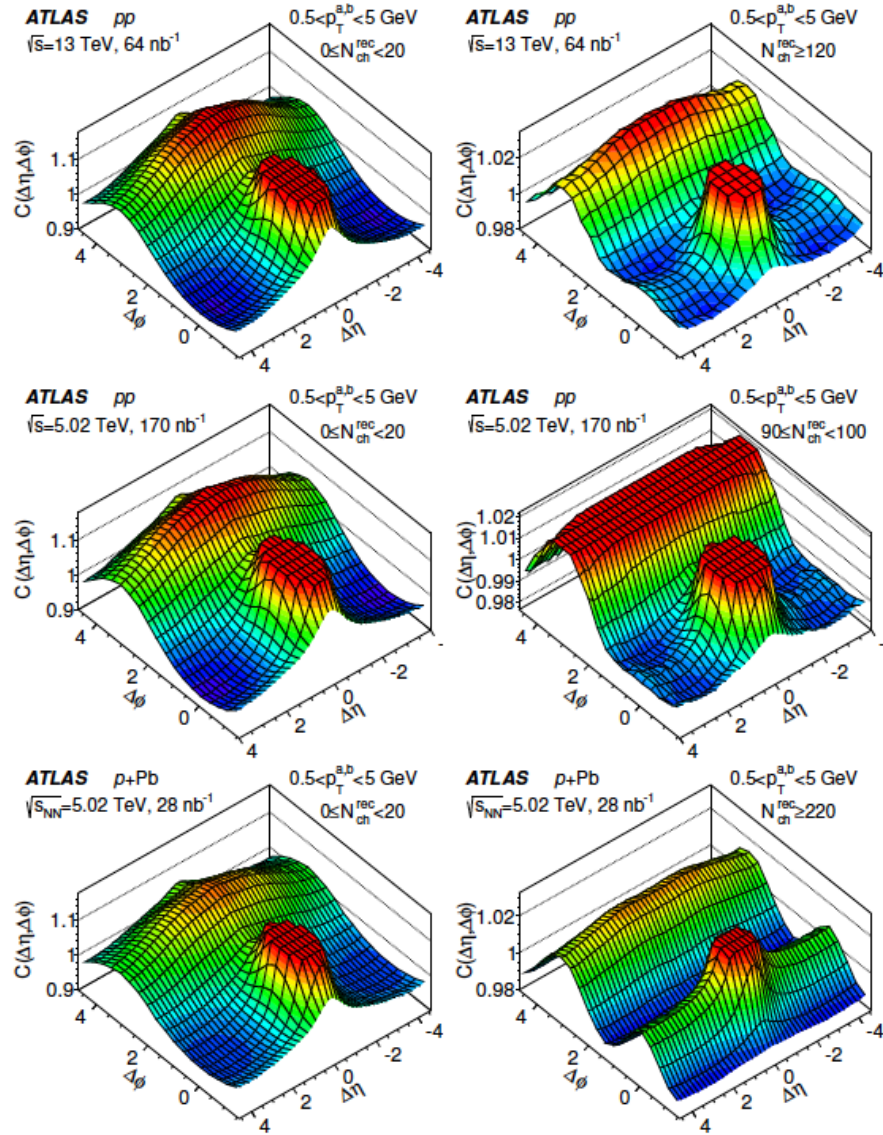


● Mass ordering for Fourier coefficients, characteristic of hydro.

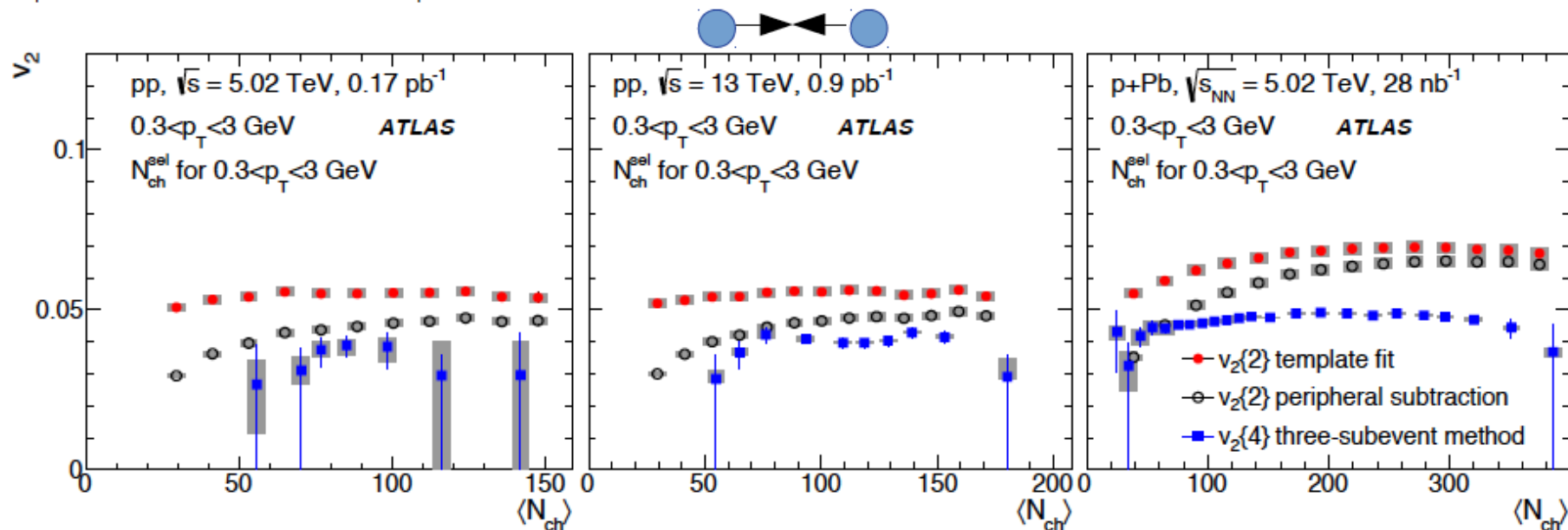


# Collective expansion:

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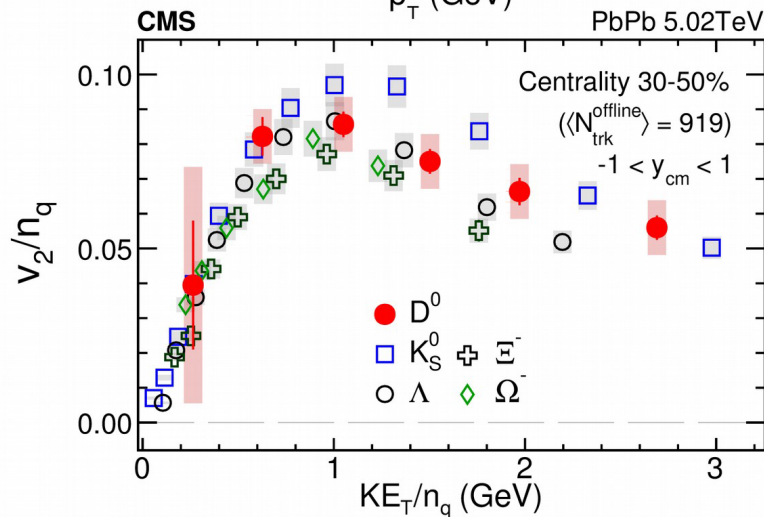
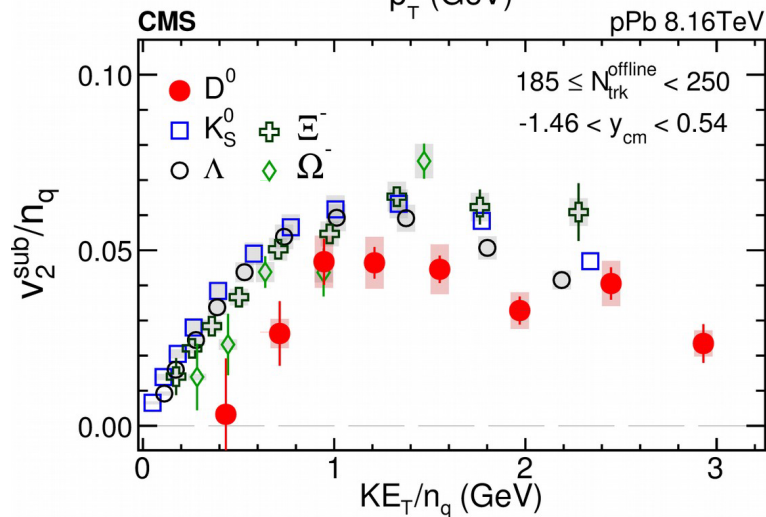
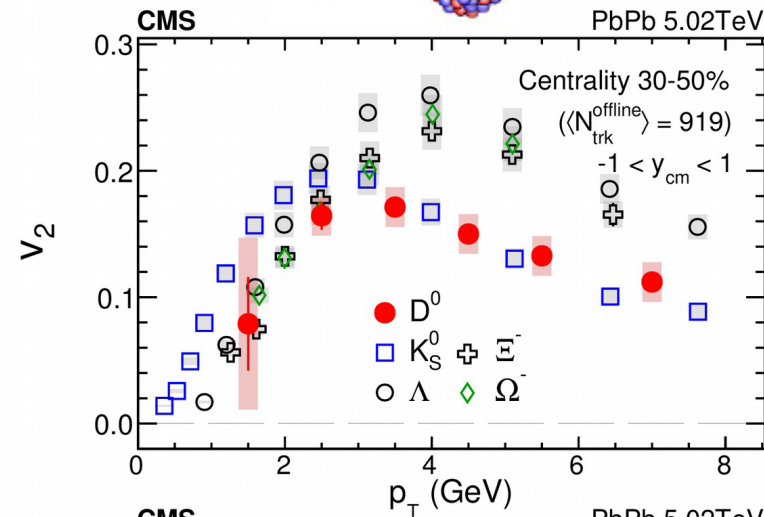
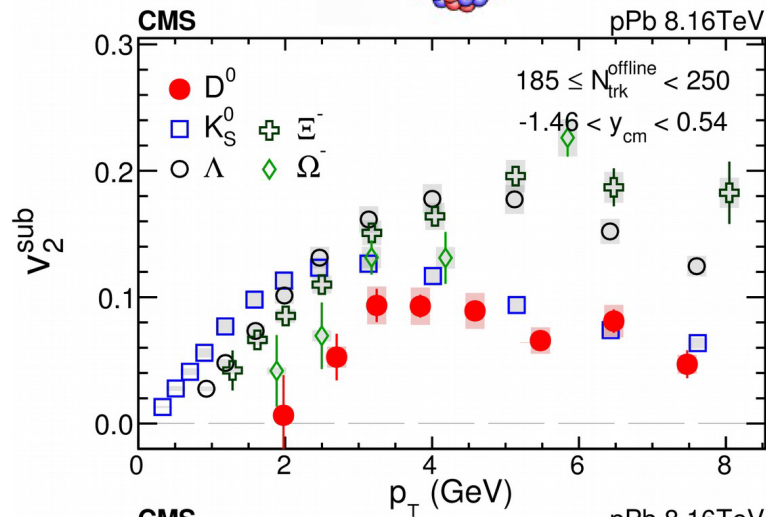
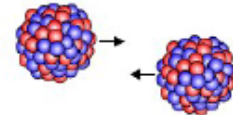
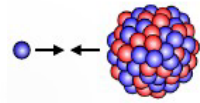
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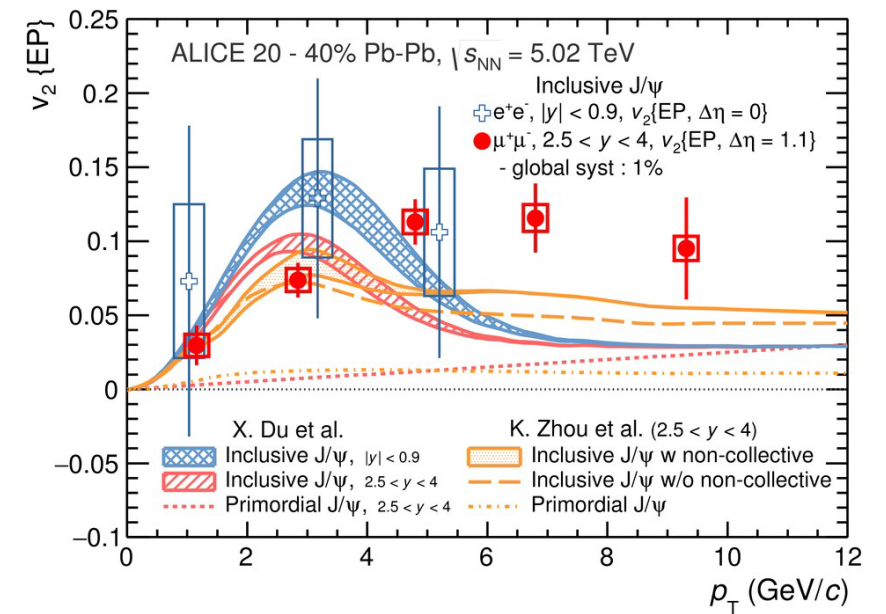
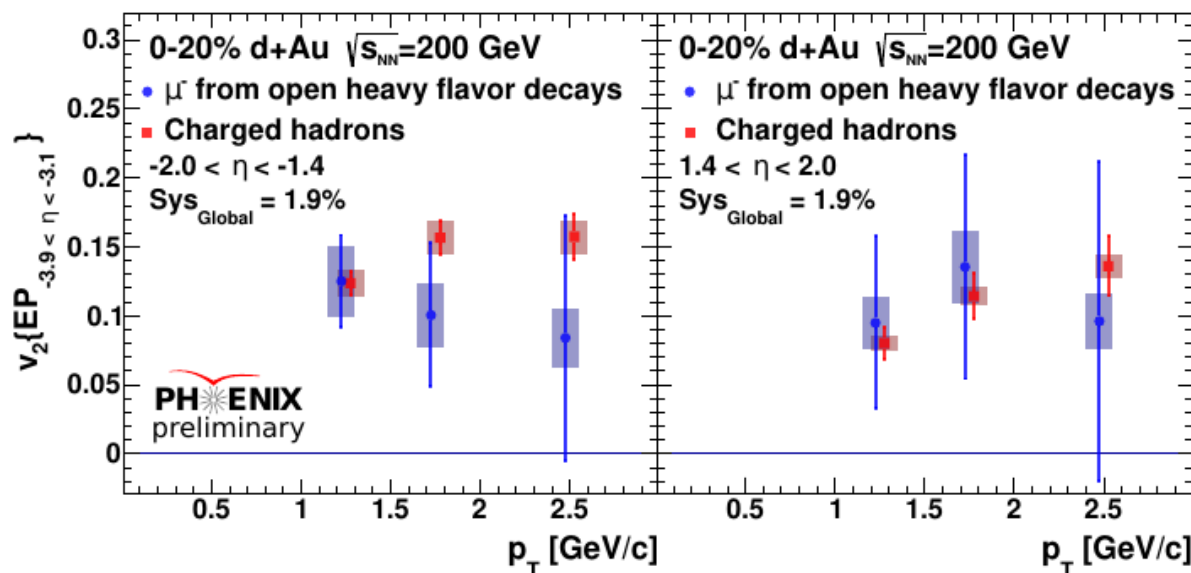
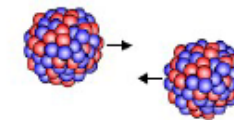
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# Collective expansion:

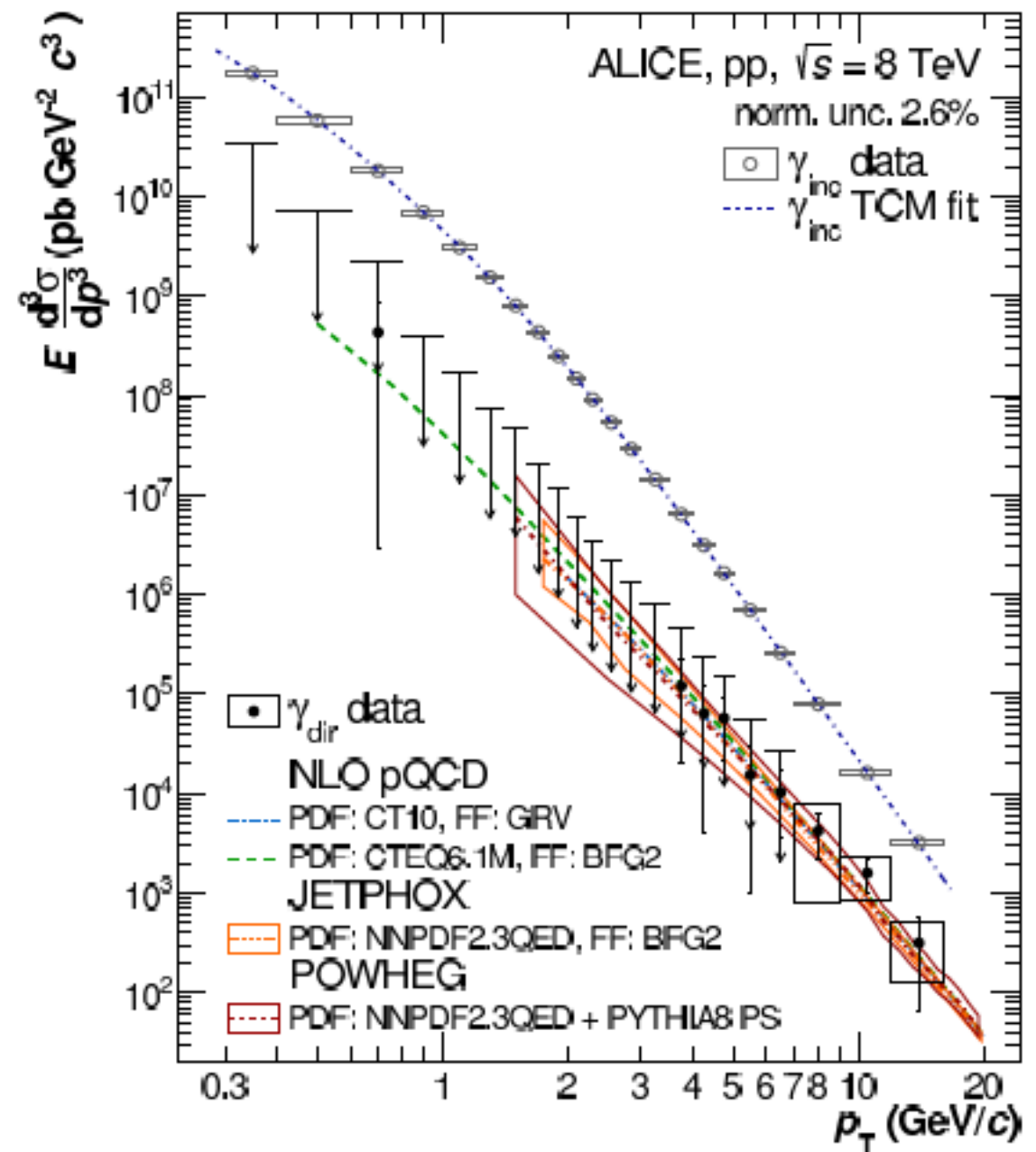
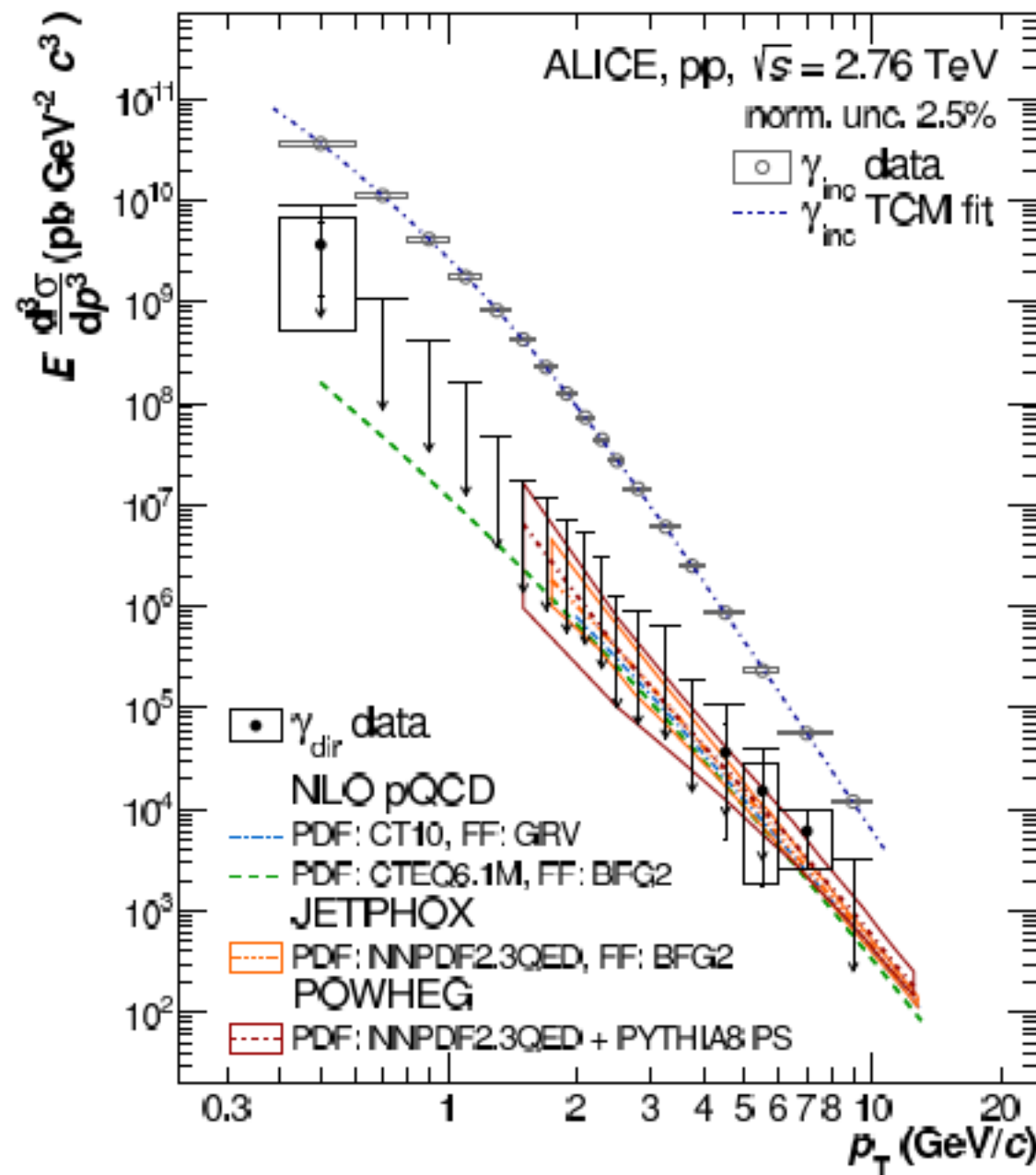


- Charm “flow” is used to extract the diffusion coefficient of heavy quarks in the QGP, is sizeable in pPb.



Nonzero  $v_2$  for heavy flavor in d+Au

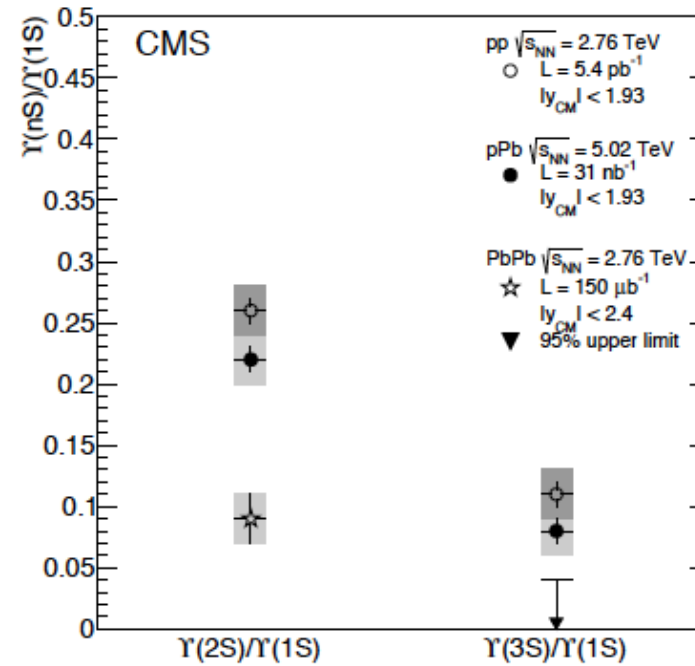
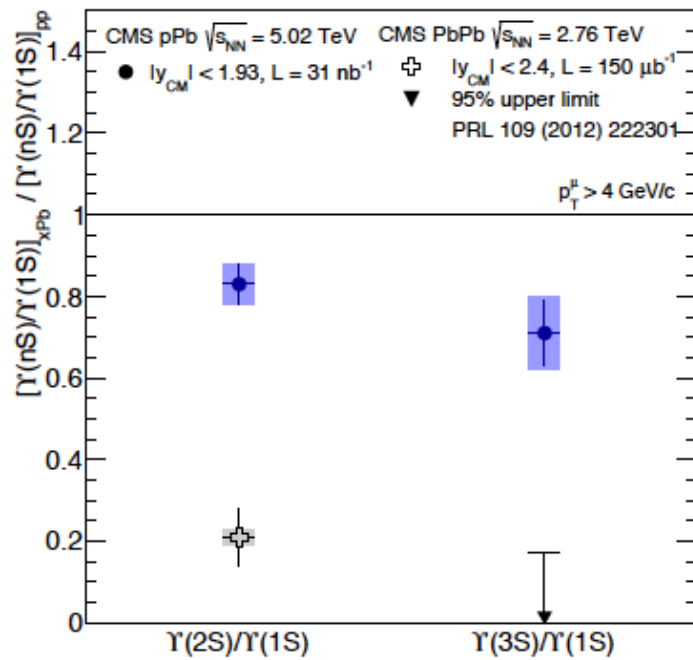
# Direct photons:



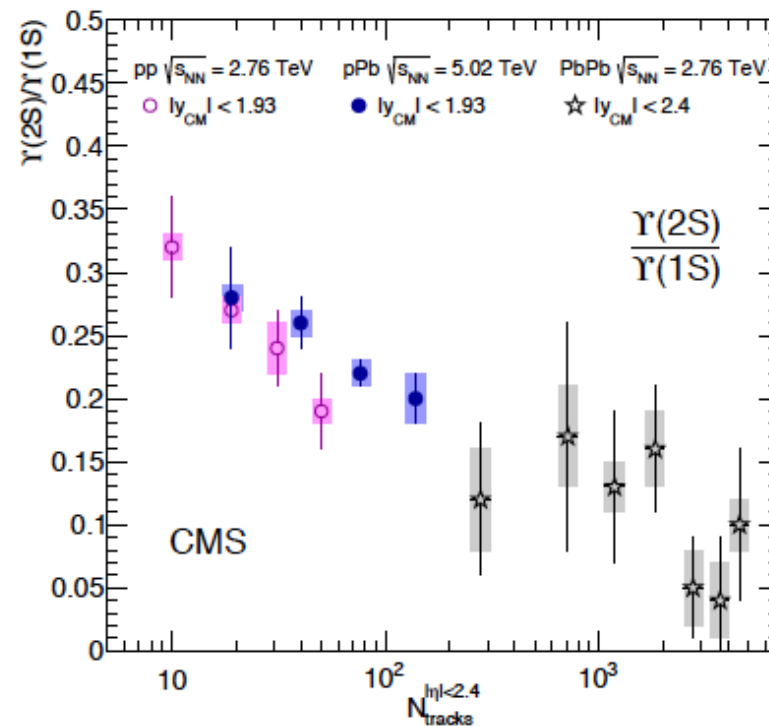
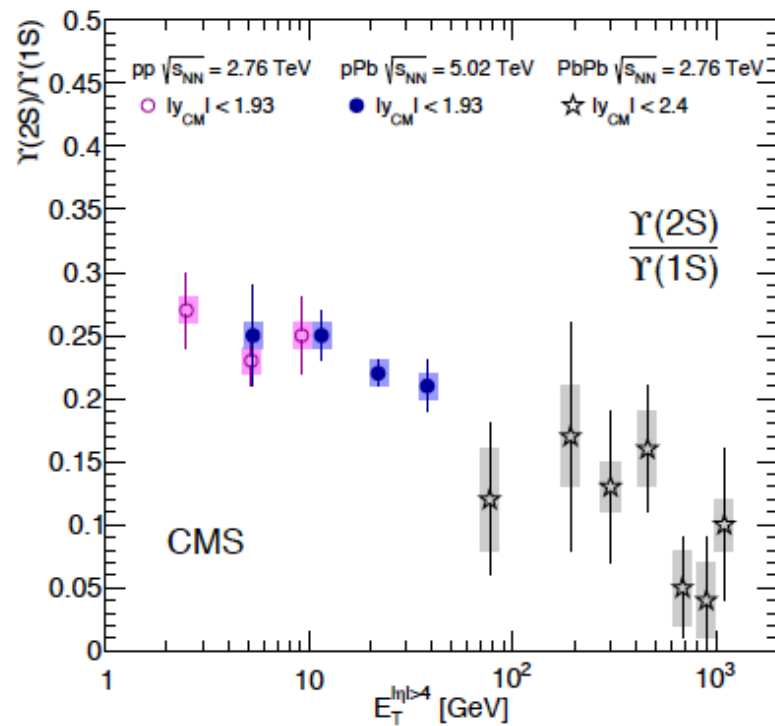
- Direct photon production in pp compatible with pQCD expectations, though room for other origins (evident in PbPb).



# Final state effects:



13 | 2.6300

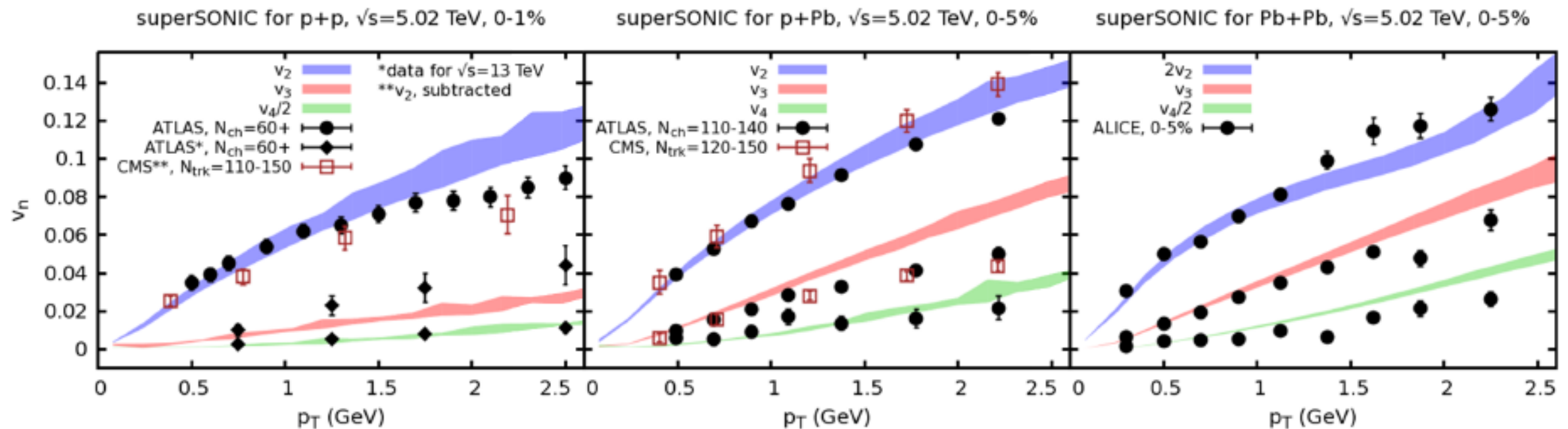


- The relative suppression of bottomonium states in PbPb was interpreted as due to Debye screening in the plasma: thermometer.

- The same effect has been observed in pPb to be smooth with increasing hadronic activity.

# The amazing hydro:

- Viscous hydro works in all three systems: pp to pPb to PbPb.

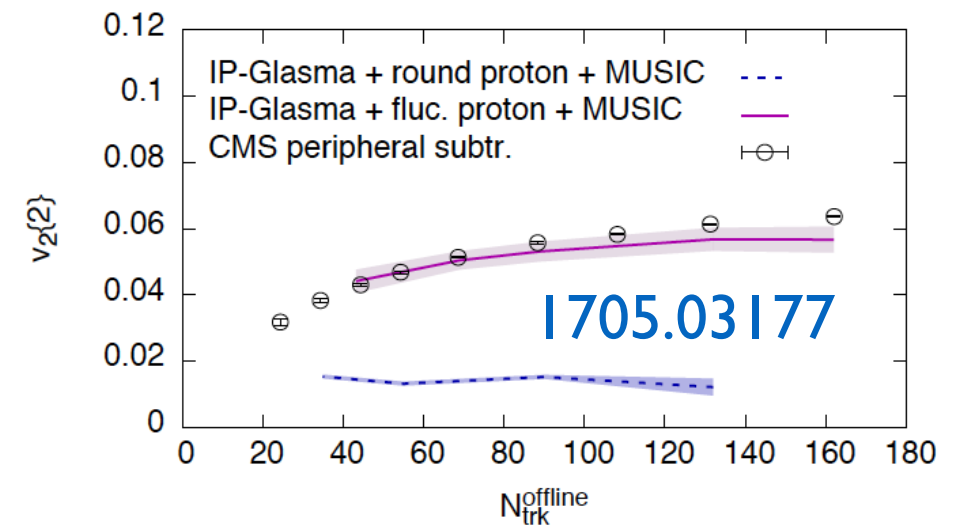
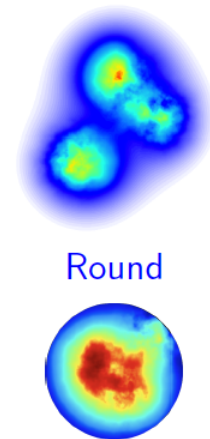


1701.07145, proton as 3 hot spots

FIG. 2. Elliptic ( $v_2$ ), triangular ( $v_3$ ) and quadrupolar ( $v_4$ ) flow coefficients from superSONIC simulations (bands) compared to experimental data from ATLAS, CMS and ALICE (symbols) for p+p (left panel), p+Pb (center panel) and Pb+Pb (right panel) collisions at  $\sqrt{s} = 5.02$  TeV [58–62]. Simulation parameters used were  $\frac{\eta}{s} = 0.08$  and  $\frac{\zeta}{s} = 0.01$  for all systems. Note that ATLAS results for  $v_3, v_4$  are only available for  $\sqrt{s} = 13$  TeV, while all simulation results are for  $\sqrt{s} = 5.02$  TeV.

- But this is non trivial: subnucleon dof's in the proton (hot spots).

Fluctuations



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See the talk by François Gelis.

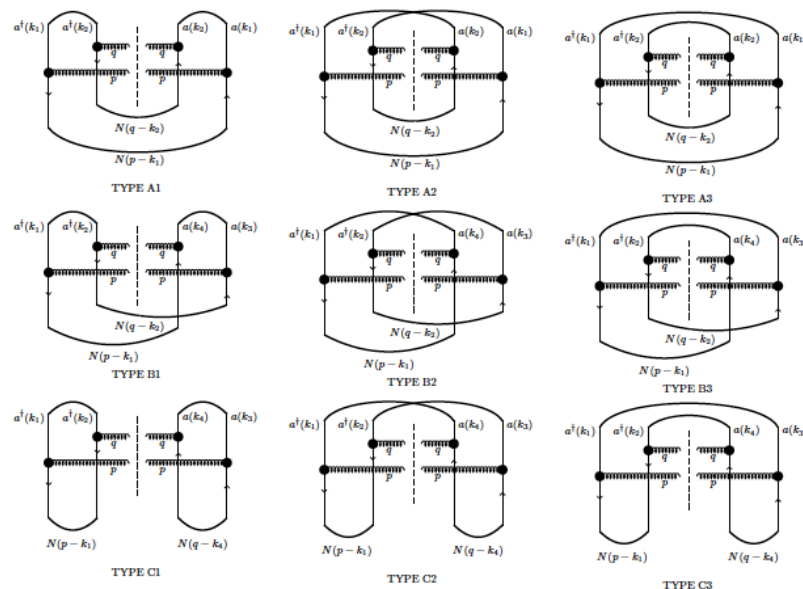
# CGC:

- Several explanations for the ridge proposed in the CGC:
  - Assume that the final state carries the imprint of initial-state correlations;
  - Use that the CGC wave function is rapidity invariant over  $Y \propto \ln(1/x)$  (we resum terms  $\alpha_s \ln(1/x) = \alpha_s Y \sim \ln$  coming from the  $1/x$  soft divergence).

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 succesful  
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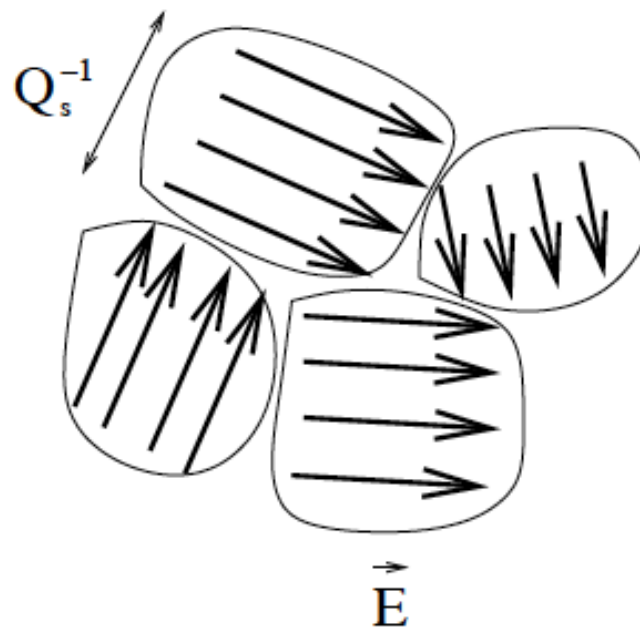
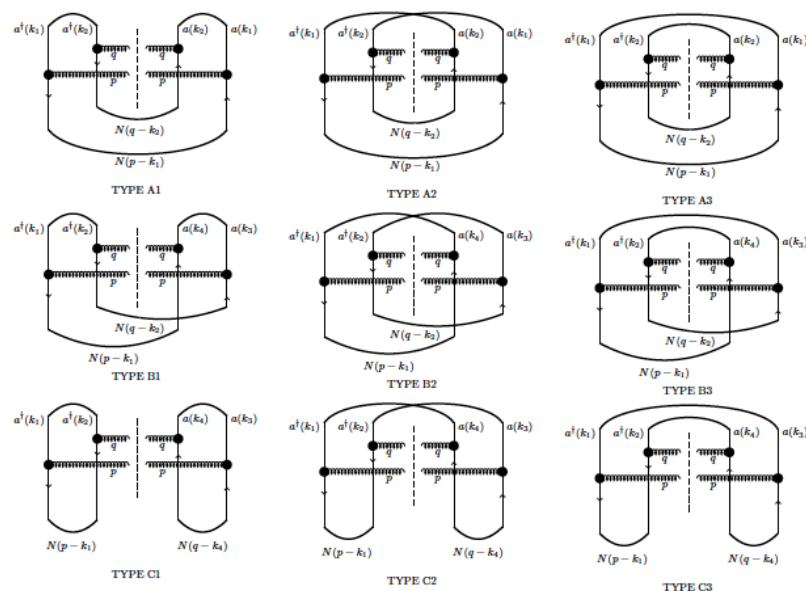


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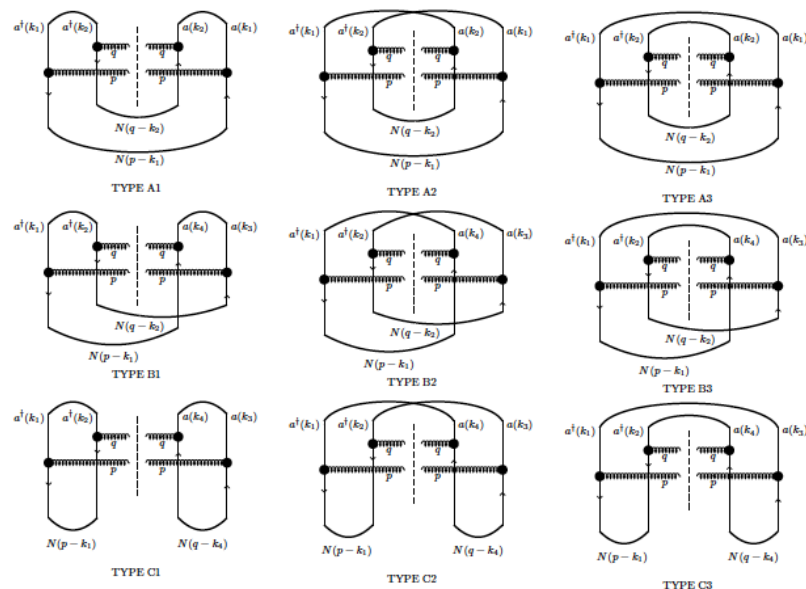
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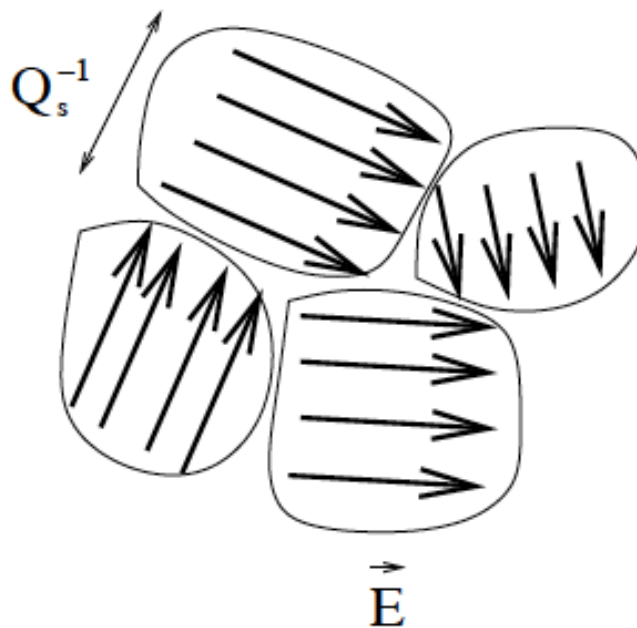
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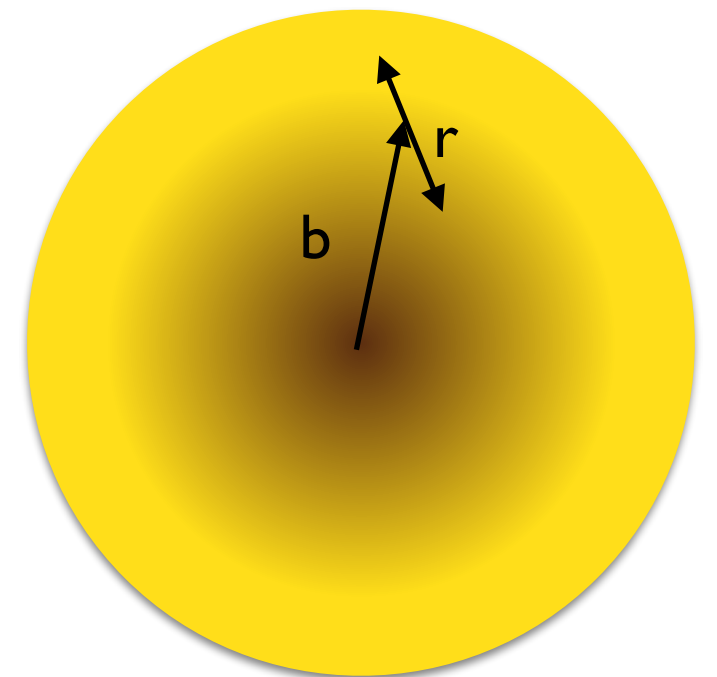
- “Glasma graphs”: successful phenomenology (Dusling-Gelis-Jalilian-Marian-Lappi-McLerran-Venugopalan, Kovchegov-Werpteny).



- Local anisotropy of target fields (Kovner-Lublinsky, Dumitru-McLerran-Skokov).



- Spatial variation of partonic density (Levin-Rezaeian-Gotsman).



# An example: two quarks

- The two-particle inclusive cross section reads:

$$\frac{d\sigma}{dp^+ d^2p dq^+ d^2q} = \frac{1}{(2\pi)^6} \langle v | \Omega \hat{S}^\dagger \Omega^\dagger [ d_{\alpha, s_1}^\dagger(p^+, p) d_{\beta, s_2}^\dagger(q^+, q) d_{\beta, s_2}(q^+, q) d_{\alpha, s_1}(p^+, p) ] \Omega \hat{S} \Omega^\dagger | v \rangle$$

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operator that diagonalises perturbatively  
the Light Cone QCD Hamiltonian

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eikonal S-matrix

$\{d_{s_1}^\omega(k^+, k), d_{s_2}^{\dagger\zeta}(q^+, q)\} = (2\pi)^3 \delta^{\omega\zeta} \delta_{s_1 s_2} \delta(k^+ - q^+) \delta^{(2)}(k - q)$  quark cre/anni. operator

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$$\frac{d\sigma}{dp^+ d^2 p dq^+ d^2 q} = \frac{1}{(2\pi)^6} \langle v | \Omega \hat{S}^\dagger \Omega^\dagger [d_{\alpha, s_1}^\dagger(p^+, p) d_{\beta, s_2}^\dagger(q^+, q) d_{\beta, s_2}(q^+, q) d_{\alpha, s_1}(p^+, p)] \Omega \hat{S} \Omega^\dagger | v \rangle$$

operator that diagonalises perturbatively  
the Light Cone QCD Hamiltonian

valence state

eikonal S-matrix

$\{d_{s_1}^\omega(k^+, k), d_{s_2}^{\dagger\zeta}(q^+, q)\} = (2\pi)^3 \delta^{\omega\zeta} \delta_{s_1 s_2} \delta(k^+ - q^+) \delta^{(2)}(k - q)$  quark cre/anni. operator



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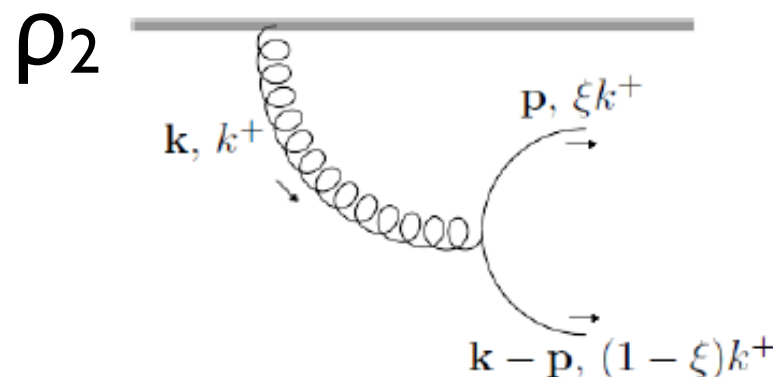
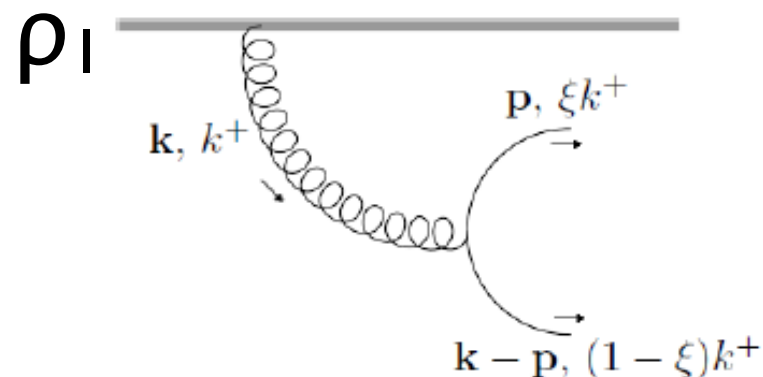
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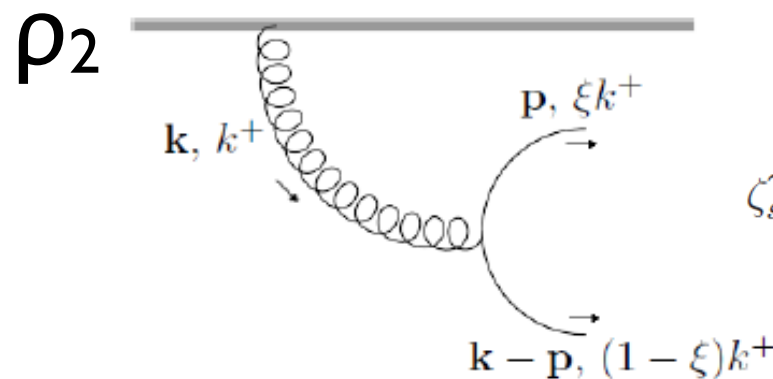
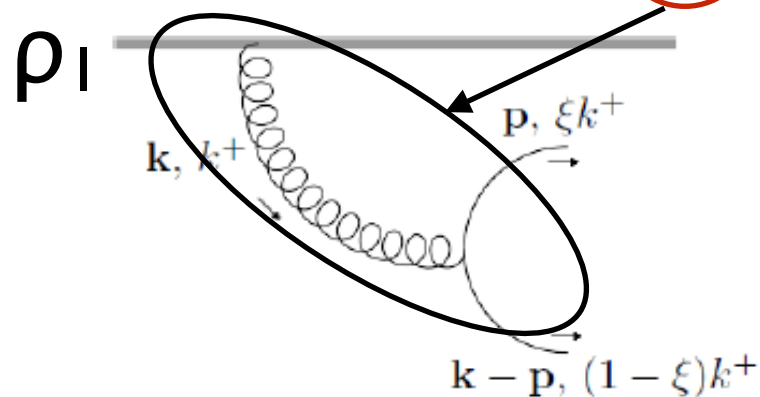
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$$\zeta_{s_1 s_2}^{\gamma \delta}(k^+, p, q, \alpha) = \tau_{\gamma \delta}^a \int \frac{d^2 k}{(2\pi)^2} \rho^a(k) \phi_{s_1 s_2}(k, p, q; \alpha)$$

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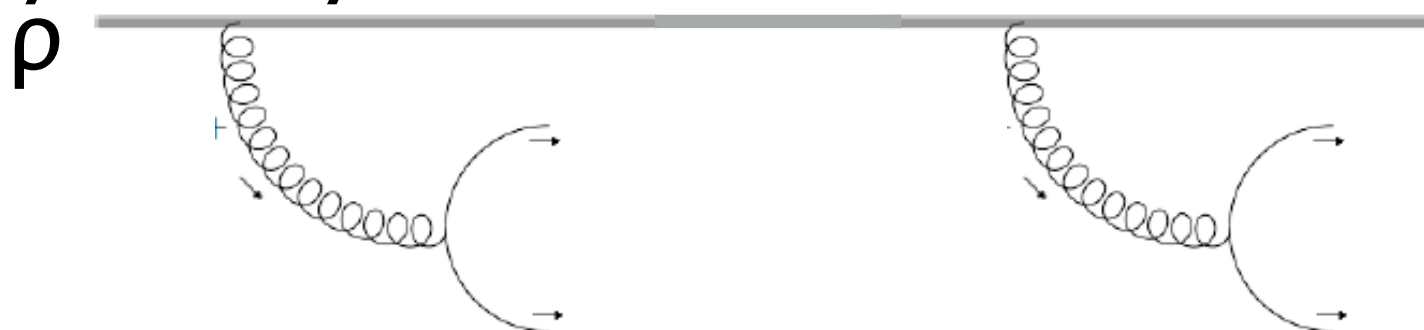
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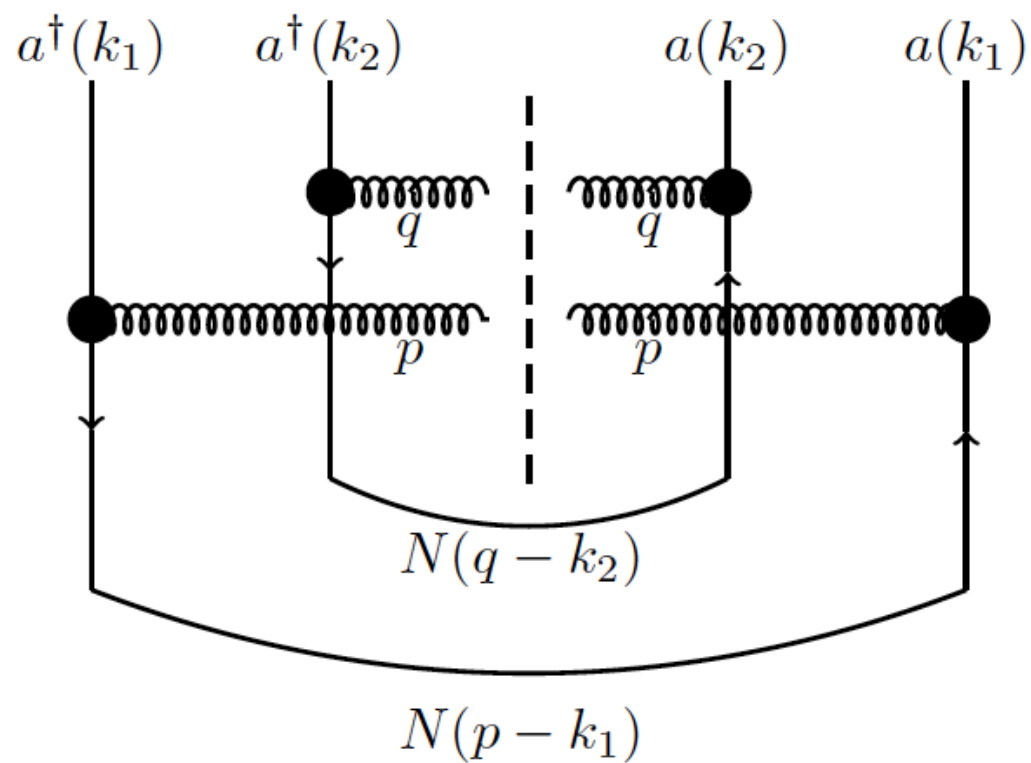
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- $\rho g \sim 1$ , so only density-enhanced contributions are taken i.e. NOT



# Glasma graphs for gluons (I):

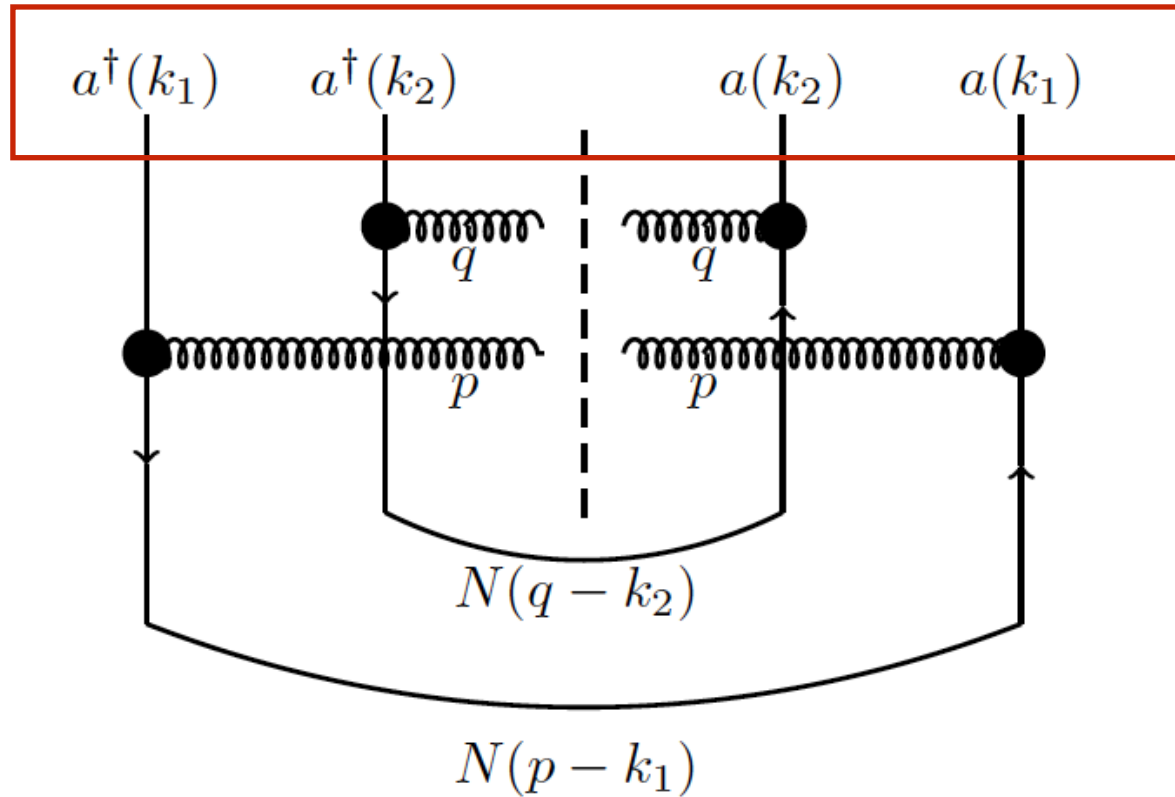
- The appearance of the ridge in the final state, within the glasma graph approach, can be traced to the Bose enhancement of gluons in the (rapidity invariant) wave function:



1503.07126,  
1509.03223

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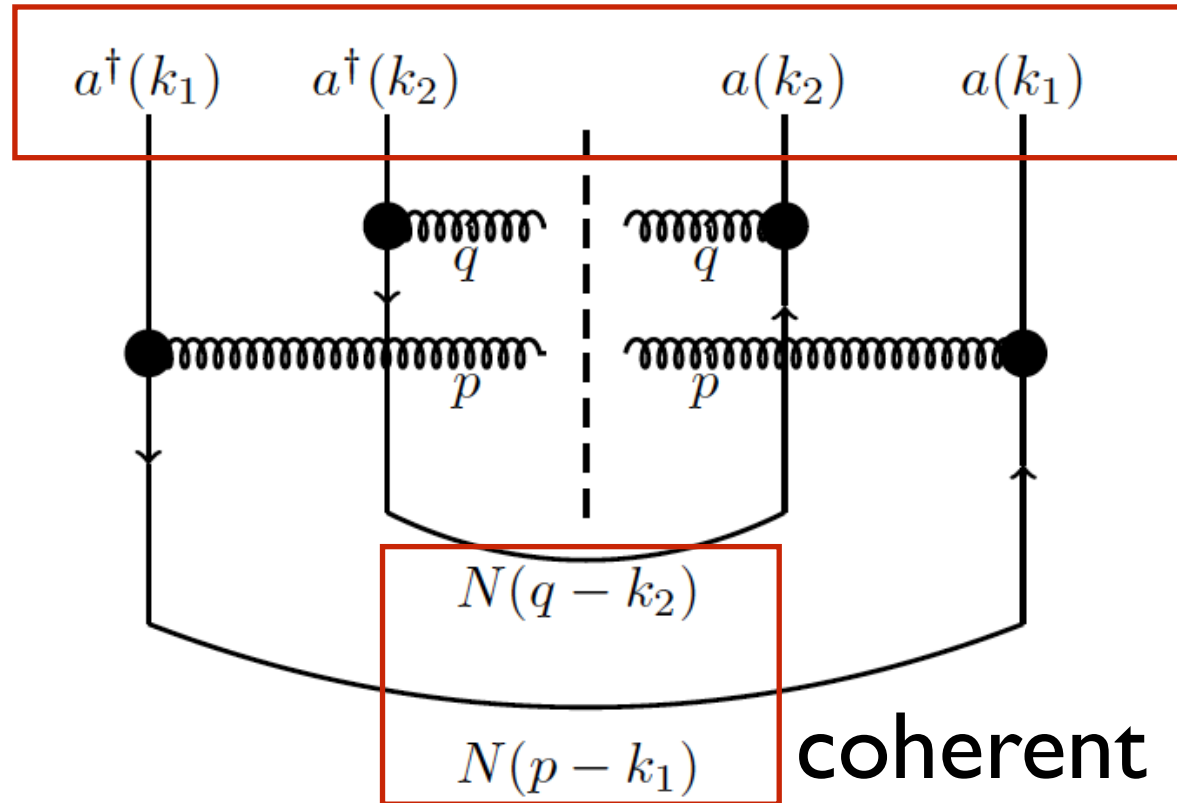
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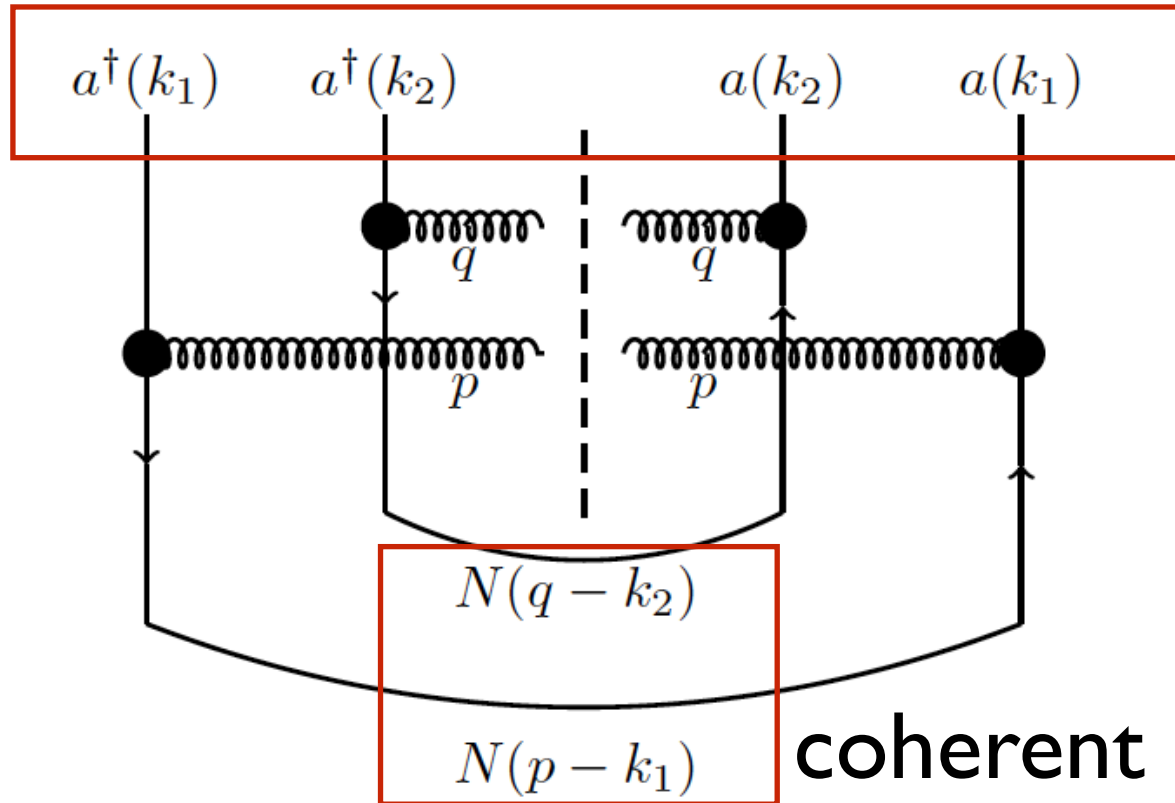
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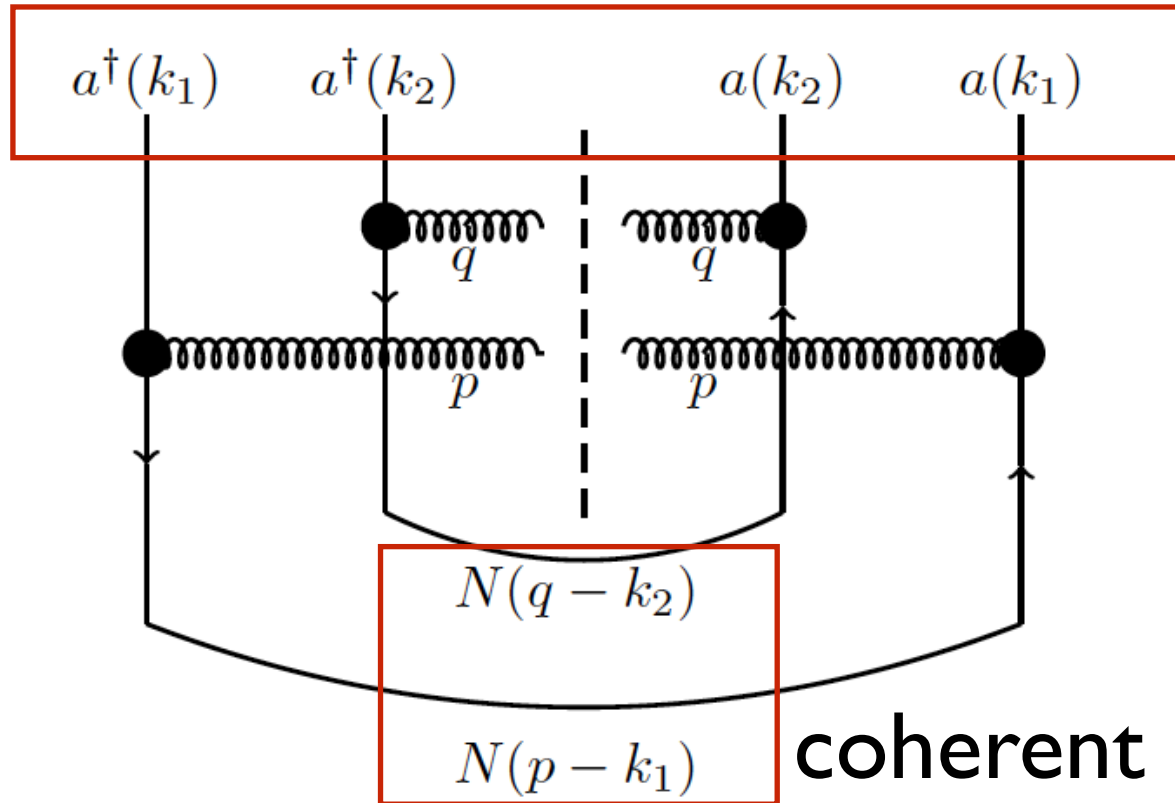
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$$C \int_{k_1, k_2} \langle in | a_a^{\dagger i}(k_1) a_b^{\dagger j}(k_2) a_a^k(k_1) a_b^l(k_2) | in \rangle \left[ \delta^{ik} - \frac{k_1^i k_1^k}{p^2} \right] \left[ \delta^{jl} - \frac{k_2^j k_2^l}{q^2} \right] N(p - k_1) N(q - k_2)$$



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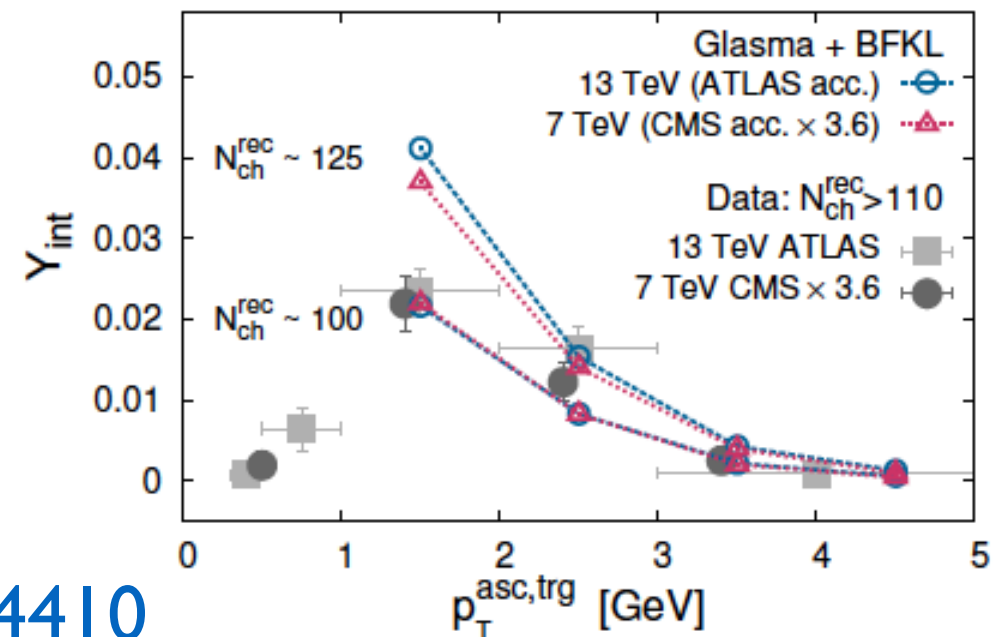
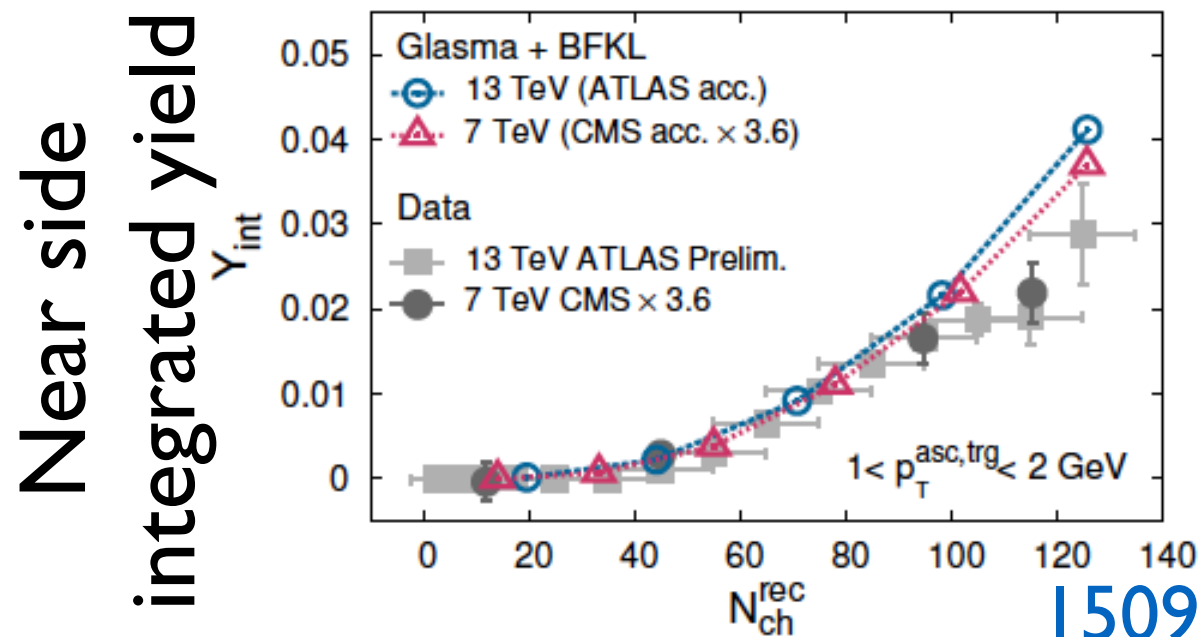
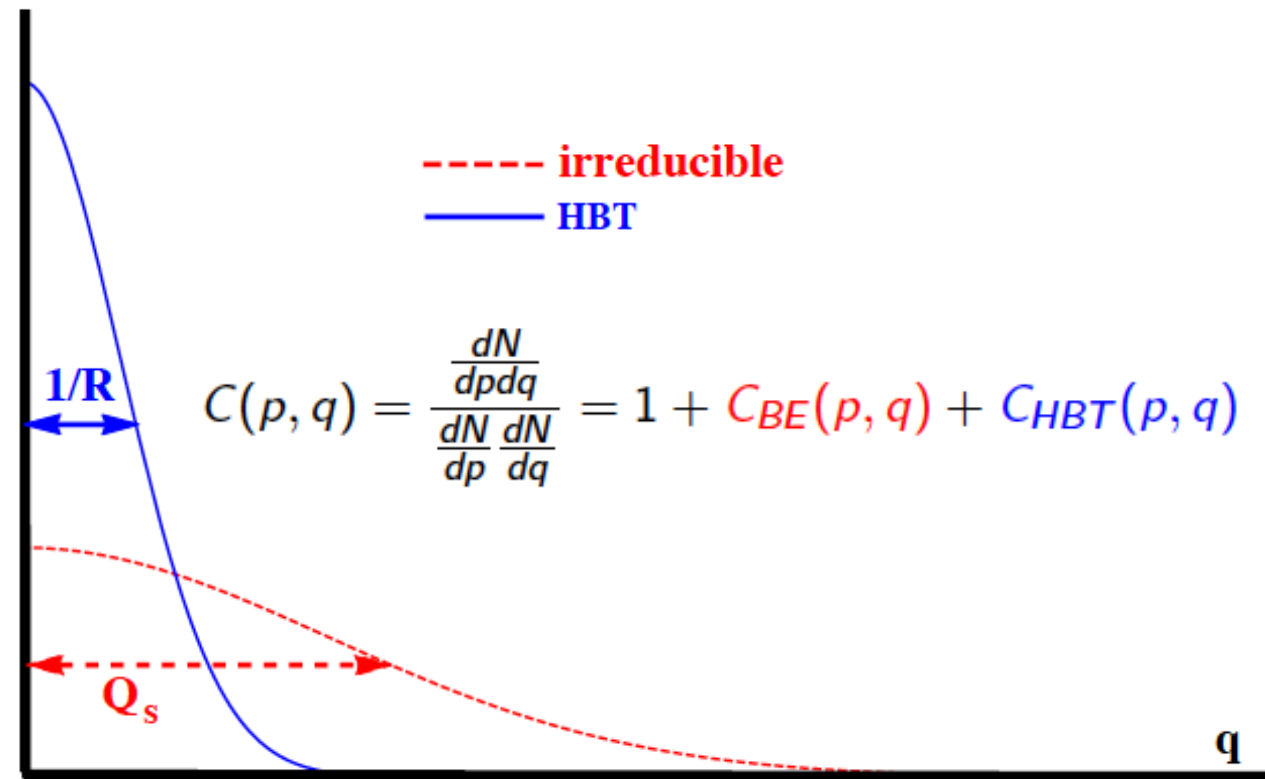
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$$D(k_1, k_2) = S^2 (N_c^2 - 1)^2 \frac{k_1^i k_1^k k_2^j k_2^l}{k_1^2 k_2^2} \frac{g^4 \mu^2(k_1) \mu^2(k_2)}{k_1^2 k_2^2} \left\{ 1 + \frac{1}{S(N_c^2 - 1)} \left[ \delta^{(2)}(k_1 - k_2) + \delta^{(2)}(k_1 + k_2) \right] \right\}$$

$$a^*(k) = a(-k)$$

# Glasma graphs for gluons (II):

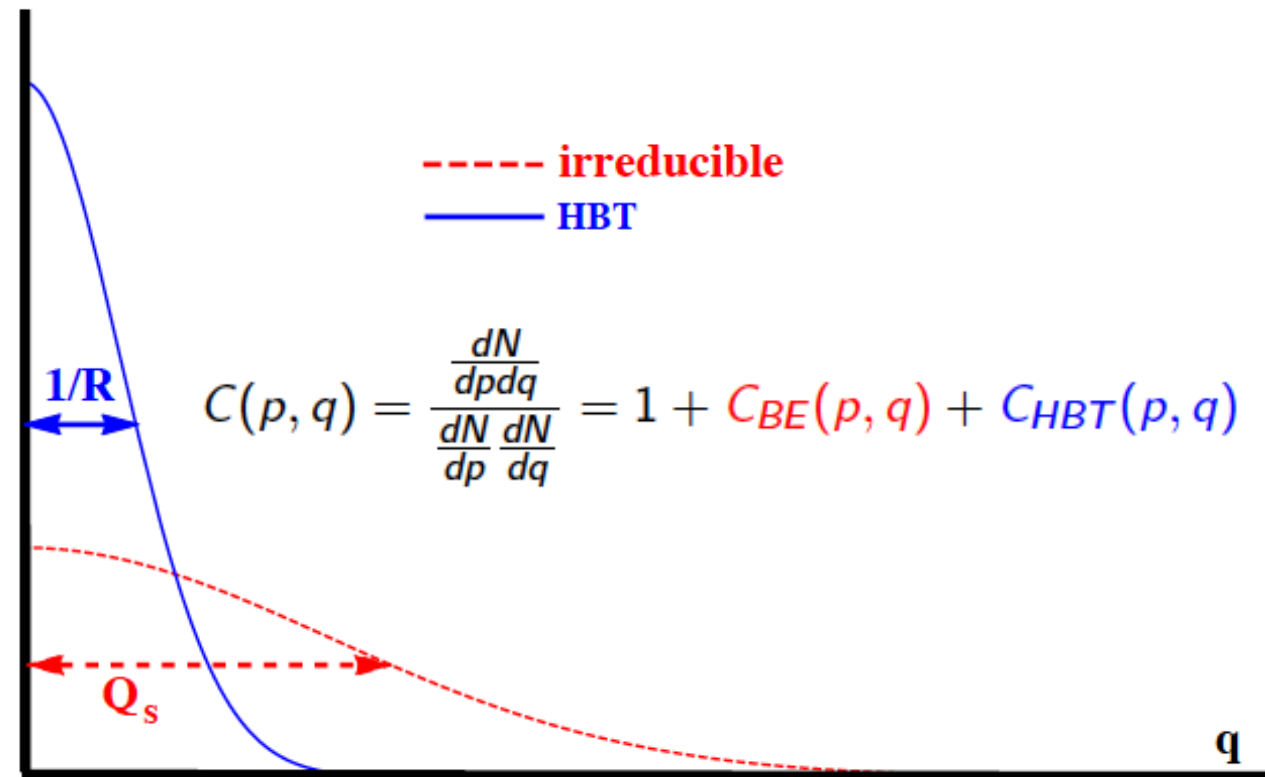
- It can be extended for **quarks** giving Pauli blocking (1610.03020): short range anticorrelation in the near side ridge.
- It contains information both on the 'source' size  $1/Q_s$  (**BE**, suppressed by the number of sources), and on the size of the distribution of 'sources'  $R$  (**HBT**).



1509.04410

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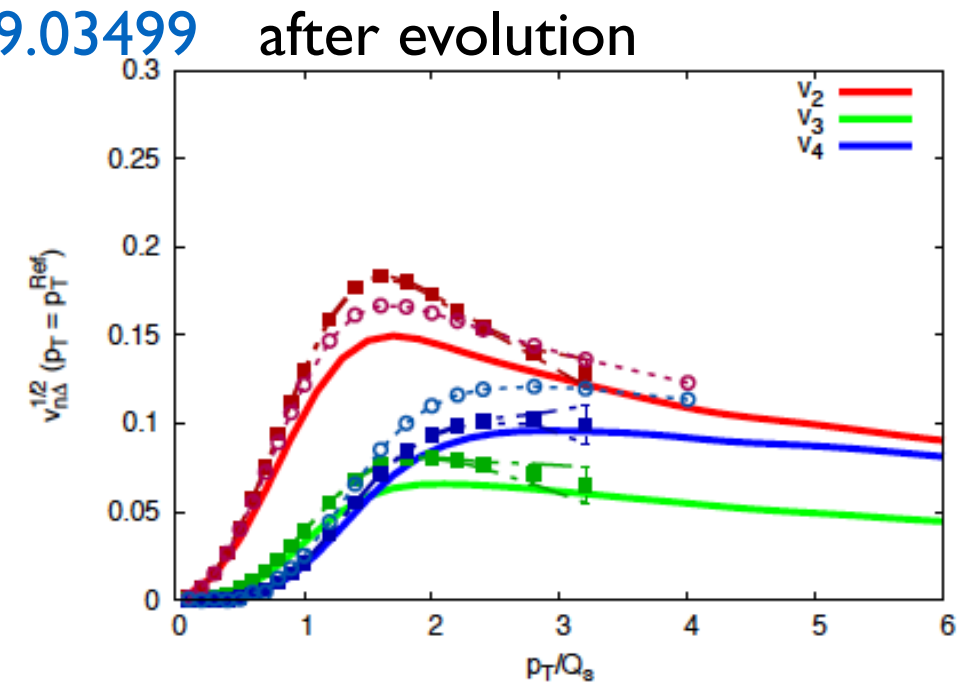
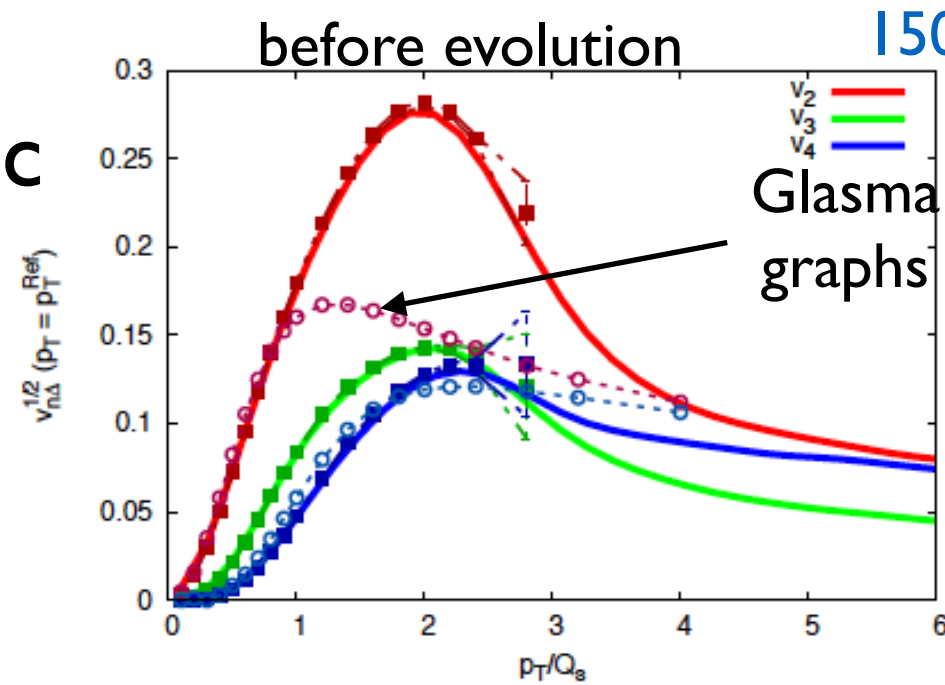
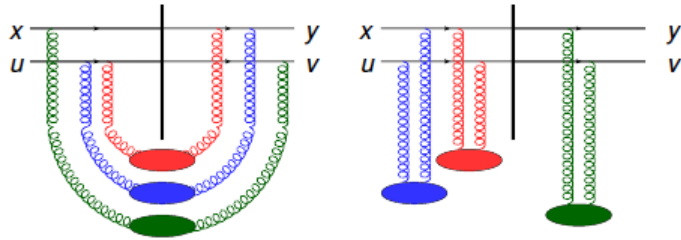


- **Limitations:**
  - S-matrices for rescattering of partons with the target are expanded in colour fields  $\Rightarrow$  **low density approximation**.
  - Gaussian (MV) isotropic colour correlations taken  $\Rightarrow$  **correlations subleading in  $N_c$ , no odd harmonics,  $c_2\{4\} > 0$ .**

$$\langle \rho_T^a(k) \rho_T^b(p) \rangle_T = (2\pi)^2 \lambda^2(k) \delta^{ab} \delta^{(2)}(k+p)$$

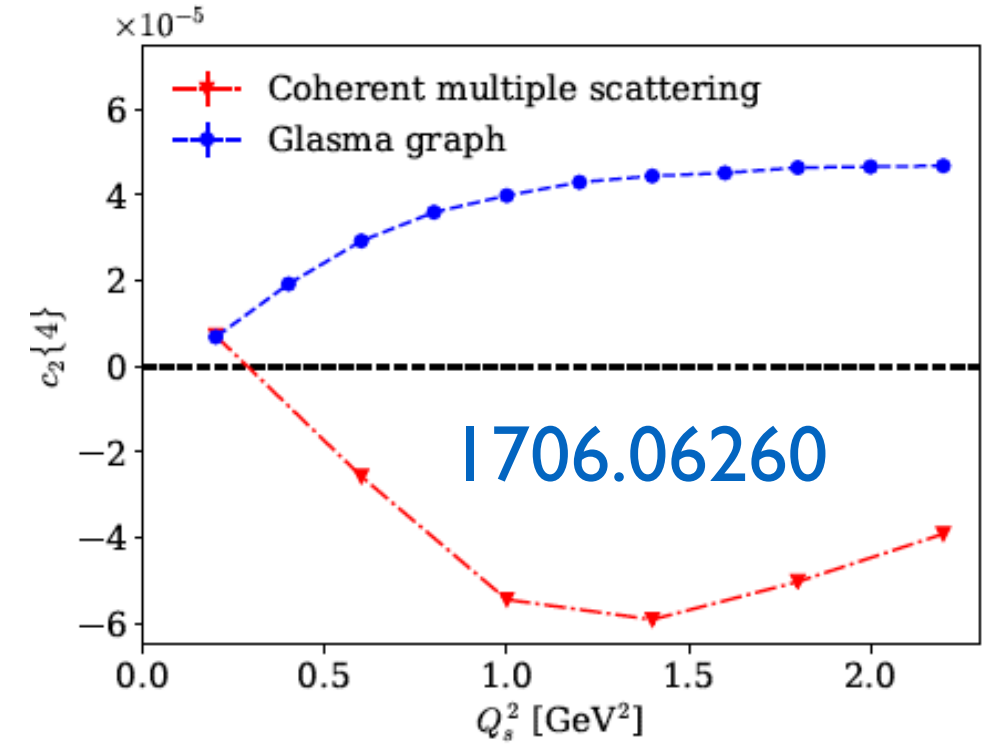
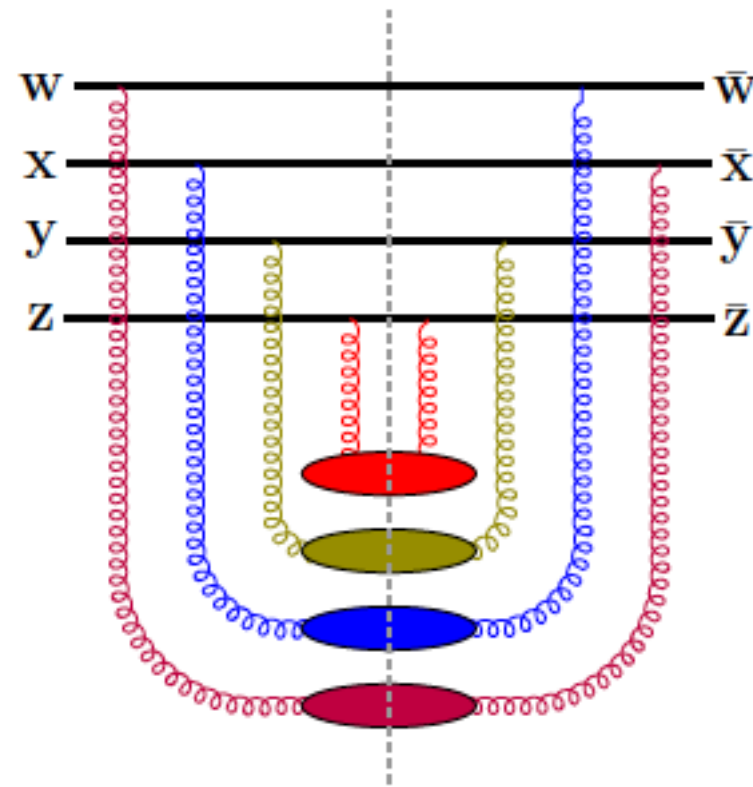
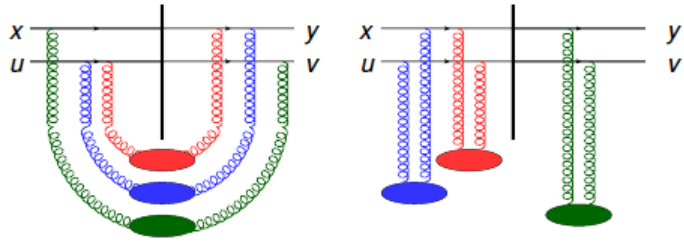
# Beyond glasma graphs (I):

- Density corrections: numeric and analytic work ([1612.07790](#); [1802.08166](#)).



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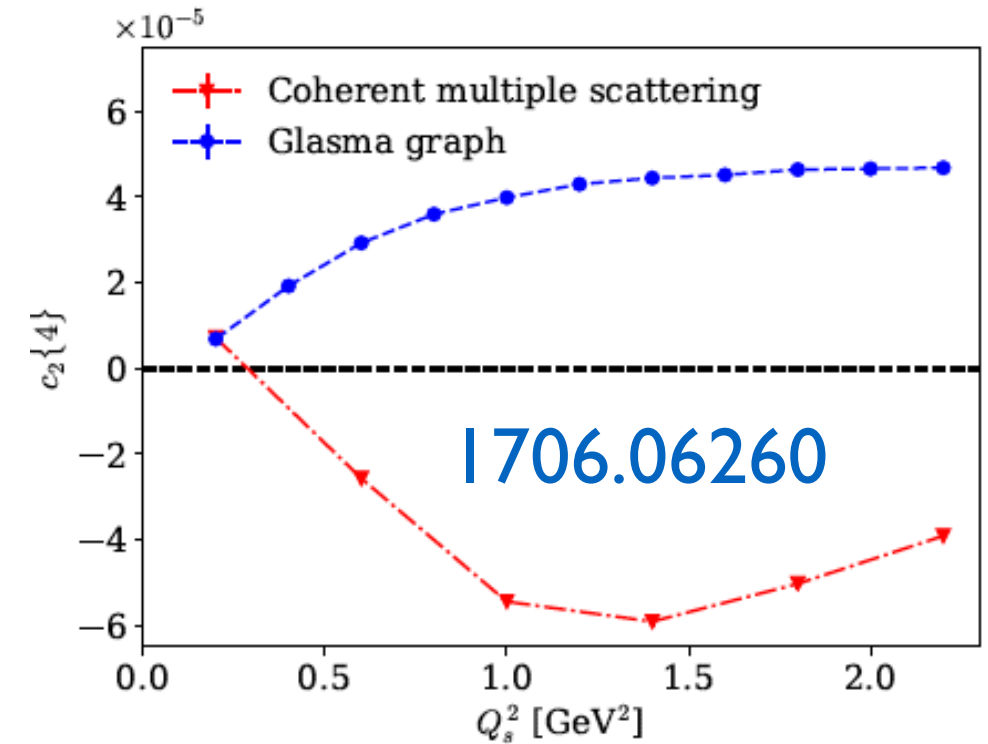
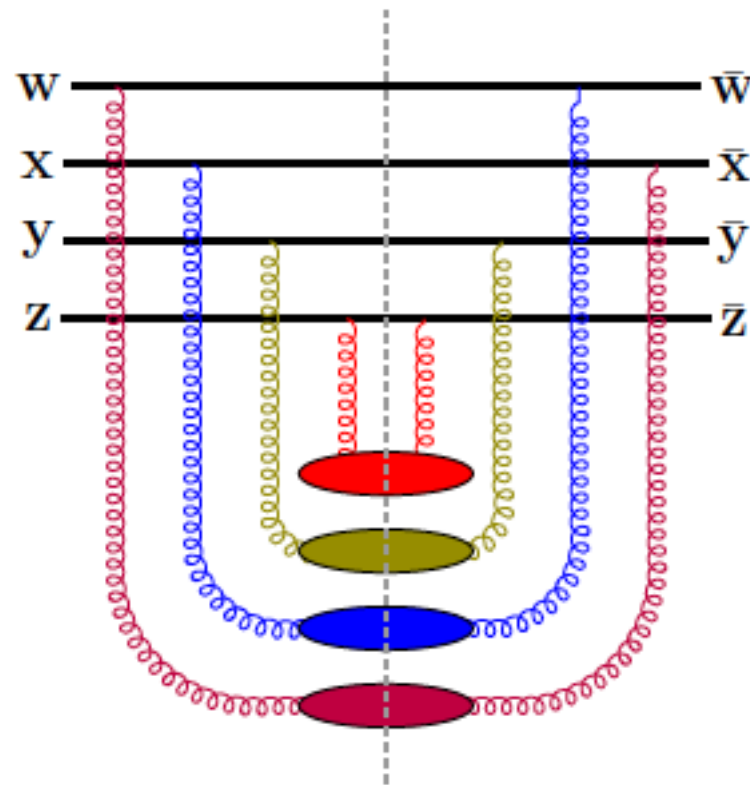
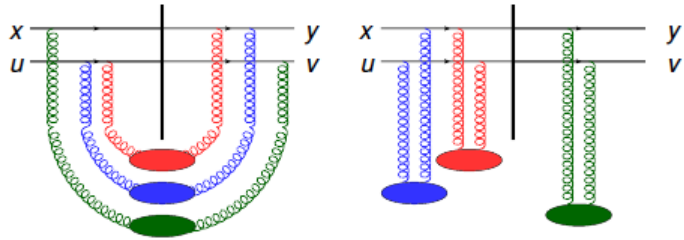
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- Anisotropic domains (1503.03897):

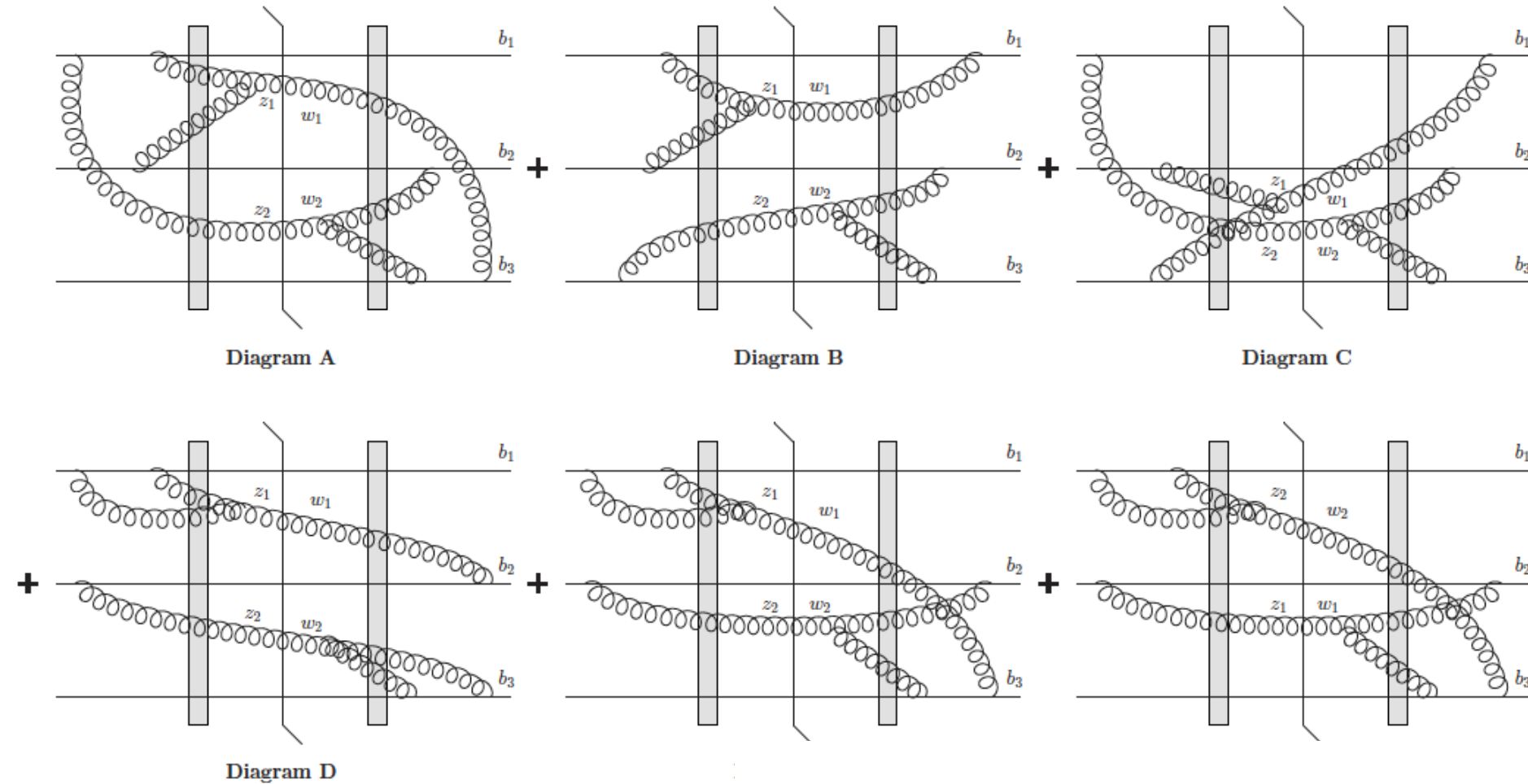
$$\frac{g^2}{N_c} \langle E_i^a(\mathbf{b}_1) E_j^b(\mathbf{b}_2) \rangle = \frac{1}{N_c^2 - 1} \delta^{ab} \delta_{ij} Q_s^2 \Delta(\mathbf{b}_1 - \mathbf{b}_2)$$

number of domains

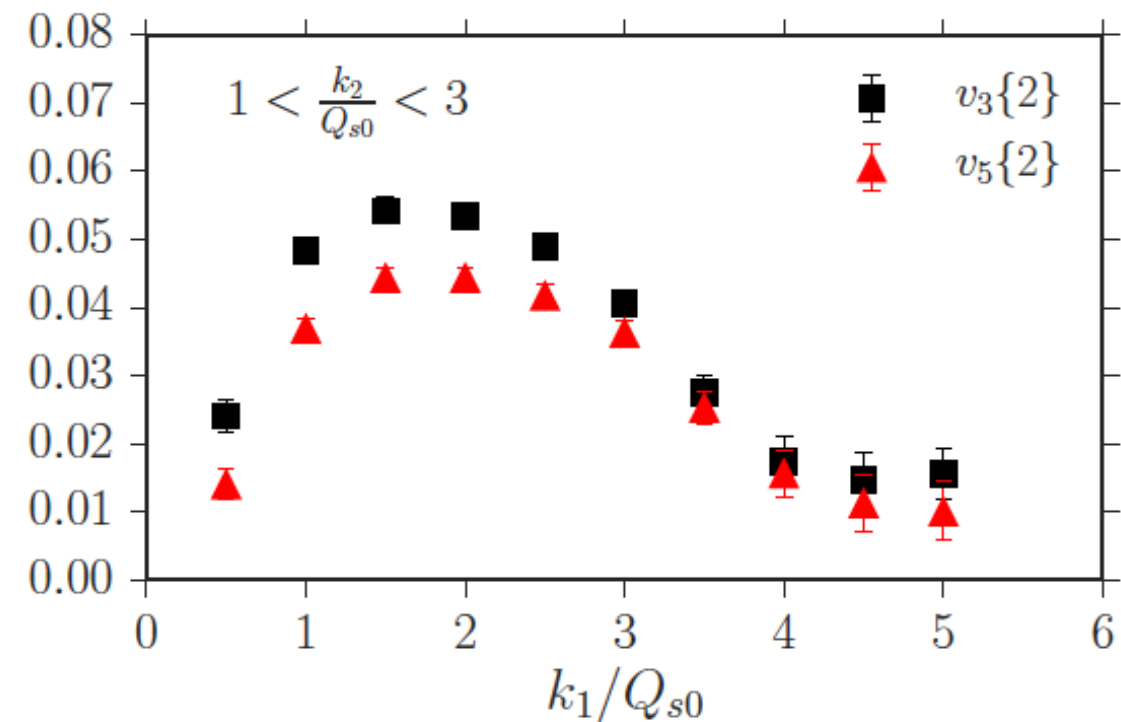
$$\frac{g^2}{N_c} \langle E_i^a(\mathbf{b}_1) E_j^b(\mathbf{b}_2) \rangle_{\hat{a}} = \frac{1}{N_c^2 - 1} \delta^{ab} Q_s^2 \Delta(\mathbf{b}_1 - \mathbf{b}_2) \left( \delta_{ij} + 2\mathcal{A} \left[ \hat{a}_i \hat{a}_j - \frac{1}{2} \delta_{ij} \right] \right)$$

$$-c_2\{4\} = -\frac{1}{4} \left[ \frac{1}{N_D(N_c^2 - 1)} \right]^3 < 0 \quad \longrightarrow \quad c_2\{4\} \equiv -(v_2\{4\})^4 = -\frac{1}{N_D^3} \left( \mathcal{A}^4 - \frac{1}{4(N_c^2 - 1)^3} \right)$$

# Beyond glasma graphs (II):



- Three scatterings for odd harmonics: higher orders in the projectile wave function  
(1612.07790; 1802.08166).





# Beyond glasma graphs (III):

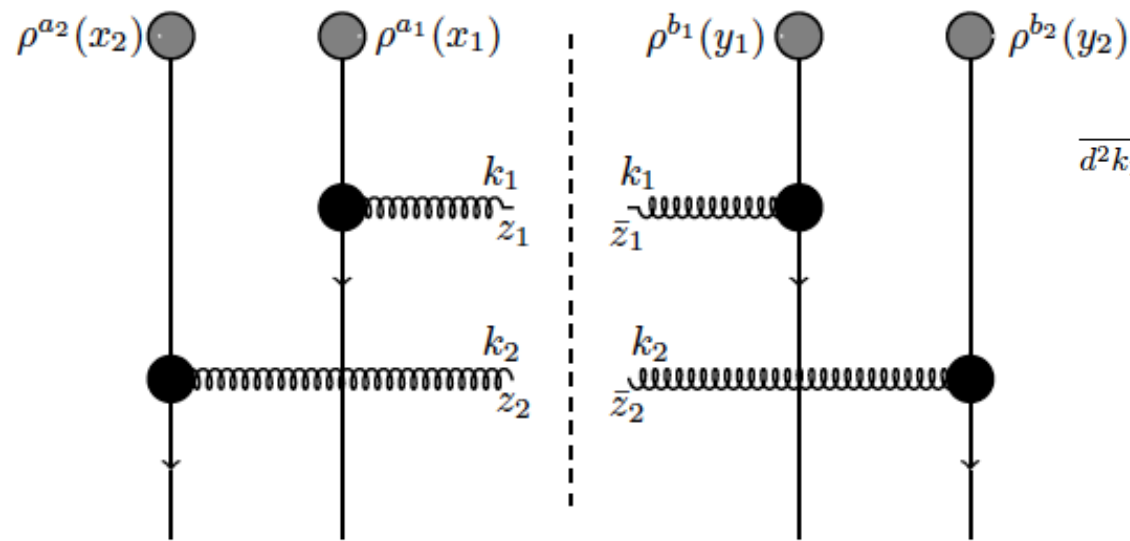
- Density corrections in the target calculated (1804.02910; 1805.07739):

→ Full two-gluon correlation, large  $N_c$  part of the three-gluon inclusive and of the 4-gluon cumulant computed.

→ Factorisation of the target averages assumed: colour neutralisation at scale  $1/Q_s$  imply pair configurations.

→ Only the highest order target correlated provides the fully correlated piece: quadrupole for two, sextuple for three, octupole for four.

→ All BE/HBT contributions, even BE from the target  $1/N_c$  suppressed.



$$\frac{d\sigma}{d^2k_1 d\eta_1 d^2k_2 d\eta_2} = \alpha_s^2 (4\pi)^2 \int_{z_1 \bar{z}_1 z_2 \bar{z}_2} e^{ik_1 \cdot (z_1 - \bar{z}_1) + ik_2 \cdot (z_2 - \bar{z}_2)} \times \int_{x_1 x_2 y_1 y_2} A^i(x_1 - z_1) A^i(\bar{z}_1 - y_1) A^j(x_2 - z_2) A^j(\bar{z}_2 - y_2) \langle \rho^{a_1}(x_1) \rho^{a_2}(x_2) \rho^{b_1}(y_1) \rho^{b_2}(y_2) \rangle_P \times \langle [U(z_1) - U(x_1)]^{a_1 c} [U^\dagger(\bar{z}_1) - U^\dagger(y_1)]^{c b_1} [U(z_2) - U(x_2)]^{a_2 d} [U^\dagger(\bar{z}_2) - U^\dagger(y_2)]^{d b_2} \rangle_T.$$

$$\langle U^{ab}(x) U^{cd}(y) \rangle_T = \delta^{ac} \delta^{bd} \frac{1}{(N_c^2 - 1)^2} \langle \text{tr} [U(x) U^\dagger(y)] \rangle_T = \delta^{ac} \delta^{bd} \frac{1}{N_c^2 - 1} d(x, y),$$

$$\langle Q(x, y, z, v) \rangle_T = d(x, y) d(z, v) + d(x, v) d(z, y) + \frac{1}{N_c^2 - 1} d(x, z) d(y, v),$$

$$\langle D(x, y) D(z, v) \rangle_T = d(x, y) d(z, v) + \frac{1}{(N_c^2 - 1)^2} [d(x, v) d(y, z) + d(x, z) d(y, v)].$$

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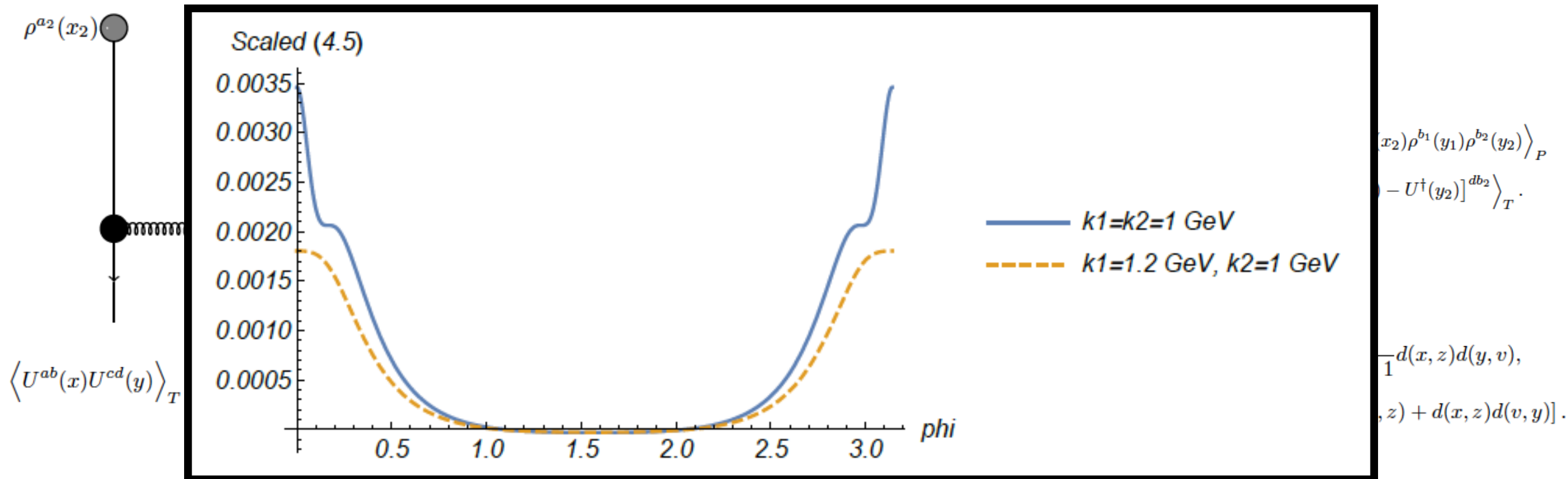
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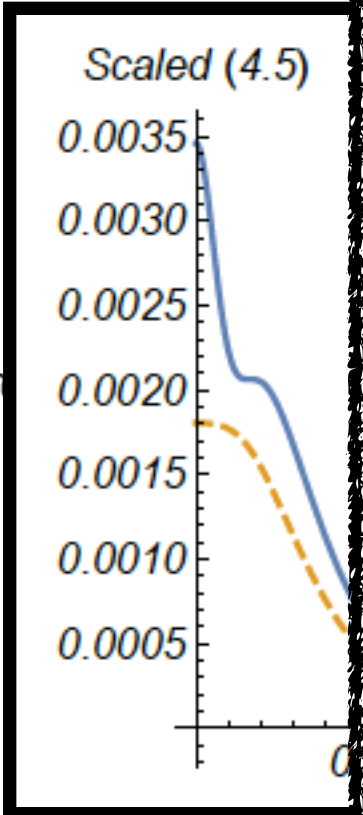
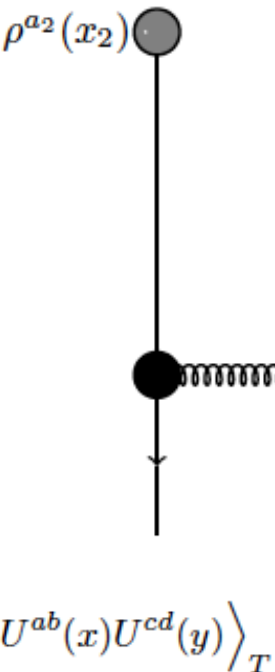
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We can now substitute Eq. (61) into the sextupole contribution to the triple inclusive gluon production cross section given by Eq. (40). The result reads

$$\frac{d\sigma}{d^2k_1 d\eta_1 d^2k_2 d\eta_2 d^2k_3 d\eta_3} \Big|_X = \alpha_s^3 (4\pi)^3 (N_c^2 - 1) \int \frac{d^2q_1}{(2\pi)^2} \frac{d^2q_2}{(2\pi)^2} \frac{d^2q_3}{(2\pi)^2} d(q_1)d(q_2)d(q_3) \times \left\{ [I_{X,1} + I_{X,2} + I_{X,3} + I_{X,4} + I_{X,5}] + \mathcal{O}\left(\frac{1}{(N_c^2 - 1)}\right) + \mathcal{O}\left(\frac{1}{(N_c^2 - 1)^2}\right) \right\}, \quad (62)$$

where

$$I_{X,1} = [\tilde{I}_{X,1} + (k_3 \rightarrow -k_3)] + [\tilde{I}'_{X,1} + (k_1 \rightarrow -k_1)] \quad (63)$$

with  $\tilde{I}_{X,1}$  and  $\tilde{I}'_{X,1}$  defined as

$$\begin{aligned} \tilde{I}_{X,1} &= \mu^2(k_2 - q_2, q_2 - k_1) \mu^2(k_1 - q_1, q_3 - k_3) \mu^2(k_3 - q_3, q_1 - k_2) L^i(k_1, q_1) L^i(k_1, q_2) L^j(k_2, q_2) L^j(k_2, q_1) \\ &\quad \times L^k(k_3, q_3) L^k(k_3, q_3) \\ &\quad + \mu^2(k_2 + q_2, k_1 - q_2) \mu^2(k_3 - q_3, q_1 - k_1) \mu^2(q_3 - k_3, -q_1 - k_2) L^i(k_1, q_1) L^i(k_1, q_2) L^j(k_2, -q_1) L^j(k_2, -q_2) \\ &\quad \times L^k(k_3, q_3) L^k(k_3, q_3), \quad (64) \\ \tilde{I}'_{X,1} &= \mu^2(k_1 - q_2, q_2 - k_2) \mu^2(k_2 - q_1, k_3 - q_3) \mu^2(q_1 - k_1, q_3 - k_3) L^i(k_1, q_1) L^i(k_1, q_2) L^j(k_2, q_1) L^j(k_2, q_2) \\ &\quad \times L^k(k_3, q_3) L^k(k_3, q_3) \\ &\quad + \mu^2(-k_1 - q_2, q_2 - k_2) \mu^2(k_2 + q_1, q_3 - k_3) \mu^2(k_3 - q_3, k_1 - q_1) L^i(k_1, -q_2) L^i(k_1, q_1) L^j(k_2, -q_1) L^j(k_2, q_2) \\ &\quad \times L^k(k_3, q_3) L^k(k_3, q_3). \quad (65) \end{aligned}$$

The terms  $I_{X,2}$  and  $I_{X,3}$  can again be defined by using the symmetry properties as

$$I_{X,2} = [\tilde{I}_{X,1}(1 \rightarrow 2, 2 \rightarrow 3, 3 \rightarrow 1) + (k_3 \rightarrow -k_3)] + [\tilde{I}'_{X,1}(1 \rightarrow 2, 2 \rightarrow 3, 3 \rightarrow 1) + (k_1 \rightarrow -k_1)], \quad (66)$$

$$I_{X,3} = [\tilde{I}_{X,1}(1 \rightarrow 3, 3 \rightarrow 2, 2 \rightarrow 1) + (k_3 \rightarrow -k_3)] + [\tilde{I}'_{X,1}(1 \rightarrow 3, 3 \rightarrow 2, 2 \rightarrow 1) + (k_1 \rightarrow -k_1)]. \quad (67)$$

The explicit expressions for the remaining two terms read

$$\begin{aligned} I_{[X,4]} &= \mu^2(k_2 - q_2, q_1 - k_1) \mu^2(k_1 - q_1, q_3 - k_3) \mu^2(k_3 - q_3, q_2 - k_2) L^i(k_1, q_1) L^i(k_1, q_1) L^j(k_2, q_2) L^j(k_2, q_2) \\ &\quad \times L^k(k_3, q_3) L^k(k_3, q_3) + (k_3 \rightarrow -k_3) \\ &\quad + \mu^2(k_2 - q_2, q_3 - k_3) \mu^2(k_3 - q_3, k_1 - q_1) \mu^2(q_1 - k_1, q_2 - k_2) L^i(k_1, q_1) L^i(k_1, q_1) L^j(k_2, q_2) L^j(k_2, q_2) \\ &\quad \times L^k(k_3, q_3) L^k(k_3, q_3) + (k_1 \rightarrow -k_1) \\ &\quad + \mu^2(k_2 - q_2, k_1 - q_1) \mu^2(k_3 - q_3, q_1 - k_1) \mu^2(q_3 - k_3, q_2 - k_2) L^i(k_1, q_1) L^i(k_1, q_1) L^j(k_2, q_2) L^j(k_2, q_2) \\ &\quad \times L^k(k_3, q_3) L^k(k_3, q_3) + (k_3 \rightarrow -k_3) \\ &\quad + \mu^2(q_1 - k_1, q_3 - k_3) \mu^2(k_1 - q_1, q_2 - k_2) \mu^2(k_2 - q_2, k_3 - q_3) L^i(k_1, q_1) L^i(k_1, q_1) L^j(k_2, q_2) L^j(k_2, q_2) \\ &\quad \times L^k(k_3, q_3) L^k(k_3, q_3) + (k_1 \rightarrow -k_1), \quad (68) \end{aligned}$$

$$\begin{aligned} I_{[X,5]} &= \mu^2(k_2 - q_2, q_2 - k_1) \mu^2(k_1 - q_1, q_1 - k_3) \mu^2(k_3 - q_3, q_3 - k_2) L^i(k_1, q_1) L^i(k_1, q_2) L^j(k_2, q_2) L^j(k_2, q_3) \\ &\quad \times L^k(k_3, q_3) L^k(k_3, q_1) + (k_3 \rightarrow -k_3) \\ &\quad + \mu^2(k_2 - q_2, q_2 - k_3) \mu^2(k_3 - q_3, q_3 + k_1) \mu^2(q_1 - k_2, -k_1 - q_1) L^i(k_1, -q_1) L^i(k_1, -q_3) L^j(k_2, q_2) L^j(k_2, q_1) \\ &\quad \times L^k(k_3, q_3) L^k(k_3, q_2) + (k_1 \rightarrow -k_1) \\ &\quad + \mu^2(k_2 + q_1, k_1 - q_1) \mu^2(k_3 - q_3, q_3 - k_1) \mu^2(q_2 - k_3, -k_2 - q_2) L^i(k_1, q_1) L^i(k_1, q_3) L^j(k_2, -q_2) L^j(k_2, -q_1) \\ &\quad \times L^k(k_3, q_3) L^k(k_3, q_2) + (k_3 \rightarrow -k_3) \\ &\quad + \mu^2(k_2 + q_3, k_3 - q_3) \mu^2(-k_1 - q_1, q_1 - k_3) \mu^2(k_1 - q_2, q_2 - k_2) L^i(k_1, -q_1) L^i(k_1, q_2) L^j(k_2, q_2) L^j(k_2, -q_3) \\ &\quad \times L^k(k_3, q_3) L^k(k_3, q_1) + (k_1 \rightarrow -k_1). \quad (69) \end{aligned}$$

1805.07739;

in inclusive and of

realisation at scale

by correlated piece:

suppressed.

GeV  
GeV,  $k_2=1$  GeV

$$\left. \left. \left. \rho^{a_2}(x_2) \rho^{b_1}(y_1) \rho^{b_2}(y_2) \right) \right)_P \right. - U^\dagger(y_2) \Big]^{db_2} \Big) \Big)_T.$$

$$\frac{1}{1} d(x, z) d(y, v),$$

$$, z) + d(x, z) d(v, y)].$$

# Other approaches: MPIs

- Multiple (partonic) interactions were known to create rapidity correlations since the 70's (Capella et al., Levin et al.).
- They are present in most, if not all, AA MC models: DPMJET, EPOS, HIJING,...

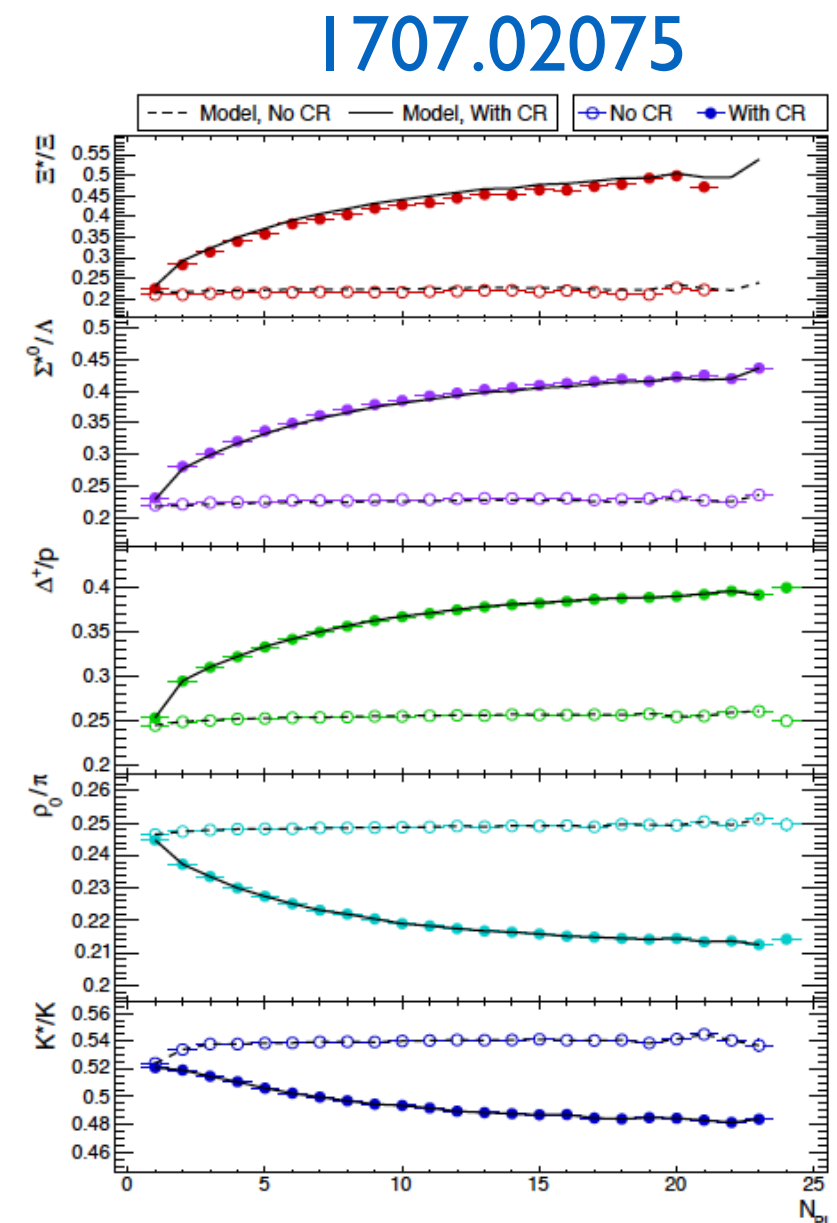
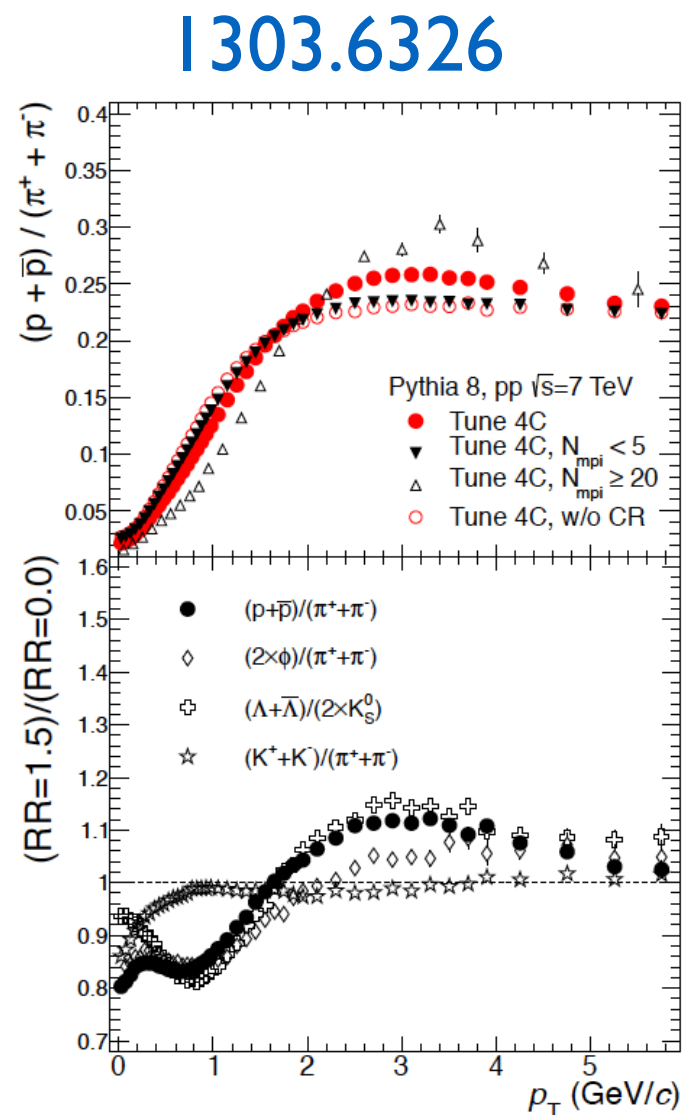
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- Other formulations: string percolation (Pajares et al.), colour ropes (RQMD, AMPT), dipole swing (in DIPSY), string effect (Brodsky et al.),...



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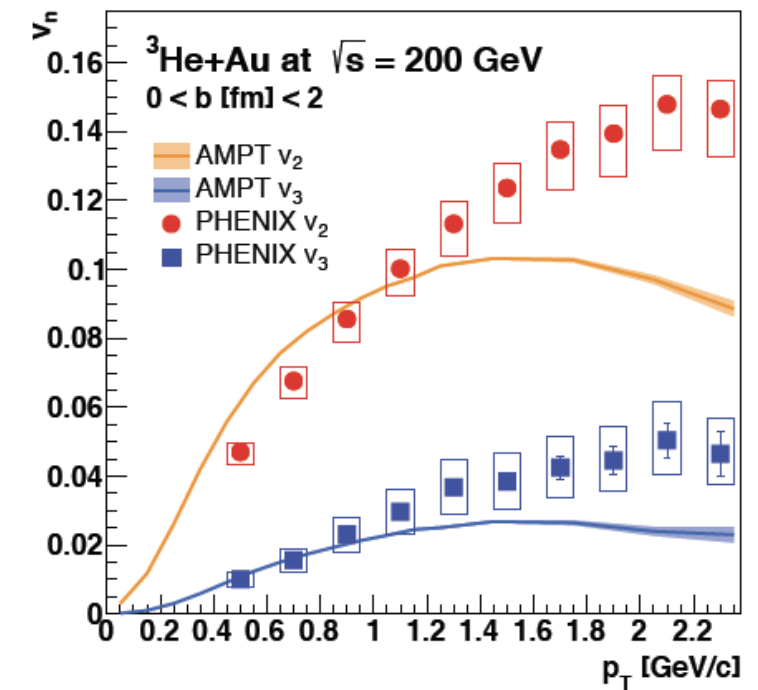
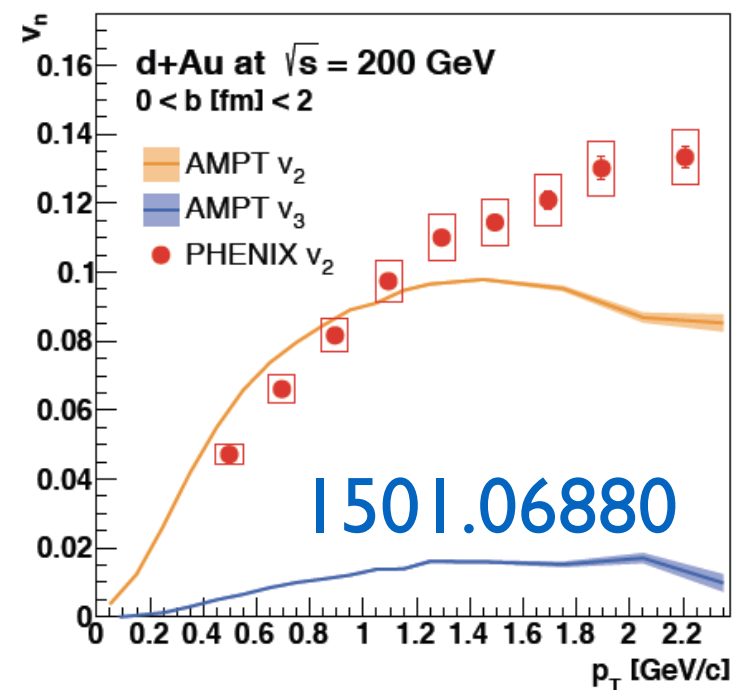
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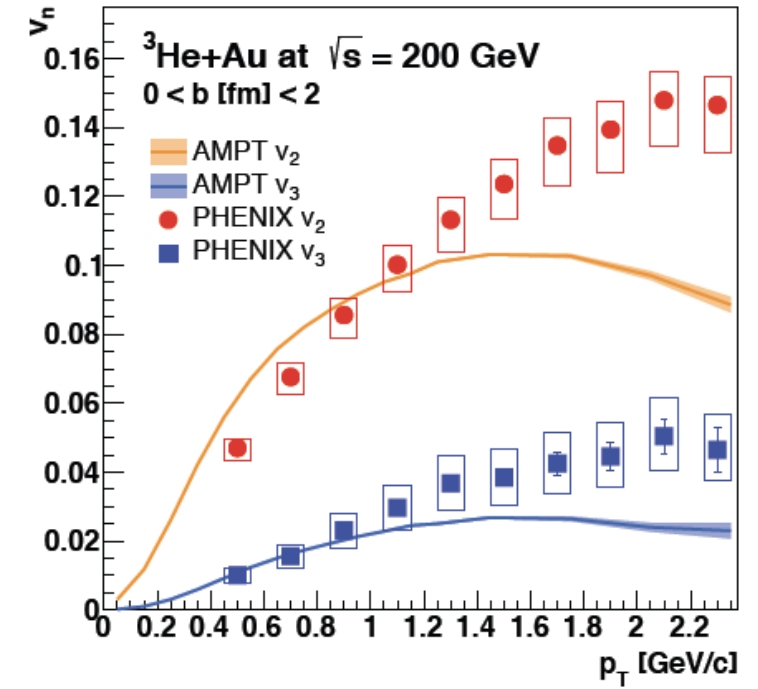
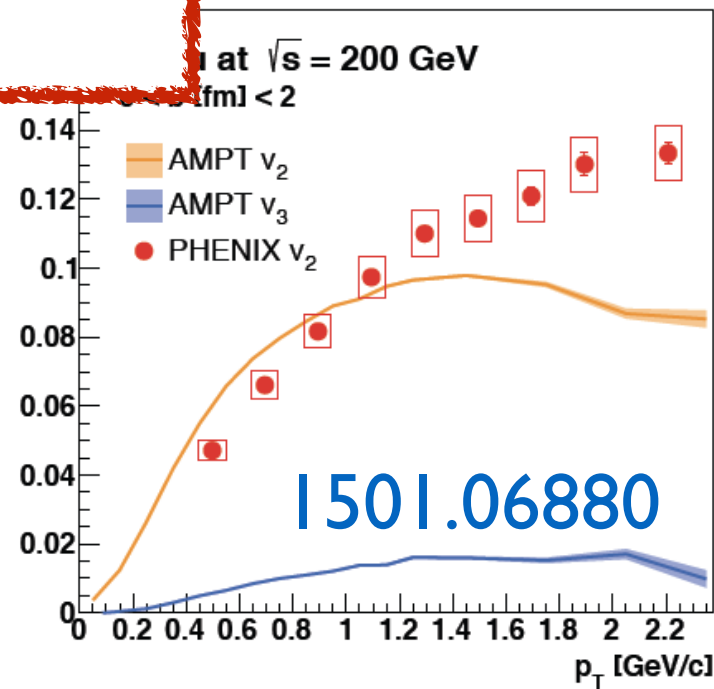
# Other approaches: MPIs

**Note:** multiple scattering is contained in the CGC but, usually, when we talk about MPIs we refer to a collinear framework where a knowledge of multiple parton densities is required: hybrid model (1701.00494).

... were known to create rapidity gaps (see, e.g., [Kharzeev et al., Levin et al.](#)).  
... all, AA MC models: DPMJET,

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- Other formulations: string percolation (Pajares et al.), colour ropes (RQMD, AMPT), dipole swing (in DIPSY), string effect (Brodsky et al.),...



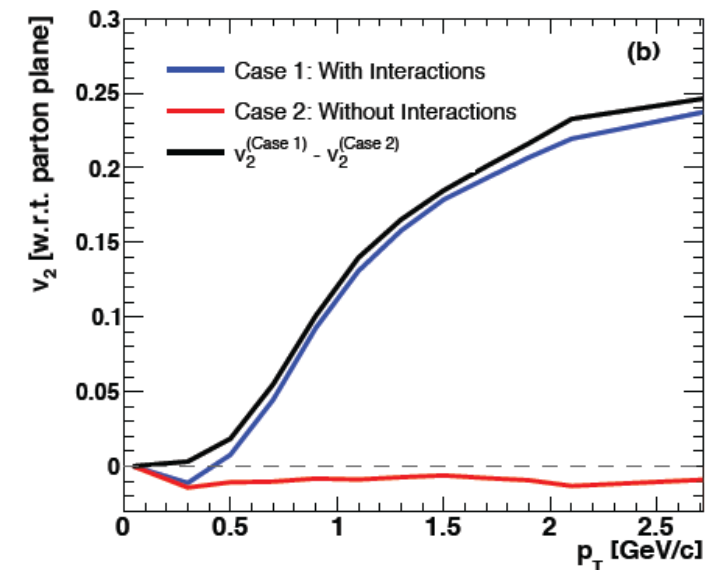
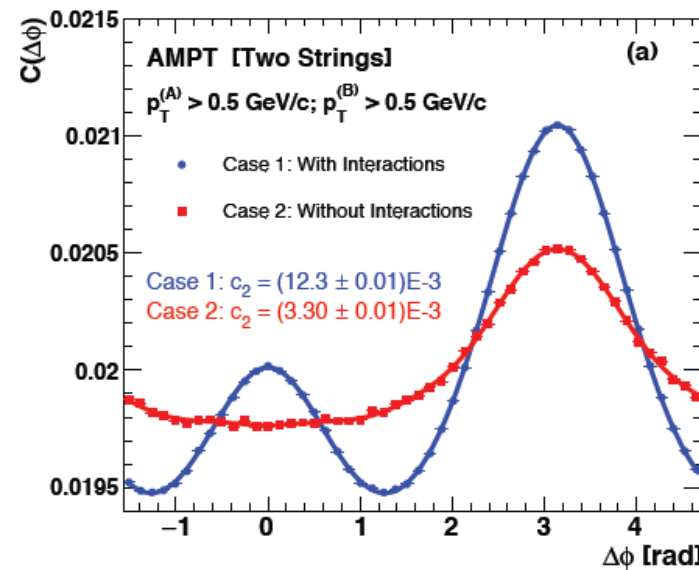
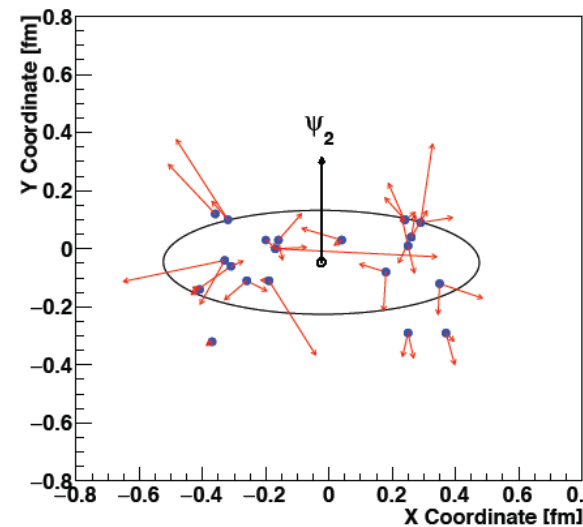
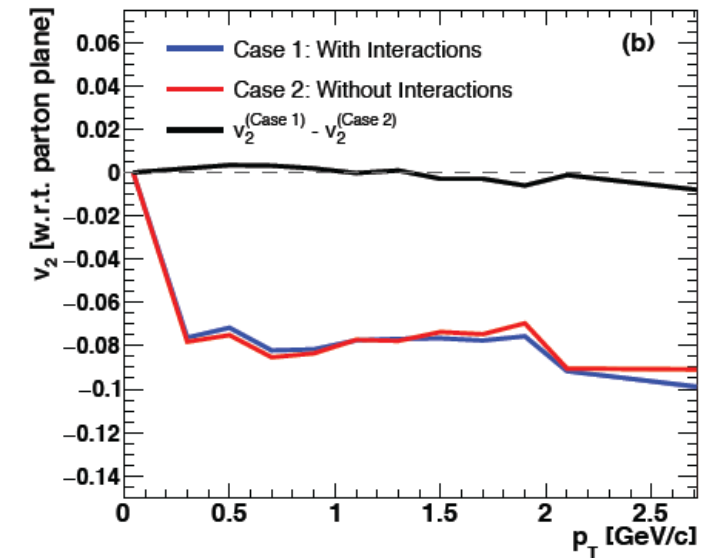
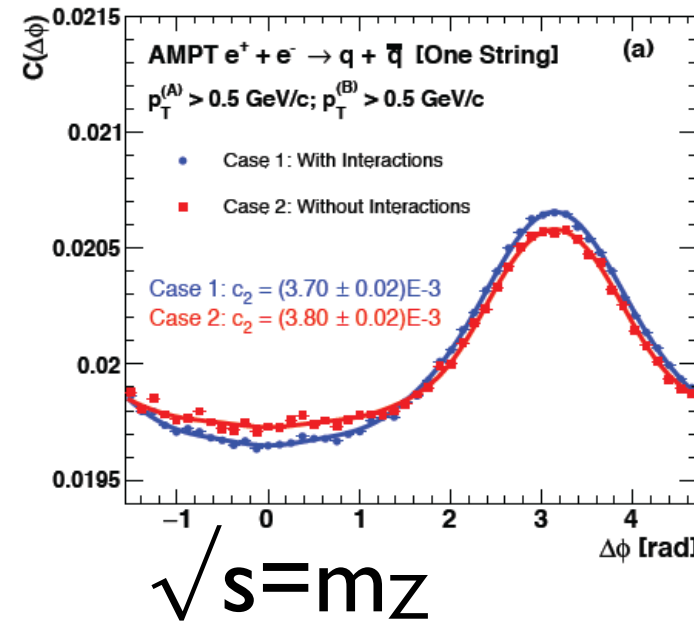
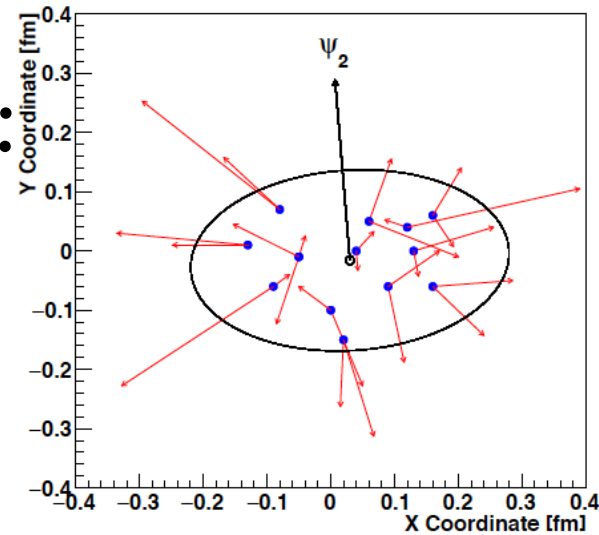
# The onset of collectivity:

- A most crucial question is when a collective behaviour appears i.e. how small a system may be while still showing collective behaviour.
- Smaller than pp: eA/ep and  $e^+e^-$  (remember CR in WW events).
- **1707.02307:**  
one string /  
two (0.5 fm  
apart) in  
AMPT,  
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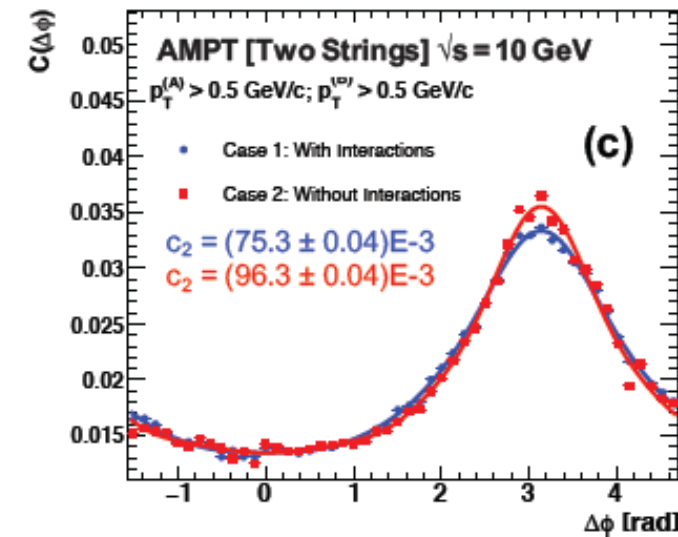
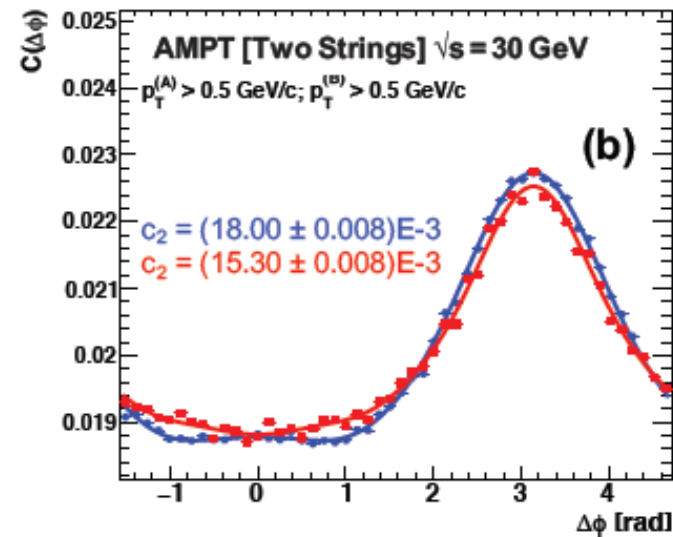
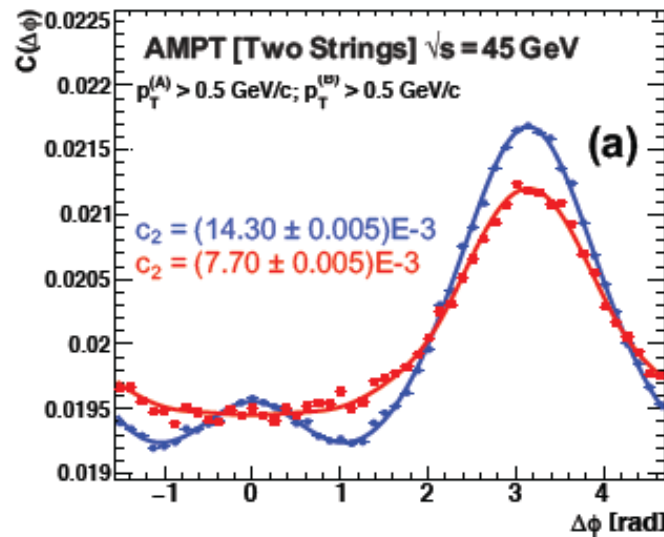
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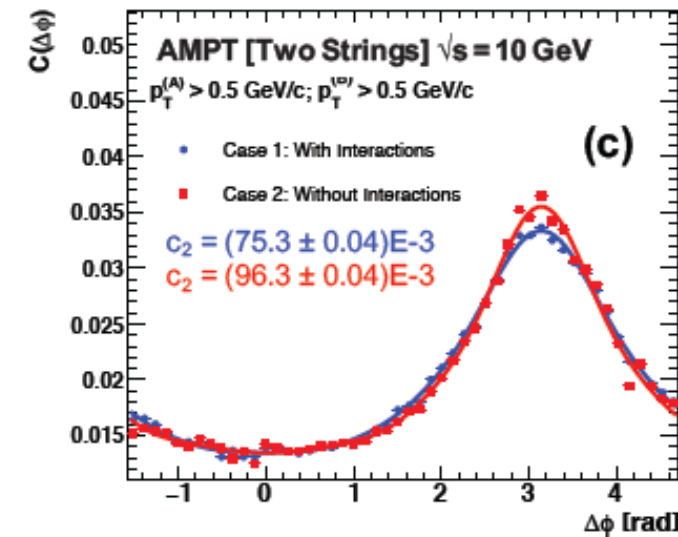
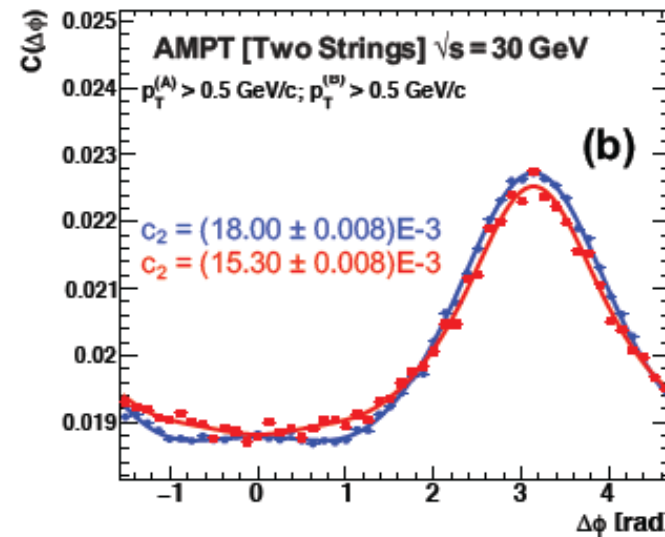
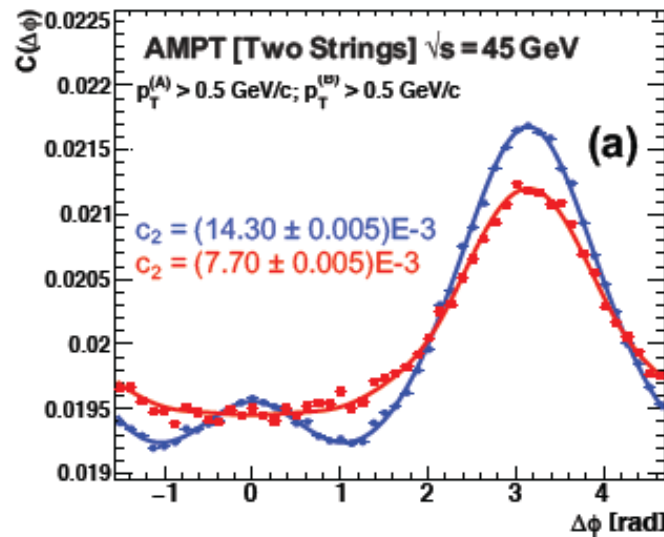
Energy (GeV)	$N_{partons}$	$dN_{ch}/d\eta$ ( $ \eta  < 2$ )	% of Partons w/ $N_{scatter} > 0$
184	95	11.6	40.4%
91	75	11.2	40.3%
60	63	10.5	39.2%
45	55	9.7	38.7%
30	44	8.3	37.6%
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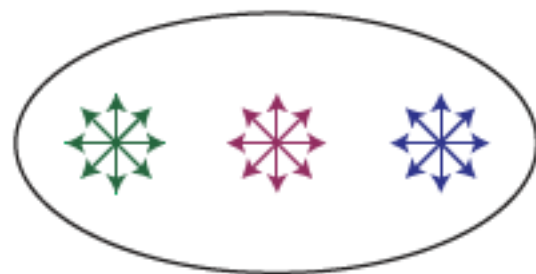
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- It seems to be the combination of large enough # of partons/ particles + more than one source that works.

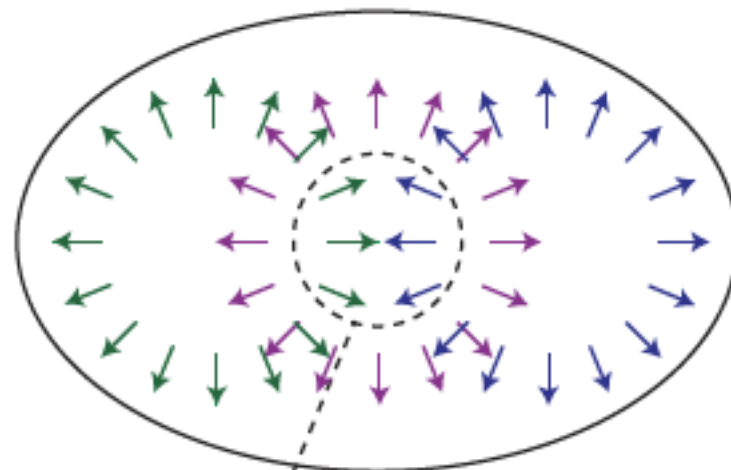
# Transport theory versus hydro:

- Recently proposed that in small systems, kinetic theory looks more sensible than hydro: one-hit dynamics to produce anisotropies (linear and non linear response), milder dependence on initial conditions, ... relevant to determine  $\eta/s$ . [[1803.02072](#), [1805.04081](#)]

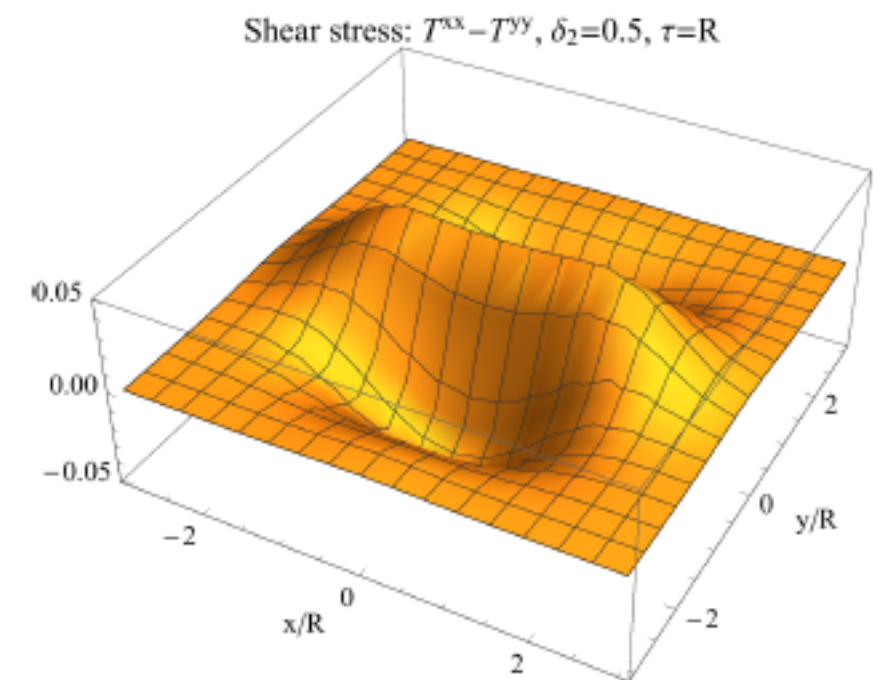
$$\hat{\gamma} = R/l_{mfp}, \quad l_{mfp} = (\gamma\epsilon^{1/4})^{-1} = \tau_\pi \quad F(\vec{x}_\perp, \phi, \tau_0) = 2\epsilon_0 \delta(v_z) \exp\left[-\frac{r^2}{R^2}\right] \left(1 + \delta_2 \frac{r^2}{R^2} \cos 2\theta\right)$$



Initially isotropic momentum distribution



More particles moving in  $\pm x$ -direction

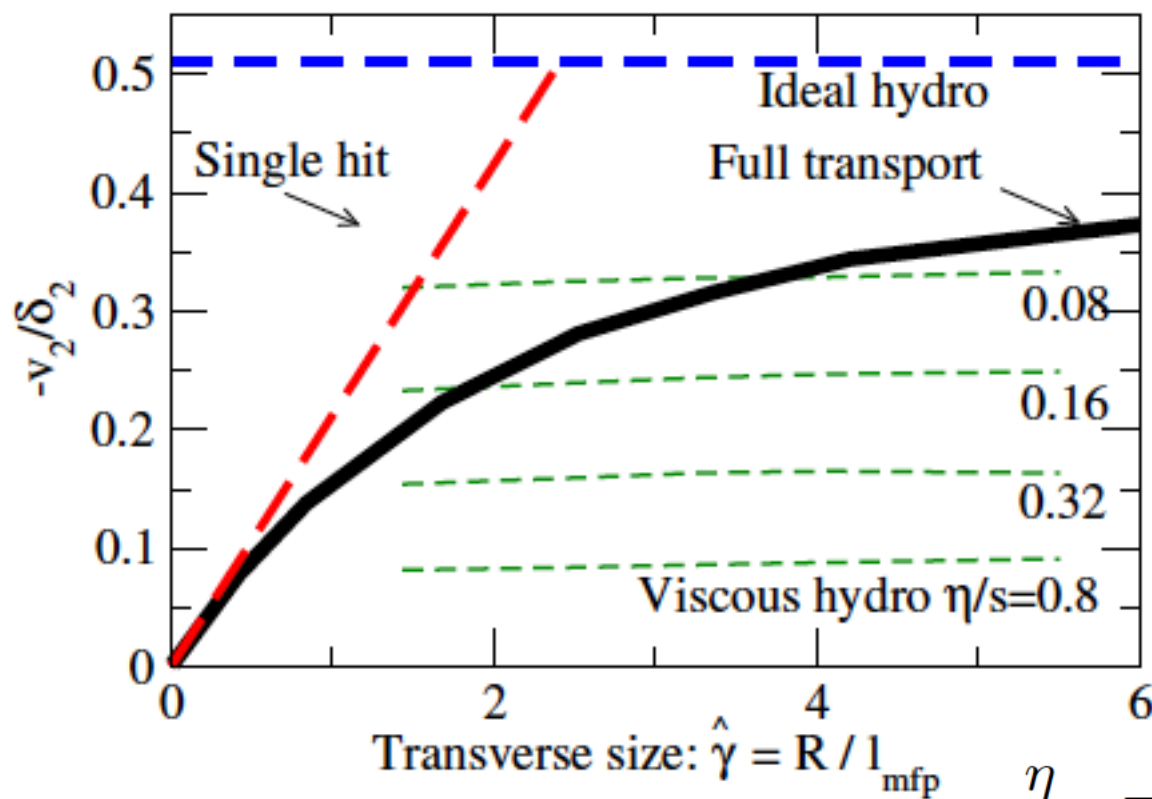


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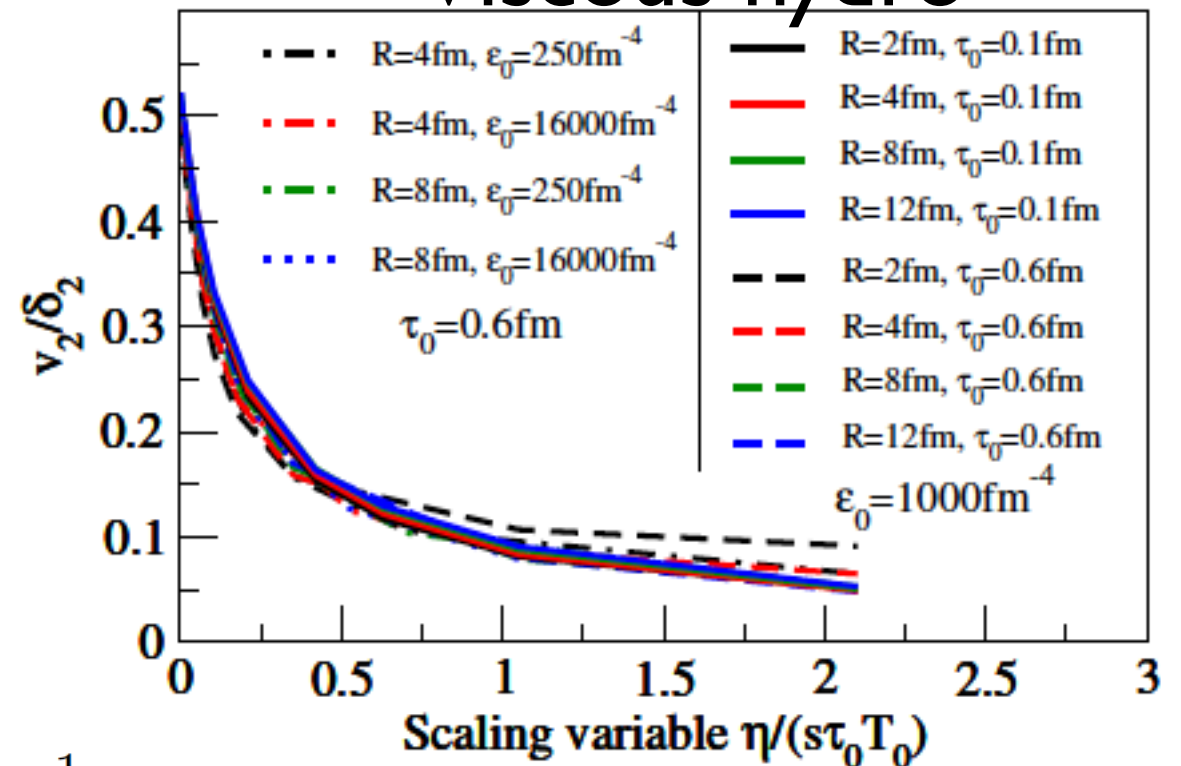
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$$\frac{\eta}{sT} = \frac{1}{\gamma\epsilon^{1/4}} \frac{1}{5}$$

## Viscous hydro



- Kinetic theory, free for these ambiguities  $\Rightarrow$  larger values of  $\eta/s$ .

# Summary:

- Initial stages contain nowadays several of the most striking uncertainties in the field: onset of collectivity? → macroscopic description versus microscopic dynamics.
- The continuity of the physics between small and large systems is motivating a change of paradigm in heavy-ion physics.
- Hydro provides a good description but fine tuning is required (dependence on initial conditions, subnucleon structure).
- Alternatives exist: microscopic calculations in CGC, kinetic theory, in the weak coupling domain.

**Is there a relation between both? How emergence works in QCD?**

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