# DIFFERENTIAL DISTRIBUTIONS FOR SINGLE TOP QUARK PRODUC-TION AT THE LHEC

Meisen Gao, Jun Gao

INPAC, School of Physics and Astronomy, Shanghai Jiao-Tong University, Shanghai 200240, China



#### INTRODUCTION

The Large Hadron Electron Collider (LHeC) is a proposed facility of using a newly built electron beam to collide with the intense hadron beams of the LHC. The LHeC will provide a cleaner environment for the study of single top quark production. The single top quark production have been used to measure the CKM matrix element Vtb and to extract the top-quark mass. Besides, various new physics have been searched for at the LHC with no discovery yet. For the LHeC, single top quark production via charged-current DIS is dominant in all the top quark production channels. We can utilize this unprecedented facility to measure the precise properties of the top quark and search for new physics. [1]

### **DIFFERENTIAL DISTRIBUTION**

Transverse momentum distributions of the charged lepton( $\ell^-$ ) with fiducial cuts applied at LO and NLO with a nominal scale choice of  $m_t/2$  and alternative scale choices of  $m_t/4$  and  $m_t$ .

 $---- NLO \mu_f = m_t/4$  $---- LO \mu_f = m_t$ ---- LO  $\mu_f = m_t/2$ ---- LO  $\mu_f = m_t/4$ ••••• NLO  $\mu_f = m_t$ eV] ••••• NLO  $\mu_f = m_t/2$ 

## SIGNAL OF NEW PHYSICS

We can write the effective Wtb vertex including SM contributions and those from new physics as [3]

$$\mathcal{L}_{tbW} = -\frac{g}{\sqrt{2}} \bar{b} (\gamma^{\mu} ((V_{tb} + \delta V_L) P_L + V_R P_R) - \frac{i\sigma^{\mu\nu} q_{\nu}}{m_W} (g_L P_L + g_R P_R)) t W_{\mu}^- + h.c.$$
(4)

We consider the asymmetry of various observables including  $\Delta \eta(b, \ell^-)$ ,  $\Delta \varphi(b, \ell^-)$ ,  $\Delta \varphi(b, \not{\!\! E_T})$ ,  $\Delta \varphi(\ell^-, \not{\!\! E_T})$  and  $\cos(b, \ell^-)$ :

# **NLO CALCULATION**

 The generic processes under consideration:

 •  $e^-\bar{b} \rightarrow \nu_e \bar{t} \rightarrow \nu_e \ell^- \bar{\nu}_{\ell^-} \bar{b}$  

 •  $e^-b \rightarrow \nu_e \ell^- \bar{\nu}_{\ell^-} b$ 

Feynman diagrams:

• One-loop



•  $\overline{b}$  initial-state real emission





# **TOP QUARK MASS**

We use a linear model on dependence of the average  $P_{T,\ell^-}$  on the top-quark mass

$$A(X, X_0) = \frac{\sigma(X > X_0) - \sigma(X < X_0)}{\sigma(X > X_0) + \sigma(X < X_0)}$$
(5)

Observable	LO	NLO	stats.error
$\Delta\eta(b,\ell^-)$	$-0.374_{+0}^{-0}$	$-0.411\substack{+0.007\\-0.008}$	0.006
$\Delta \varphi(b,\ell^-)$	$0.420\substack{+0.001\\-0.002}$	$0.388\substack{+0.004\\-0.002}$	0.006
$\Delta \varphi(b, E_T)$	$0.805_{+0}^{-0}$	$0.746\substack{+0.012\\-0.013}$	0.005
$\Delta \varphi(\ell^-, \not\!\!\!E_T)$	$0.346^{+0}_{-0}$	$0.292^{-0.008}_{+0.010}$	0.007
$\cos(b,\ell^-)$	$0.419_{+0.011}^{-0.009}$	$0.548_{+0.018}^{-0.018}$	0.006

We can set constraints on the new physics by comparing the SM predictions with the projected measurements. We show the projected bounds on the effective couplings  $g_R$  and  $\delta V_L$  at the 95% CL.

	NLO	$NLO + \Delta scale$
$g_R(\sigma_{tot})$	[-0.039,0.036]	[-0.057,0.050]
$g_R(\Delta\eta(b,\ell^-))$	[-0.060,0.051]	[-0.071,0.059]
$\delta V_L(\sigma_{tot})$	[-0.0073,0.0071]	[-0.010,0.010]

(3)

• g initial-state real emission



We adopt the dipole subtraction method to calculate the NLO cross section: [2]

$$\sigma^{\mathrm{NLO}\{5\}}(p) + \sigma^{\mathrm{NLO}\{4\}}(p) + \int_{0}^{1} dx \hat{\sigma}^{\mathrm{NLO}\{4\}}(x; xp)$$

$$\equiv \int_{5} \left[ \left( \mathrm{d}\sigma^{\mathrm{R}}(p) \right)_{\epsilon=0} - \left( \sum_{\mathrm{dipoles}} \mathrm{d}\sigma^{\mathrm{B}}(p) \otimes \mathrm{d}V_{\mathrm{dipole}} \right)_{\epsilon=0} \right]$$

$$+ \int_{4} \left[ \mathrm{d}\sigma^{\mathrm{V}}(p) + \mathrm{d}\sigma^{\mathrm{B}}(p) \otimes \boldsymbol{I} \right]_{\epsilon=0}$$

$$+ \int_{0}^{1} dx \int_{4} \left[ \mathrm{d}\sigma^{\mathrm{B}}(xp) \otimes (\boldsymbol{P} + \boldsymbol{K})(x) \right]_{\epsilon=0}$$
(1)

# NUMERICAL RESULT

We use  $m_t = 172.5 \,\text{GeV}$  at the LHeC with an electron beam energy of 70 GeV and a proton beam energy of 7 TeV. The selection cuts are:

$$|\eta_{\ell^-}| < 5, \ p_{T,\ell^-} > 10 \,\text{GeV}$$

$$p_{T,\ell^-}\rangle = p_{T,0} + \lambda \left[\frac{m_\ell}{\text{GeV}} - 172.5\right].$$

This table shows various parametric uncertainties, expected statistical error and dependence on the top-quark mass, of the average  $P_{T,\ell^-}$ .

[GeV]	$\delta \langle p_{T,\ell^-}  angle$
PDFs(68% C.L.)	+0.0126 - 0.0081
$\alpha_S(m_Z)(0.001)$	+0.0034 - 0.0031
$m_b(0.5 GeV)$	$\pm 0.0011$
Statistical error	0.1341
$m_t(1.0 GeV)$	0.1225

We present the projection of the top-quark mass measurement with a hypothetical value of 172.5 GeV. Vertical lines indicate various uncertainties of the extracted top-quark mass.



#### CONCLUSION

We present a detailed phenomenological study of the single top (anti-)quark production with leptonic decays at the LHeC at NLO in QCD. The calculations are based on the dipole subtraction method and the complex-mass scheme. The NLO corrections reduce the inclusive cross section by 8.5%. While in a typical fiducial region, the NLO corrections reduce the cross section by 14%. We also present predictions of various distributions. The NLO predictions exhibits strong stability under scale variations for both the total cross section and the distributions. The PDF uncertainty can be larger than the scale variations at the NLO depending on the kinematic region considered.

We find that the statistical error of the extracted topquark mass amounts to 1.1 GeV. The theoretical uncertainty due to the scale variations at the NLO are +1.3 GeV and -0.9 GeV. Besides, we study the possible improvement on searches of new physics with the NLO predictions of the single top quark production. We obtain better constraints on *Wtb* effective couplings  $g_R$  and  $\delta V_L$  using the NLO predictions comparing with the LO predictions. We anticipate our best bounds on  $g_R$  and  $\delta V_L$  at the 95% CL being [-0.057, 0.050] and [-0.010, 0.010] respectively as derived using the NLO SM predictions with scale variations.

#### $|\eta_j| < 5, \ p_{T,jet} > 30 \,\text{GeV}$

(2)

Fiducial cross sections with scale choice of  $m_t/2$ :

fiducial [pb]	LO	NLO
$\sigma[total]$	$0.242^{+8.1\%}_{-11\%}$	$0.205^{+0.76\%}_{+3.1\%}$
$\sigma[\overline{b}]$	0.242	0.207
$\sigma[b]$	$5.01 \times 10^{-4}$	$4.62 \times 10^{-4}$
$\sigma[g]$		$-2.95 \times 10^{-3}$

#### References

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[3] I. A. Sarmiento-Alvarado et al. "Analysis of top-quark charged-current coupling at the LHeC". In: J. Phys. G 42.8 (2015), p. 085001. DOI: 10.1088/0954-3899/42/8/085001. arXiv: 1412.6679 [hep-ph].

#### Contact: gmason@sjtu.edu.cn