

# Pionium Lifetime Measurement by DIRAC

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PHYSICS

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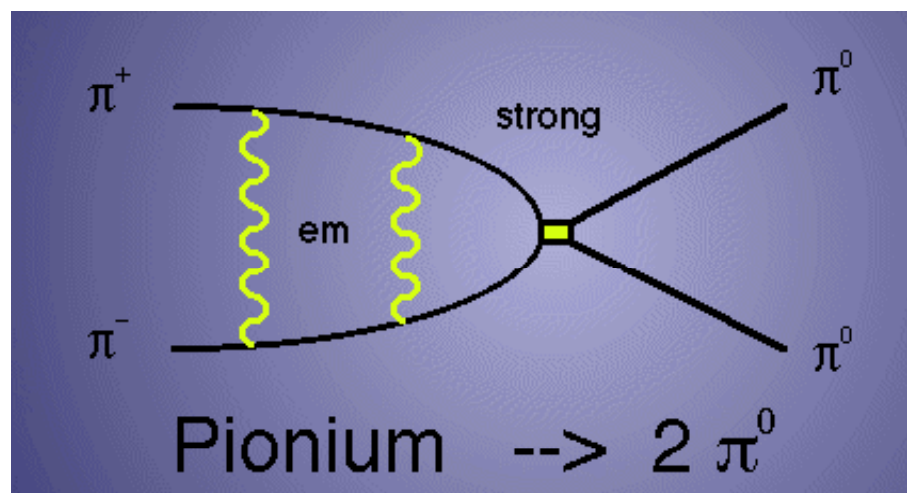
# DIRAC



## DImeson Relativistic Atomic Complexes

Lifetime Measurement of  $\pi^+\pi^-$  atoms to test low energy QCD predictions

[www.cern.ch/DIRAC](http://www.cern.ch/DIRAC)



Basel Univ., Bern Univ., Bucharest IAP, CERN, Dubna JINR, Frascati LNF-INFN, Ioannina Univ., Kyoto-Sangyo Univ., Kyushu Univ. Fukuoka, Moscow NPI, Paris VI Univ., Prague TU, Prague FZU-IP ASCR, Protvino IHEP, Santiago de Compostela Univ., Tokyo Metropolitan Univ., Trieste Univ./INFN, Tsukuba KEK.

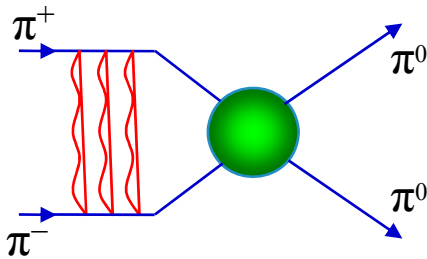
90 Physicists from 18 Institutes

# Pionium lifetime

Pionium is a hydrogen-like atom consisting of  $\pi^+$  and  $\pi^-$  mesons

$$E_B = -1.86 \text{ keV}, \quad r_B = 387 \text{ fm}, \quad p_B \approx 0.5 \text{ MeV}$$

The lifetime of  $\pi^+\pi^-$  atoms is dominated by charge exchange process into  $\pi^0\pi^0$ :



$$\Gamma = \frac{1}{\tau} = \Gamma_{2\pi_0} + \Gamma_{2\gamma} \quad \frac{\Gamma_{2\gamma}}{\Gamma_{2\pi_0}} \approx 4 \times 10^{-3}$$

at lowest order :

$$\Gamma_{2\pi_0} = \frac{2}{9} \alpha^3 p (a_0 - a_2)^2$$

$a_0$  and  $a_2$  are the  $\pi\pi$  S-wave scattering lengths for isospin  $I=0$  and  $I=2$ .

# Pionium lifetime in QCD

At next-to-leading order in  $\alpha$  and  $(m_d - m_u)^2$  :

$$\Gamma_{1s} = \frac{1}{\tau_{1s}} = \frac{2}{9} \alpha^3 p |a_0 - a_2|^2 (1 + \delta) M_{\pi^+}^2 \quad p = \sqrt{M_{\pi^+}^2 - M_{\pi^0}^2 - \frac{1}{4} \alpha^2 M_{\pi^+}^2}$$

J. Gasser et al , Phys. Rev. D62 (2001) 016008

- $\delta = (5.8 \pm 1.2) \times 10^{-2}$  significant correction

**Measurement of  $\tau$  (10%)  $\leftrightarrow$   $|a_0 - a_2|$  (5%)**

# Pionium lifetime in QCD

The  $\pi\pi$  scattering lengths have been calculated in the framework of Chiral Perturbation Theory (ChPT):

G. Colangelo, J. Gasser and H. Leutwyler, Nucl. Phys. B603 (2001) 125.

$$a_0 = 0.220 \pm 0.005 \quad a_2 = -0.0444 \pm 0.0010$$
$$a_0 - a_2 = 0.265 \pm 0.004$$

$$\tau_{1s} = 2.9 \pm 0.1 \text{ fs}$$

# Experimental results

## $K^+ \rightarrow \pi^+ \pi^- e^+ \nu_e$ ( $K_{e4}$ ) decay

$a_0 = 0.26 \pm 0.05$  L. Rosselet et al., Phys. Rev. D 15 (1977) 574

$a_0 = 0.216 \pm 0.013$  New measurement at BNL (E865)

$\pm 0.003$  (syst) S. Pislak et al., Phys. Rev. D 67 (2003) 072004

$a_2 = -0.0454 \pm 0.0031$

$\pm 0.0013$  (syst)

## $\pi N \rightarrow \pi \pi N$ near threshold

$a_0 = 0.26 \pm 0.05$  C.D. Froggatt, J.L. Petersen, Nucl. Phys. B 129 (1977) 89

$a_0 = 0.204 \pm 0.014$  M. Kermani et al., Phys. Rev. C 58 (1998) 3431

$\pm 0.008$  (syst)

## $K^+ \rightarrow \pi^+ \pi^0 \pi^0$ and $K_L \rightarrow 3\pi^0$ NA48/2

$|a_0 - a_2| = 0.261$  N. Cabibbo, Phys. Rev. Lett. 93, 121801 (2004)

N. Cabibbo, G. Isidori, hep-ph/0502130

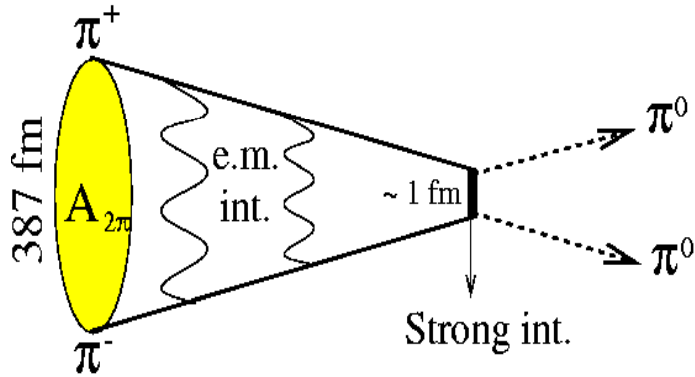
$\pm 0.006$  (*stat.*)

$\pm 0.003$  (*syst.*)

$\pm 0.0013$  (*ext*)

$\pm 0.013$  (*theor*)

# Production of pionium



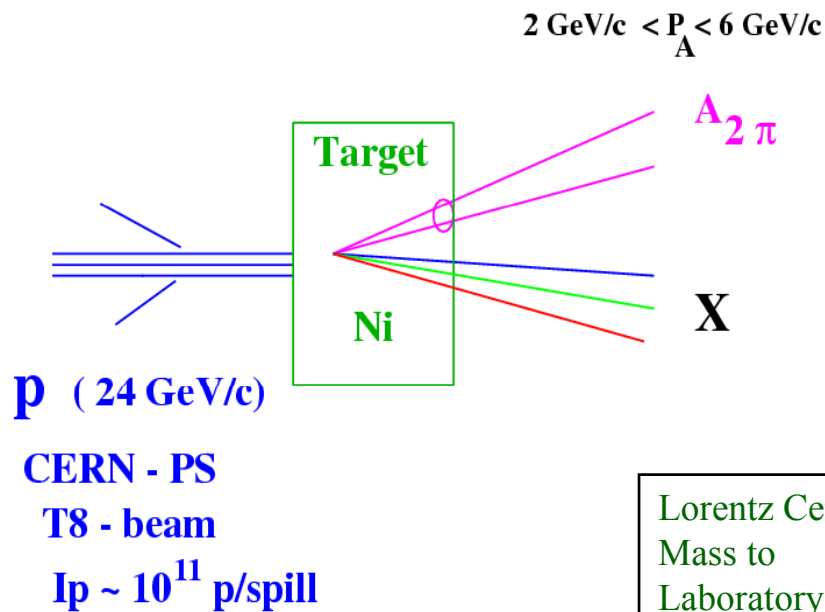
The pionium is a Coulomb bound state:

$$E_B = -1.858 \text{ keV}$$

$$J^{PC} = 0^{++}$$

$$R(A_{2\pi}) = 387 \text{ fm}$$

$$P_B \approx 1 \text{ MeV}$$



$\pi^+$  and  $\pi^-$  originating from short lived sources ( $\rho$ ,  $K^*$ ,  $\omega$ , ...) and resonance decays may form a pionium atom. The differential cross section is:

$$\frac{d\sigma_n^A}{d\vec{p}_A} = (2\pi)^3 \frac{E_A}{M_A} |\Psi_n(0)|^2 \left( \frac{d\sigma_s^0}{d\vec{p}d\vec{q}} \right)_{p=q=P_A/2}$$

Lorentz Center of Mass to Laboratory factor.

Wave function at origin (accounts for Coulomb interaction).

Pion pair production from short lived sources.

# Method of pionium detection

L.Nemenov, Sov.J.Nucl.Phys. 41 (1985) 629

**Pionium is created in nS states then it interacts with target material:**

**Annihilation:**  $A_{2\pi} \rightarrow \pi^0 \pi^0$

$$\lambda_{\text{decay}} = \gamma c \tau \approx 15 \mu\text{m} \text{ for } \gamma \approx 17$$

**Excitation:** transitions between atomic levels

$$\lambda_{\text{int}}^{1S} \approx 20 \mu\text{m} \text{ for Ni}$$

**Break-up(ionisation):** characteristic “atomic” pairs  $n_A$

- $Q_{\text{cms}} < 3 \text{MeV}/c$
- $\rightarrow$  in laboratory system  $E_+ \approx E_-$ , small opening angle  $\theta < 3 \text{mrad}$

**Coulomb and atomic pairs are detected simultaneously:**

$$P_{Br} = \frac{n_A}{N_A} = \frac{1}{K^{th}} \frac{n_A}{N_C}$$



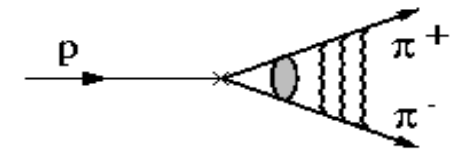
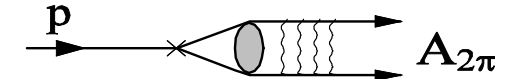
# Production of pionium

**Atoms** are Coulomb bound state of two pions produced in one proton-nucleus collision

$$\frac{d\sigma_n^A}{d\vec{p}_A} = (2\pi)^3 \frac{E_A}{M_A} |\Psi_n(0)|^2 \left( \frac{d\sigma_s^0}{d\vec{p}d\vec{q}} \right)_{p=q=p_A/2}$$

## Background processes:

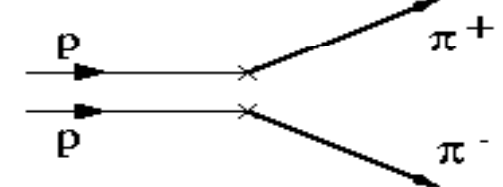
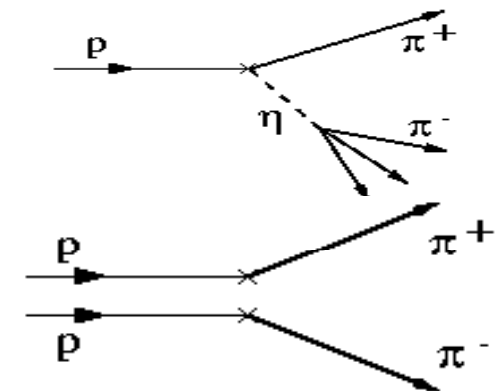
**Coulomb pairs.** They are produced in one proton nucleus collision from fragmentation or short lived resonances ( $\rho$ ,  $K^*$ ,  $\omega$ , ...) and exhibit Coulomb interaction in the final state:



$$\frac{d^2\sigma_c}{dp_+ dp_-} = A_c(q) \frac{d^2\sigma_s^0}{dp_+ dp_-} \quad A_c(q) = \frac{2\pi M_\pi \alpha / q}{1 - \exp(-2\pi M_\pi \alpha / q)}$$

**Non-Coulomb pairs.** They are produced in one proton nucleus collision. At least one pion originates from a long lived resonance. No Coulomb interaction in the final state

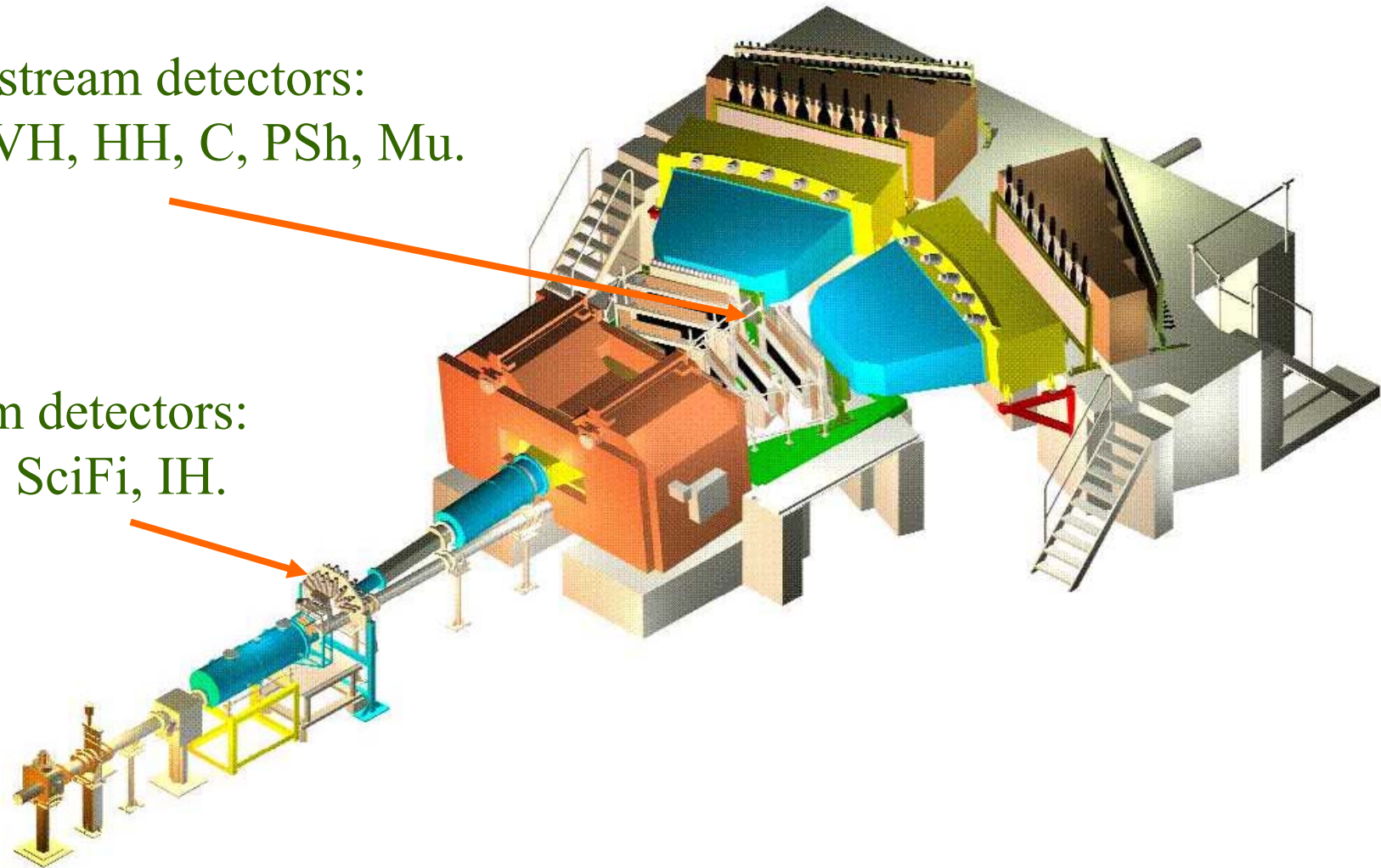
**Accidental pairs.** They are produced in two independent proton nucleus collision. They do not exhibit Coulomb interaction in the final state



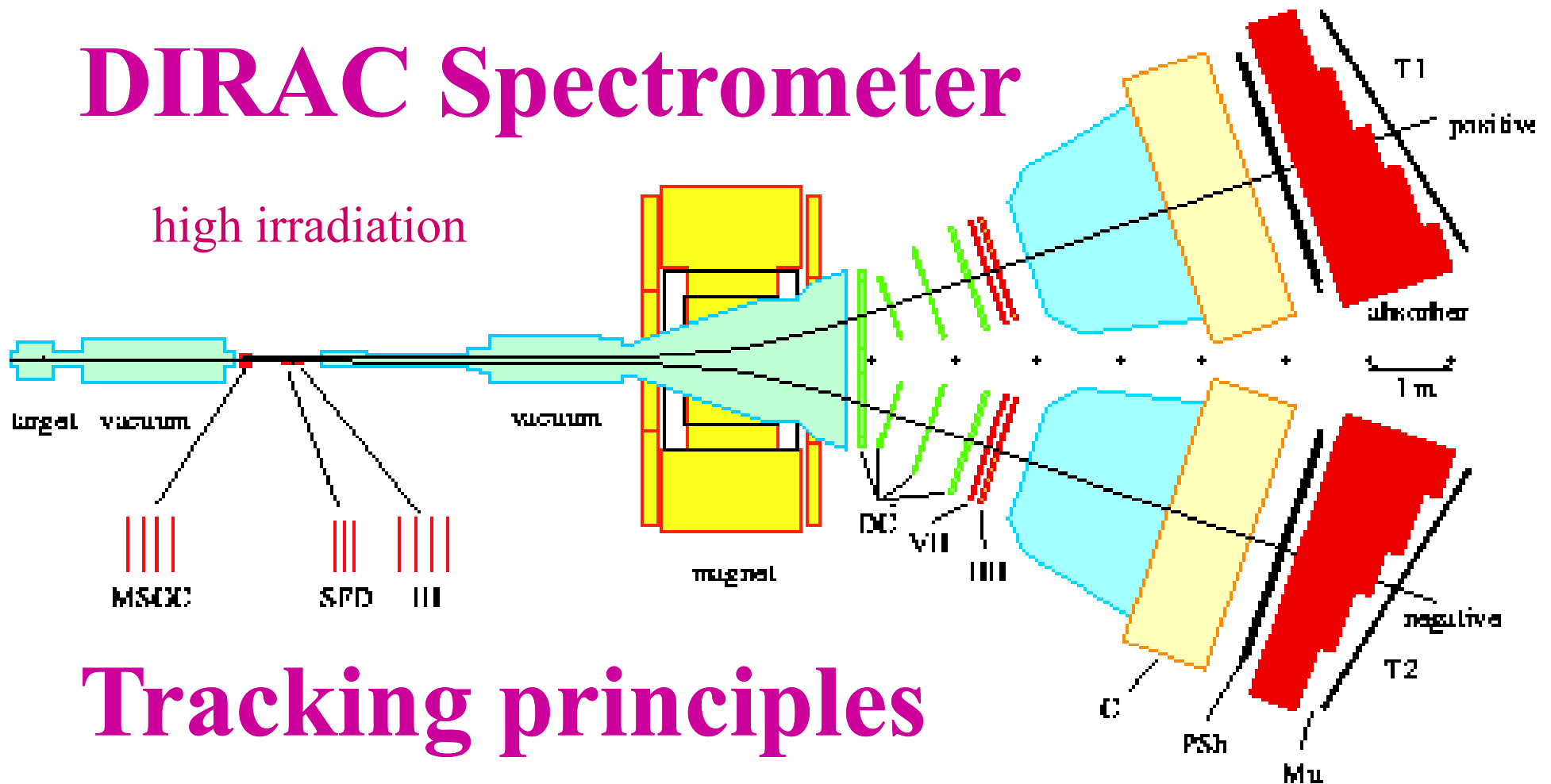
# DIRAC Spectrometer

Downstream detectors:  
DCs, VH, HH, C, PSh, Mu.

Upstream detectors:  
MSGCs, SciFi, IH.



# DIRAC Spectrometer



## Tracking principles

- Precision **time-of-flight** to reduce accidental and proton background
- Strong **e+e- rejection** by Čerenkov counters
- Unambiguous transverse momentum  $Q_T$  by **upstream tracking** (MSGC+SFD)
- Longitudinal momentum  $Q_L$  measured by **fast drift chambers** and upstream tracks

# DIRAC Spectrometer

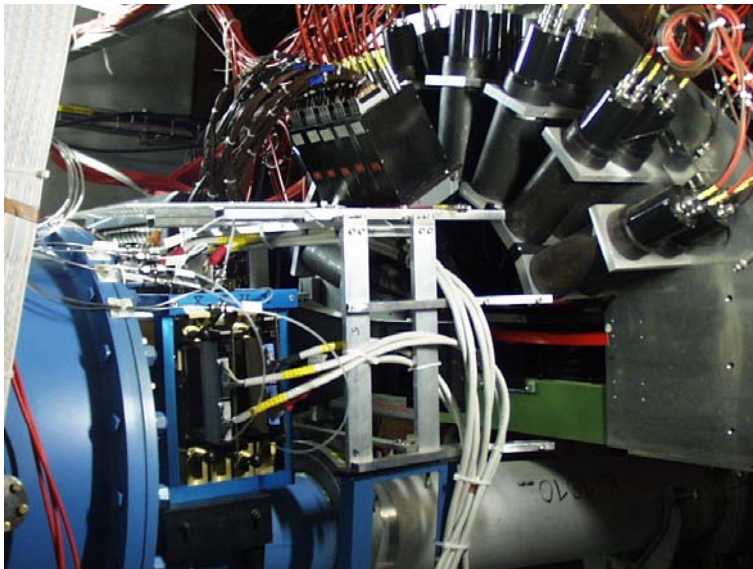


**Nucl. Inst. Meth. A515 (2003) 467.**

## **Downstream detectors:**

Drift chambers  
Cherenkov  
Time-of-Flight

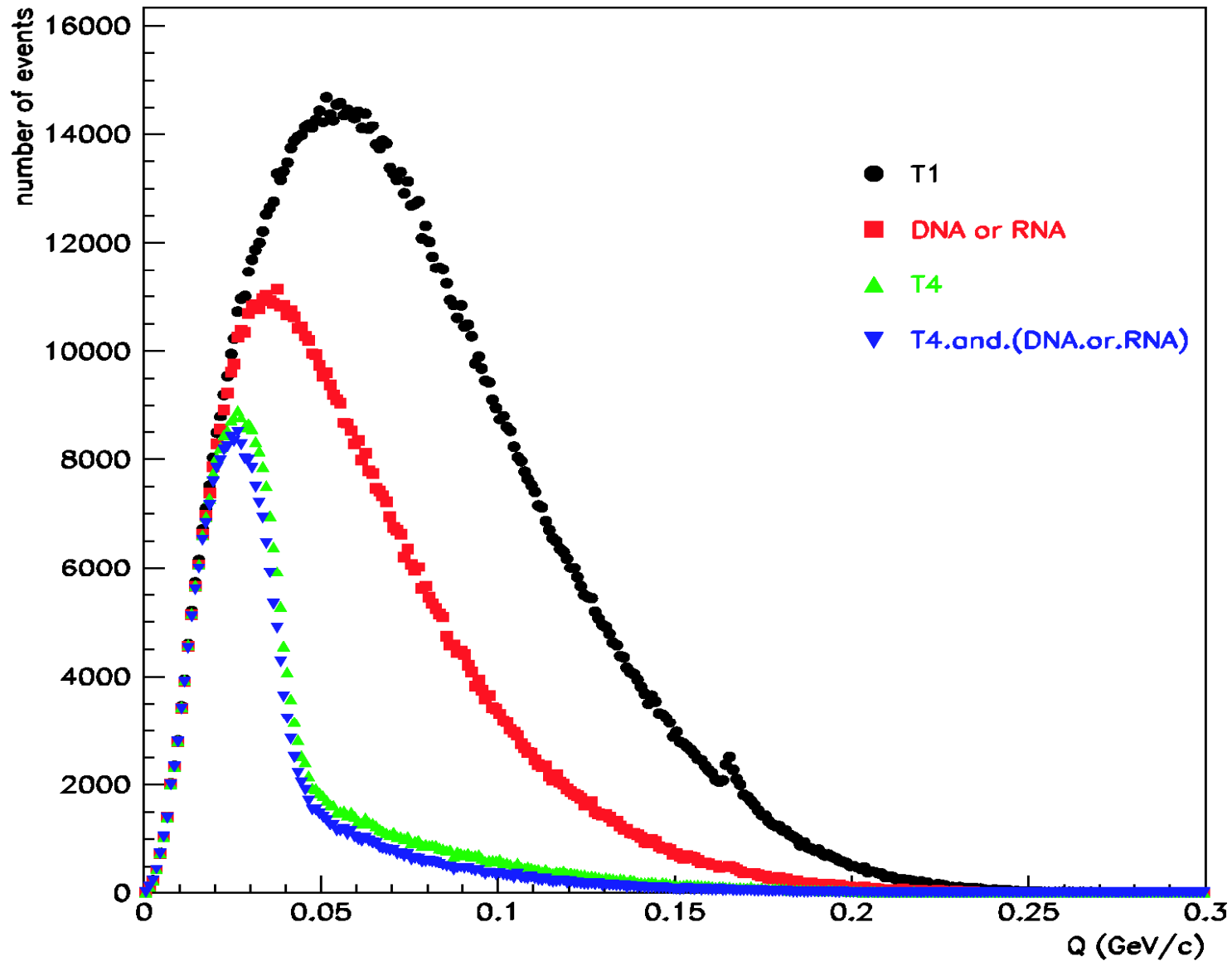
Pre-Shower and  
Muon Counters unseen



## **Upstream detectors:**

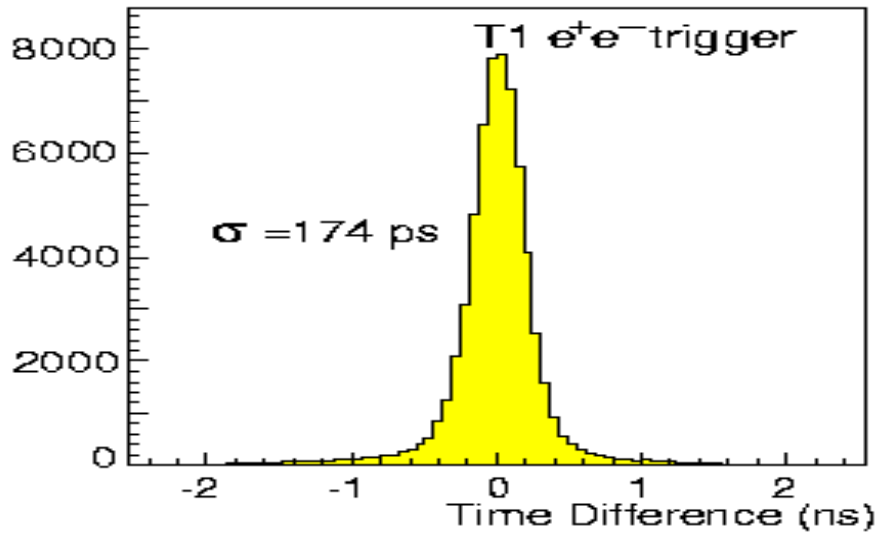
MSGC/GEM  
SFD  
Ionisation Hodoscope

# Trigger performance



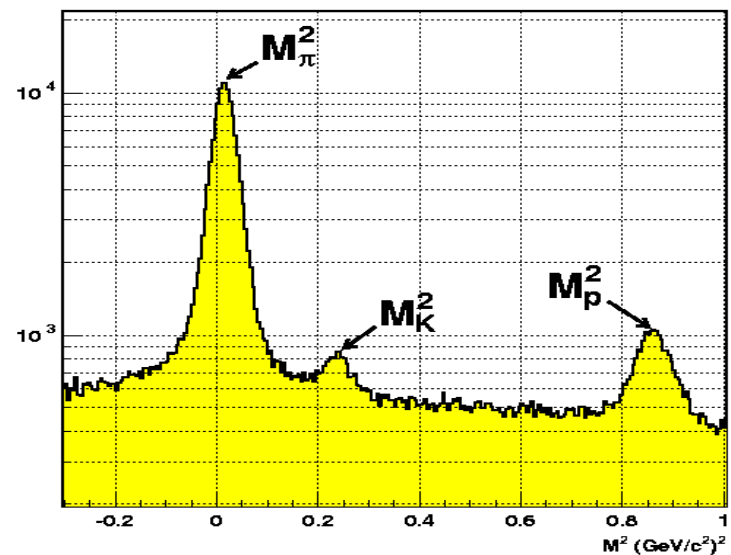
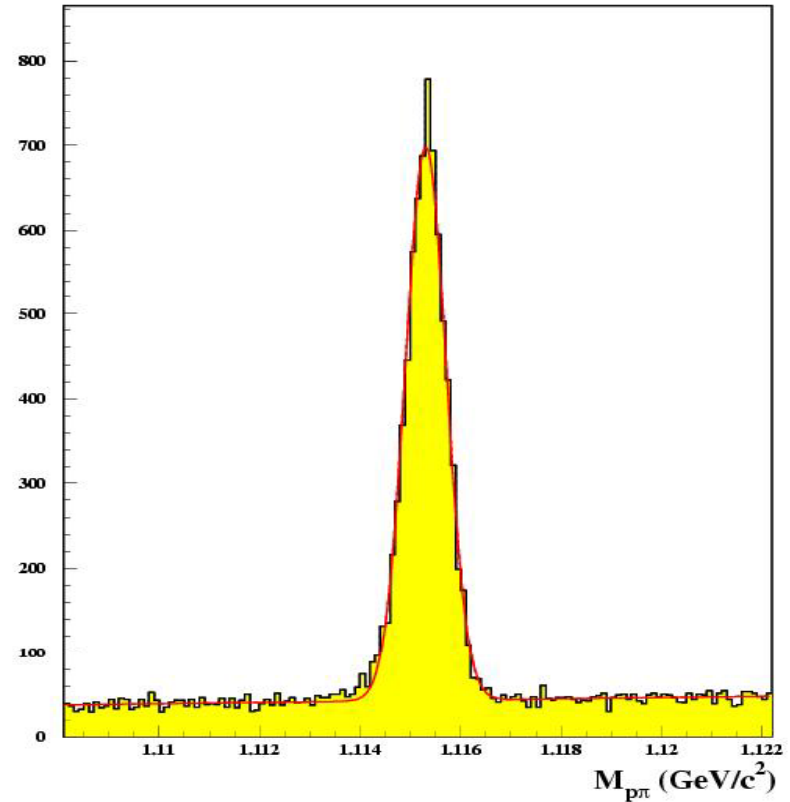
# Calibrations

Mass distribution of  $p\pi^-$  pairs  
from  $\Lambda$  decay.  $\sigma_\Lambda = 0.39 \text{ MeV}/c^2$

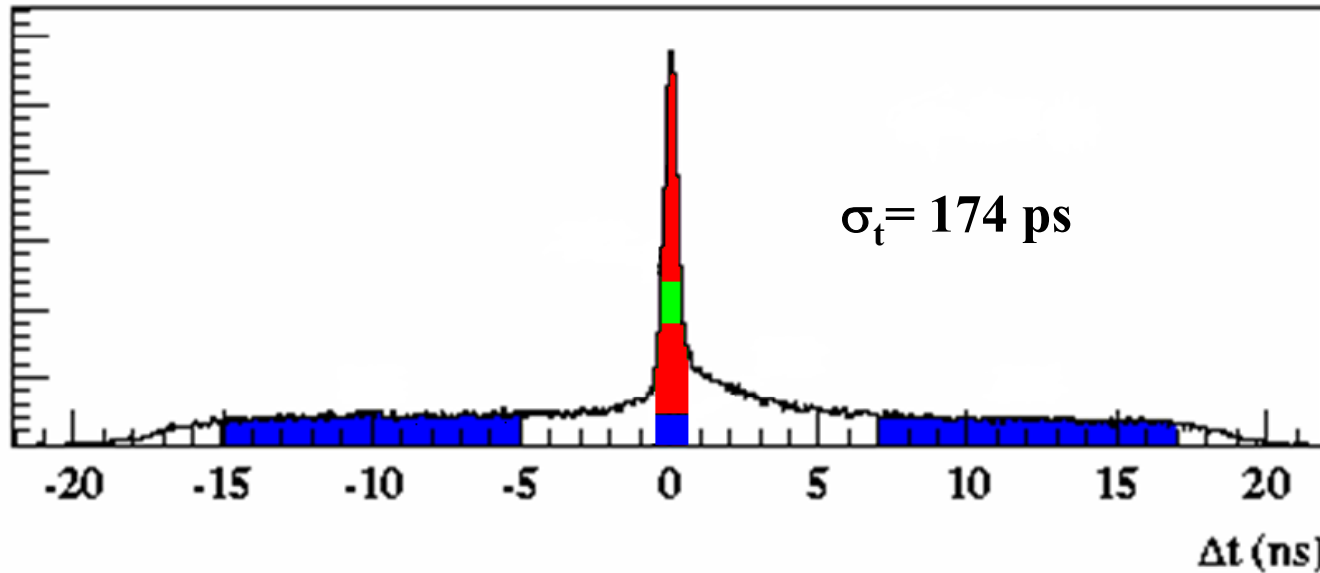


Time difference spectrum  
at VH with  $e^+e^-$  T1 trigger.

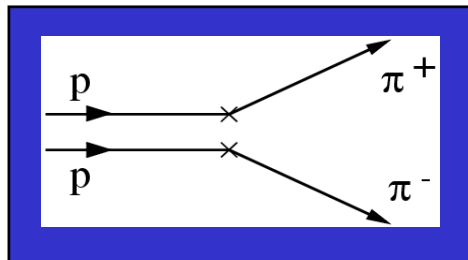
Positive arm mass spectrum,  
obtained by TOF difference, under  
 $\pi^-$  hypothesis in the negative arm.



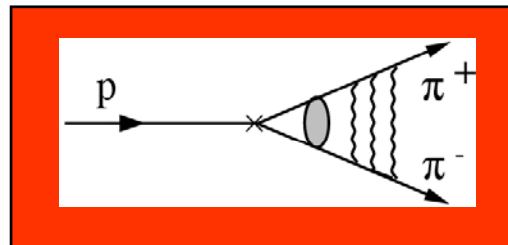
# Time-of-Flight spectrum



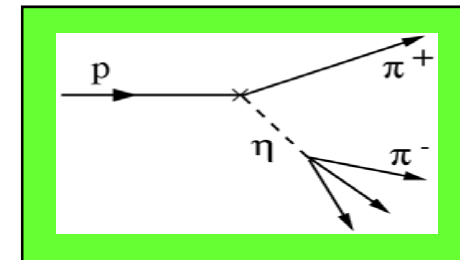
$\pi^+\pi^-$  pairs



Accidental pairs,  
different proton  
interactions in the  
target



Coulomb pairs.  
From short lived  
sources.  
 $r < 3 \text{ fm}, < R(A_{2\pi})$



Non Coulomb  
pairs. From long  
lived sources.  
 $r \sim 1000 \text{ fm}.$

# Analysis based on MC

**Atoms** are generated in **nS states** using measured momentum distribution for **short-lived** sources. The atomic pairs are generated according to the evolution of the atom while propagating through the target

## Background processes:

**Coulomb pairs** are generated according to  $A_c(Q)Q^2$  using measured momentum distribution for **short-lived** sources.

**Non-Coulomb pairs** are generated according to  $Q^2$  using measured momentum distribution for **long-lived** sources.

*Monte Carlo simulation is restricted to detector response only, without relying on specific assumptions from proton-nucleus collision models*



## 2D $\chi^2$ FIT TO ( $Q_T, Q_L$ ) SPECTRUM

$$\frac{dn_p}{d^2Q} = \alpha_1 \frac{dn_{CC}}{d^2Q} + \alpha_2 \frac{dn_{NC}}{d^2Q} + \alpha_3 \frac{dn_{AC}}{d^2Q} + \gamma \frac{dn_{AT}}{d^2Q}$$

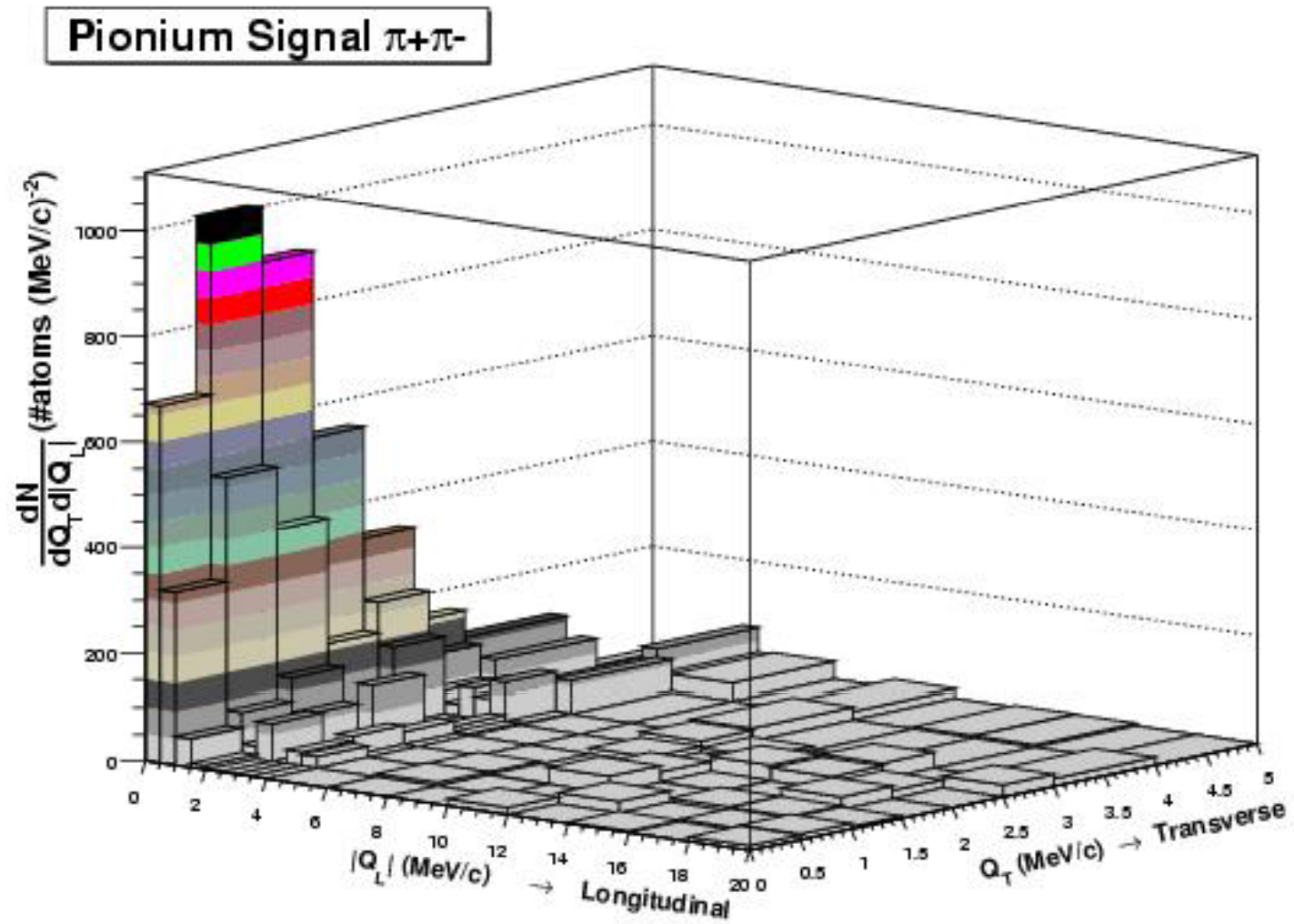
$$\frac{dn_i}{d^2Q} = \frac{1}{N_i} \frac{dn_i}{d^2Q} \quad d^2Q = dQ_T dQ_L \quad \alpha_1 + \alpha_2 + \alpha_3 + \gamma = 1$$

$\alpha_3$  (accidentals fraction) measured from TOF

$\alpha_1$  and  $\gamma$  free parameters in 10 independent  
600 MeV/c  $\pi^+\pi^-$  momentum bins

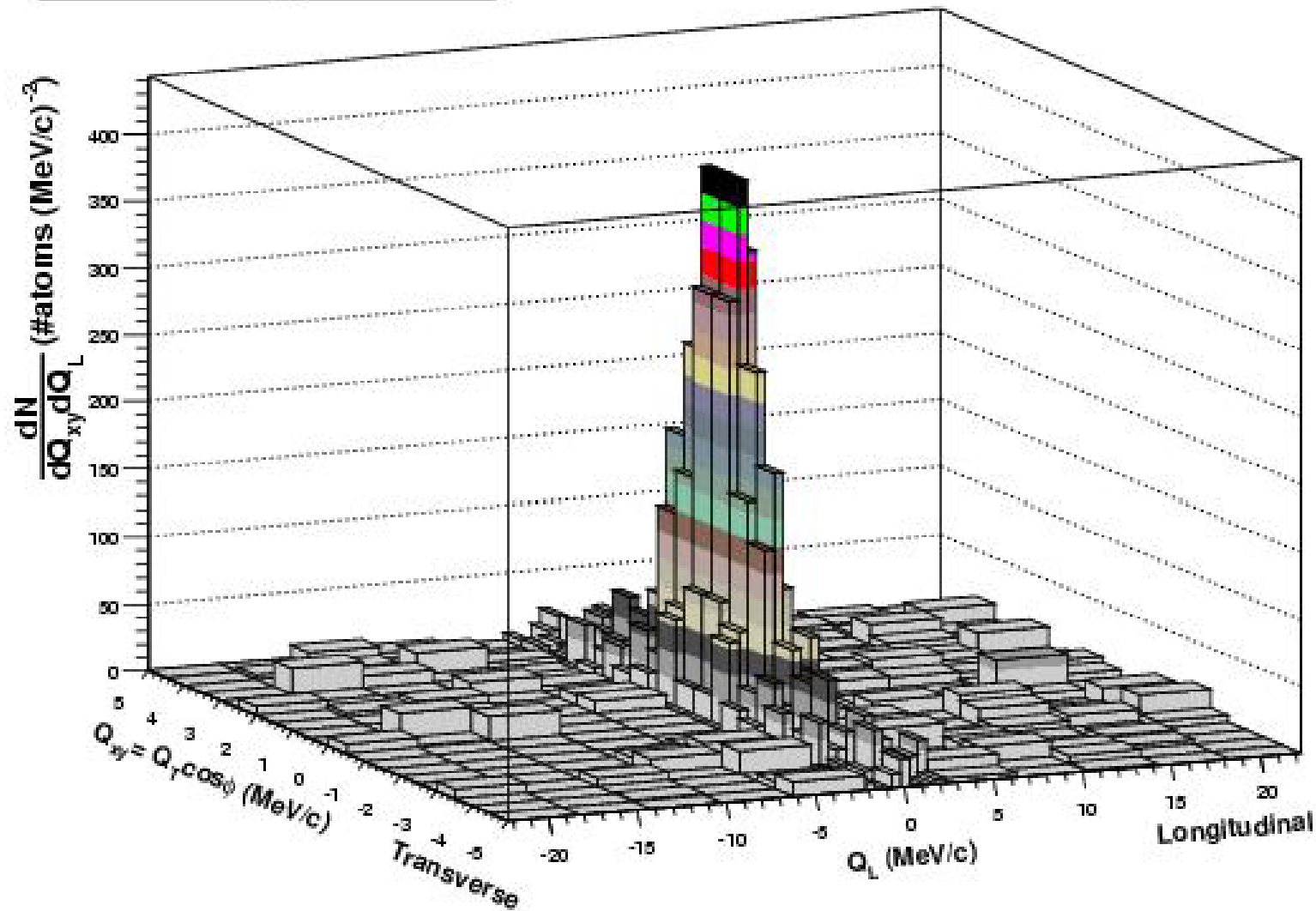
**Atom signal defined as difference between  
prompt data and Monte Carlo with  $\gamma = 0$**

# Pionium signal in $Q_t$ vs $Q_l$

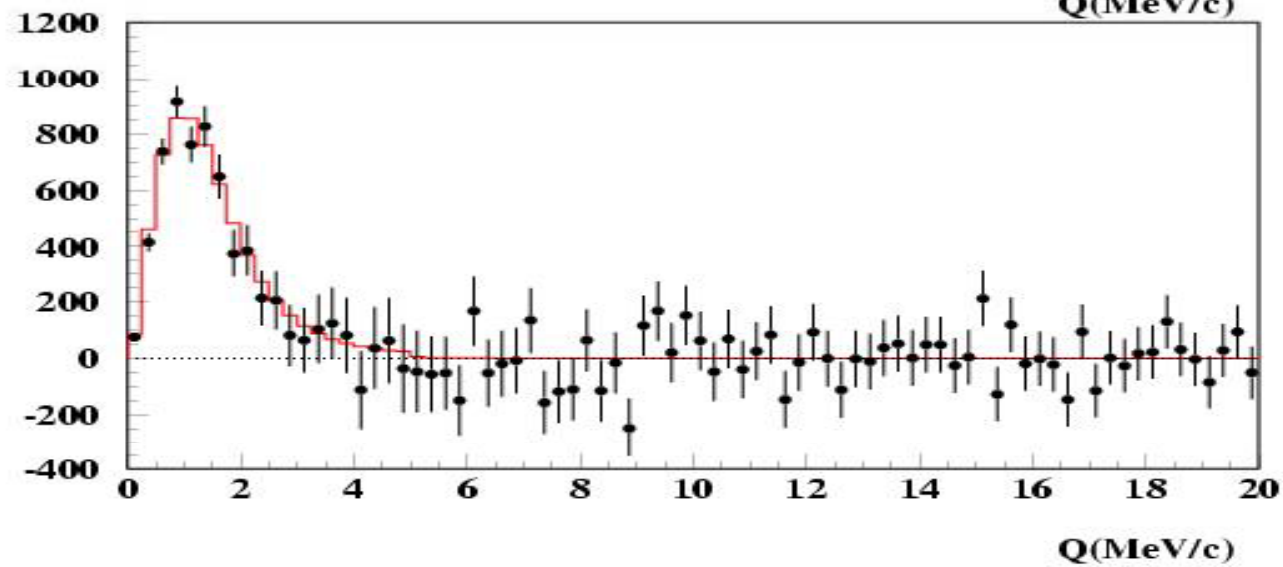
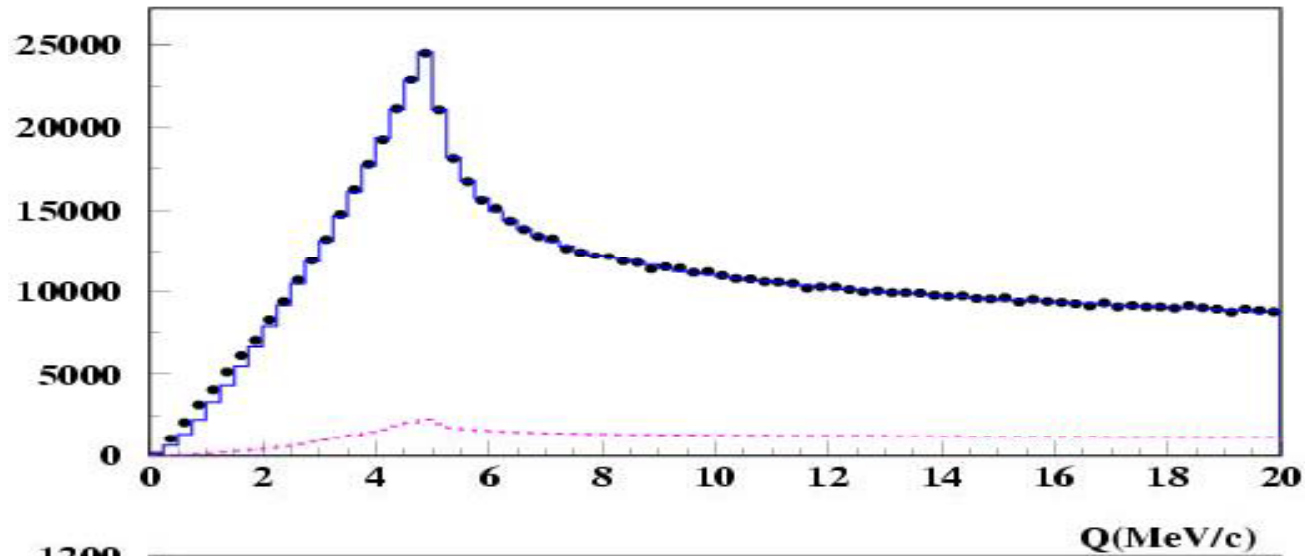


# PIONIUM BREAK-UP SIGNAL IN $\pi^+\pi^-$ SPECTRUM

Pionium Signal  $\pi^+\pi^-$

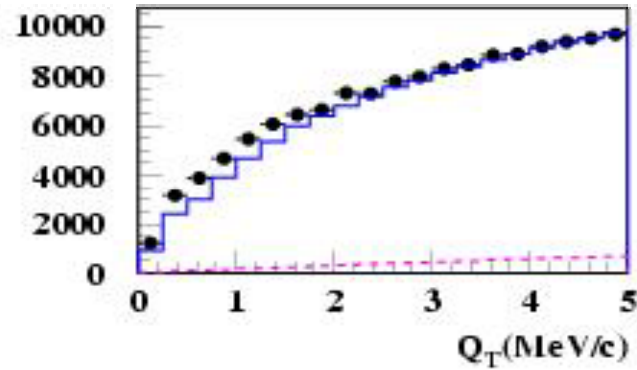


# Pionium signal in $Q = \sqrt{Q_L^2 + Q_T^2}$

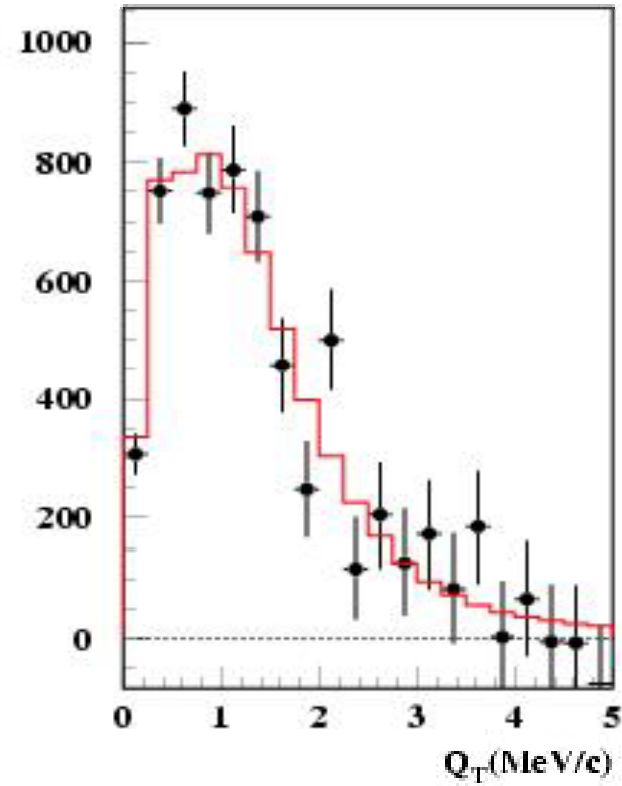
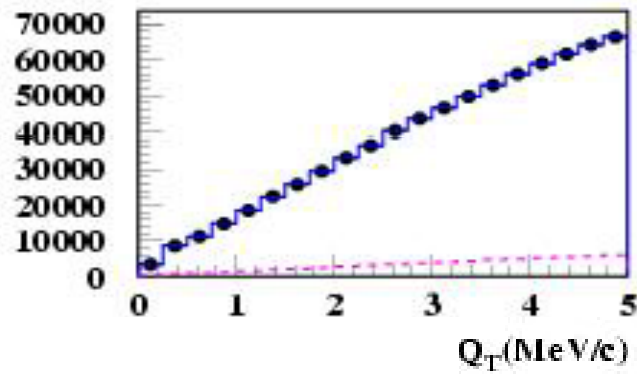


# PIONIUM TRANSVERSE SIGNAL

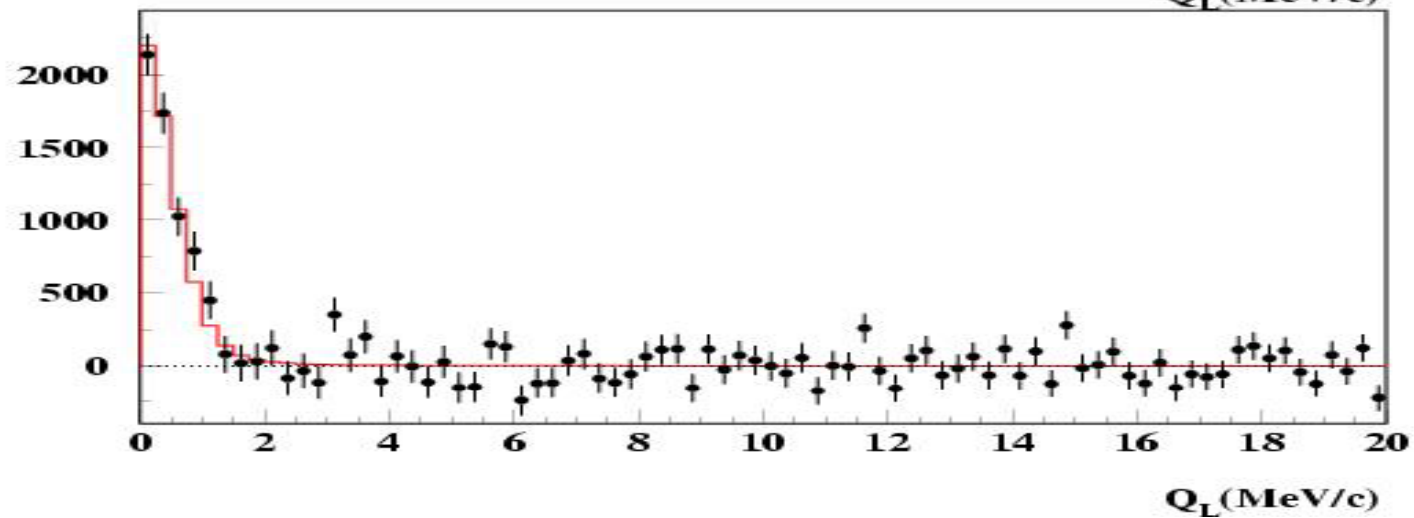
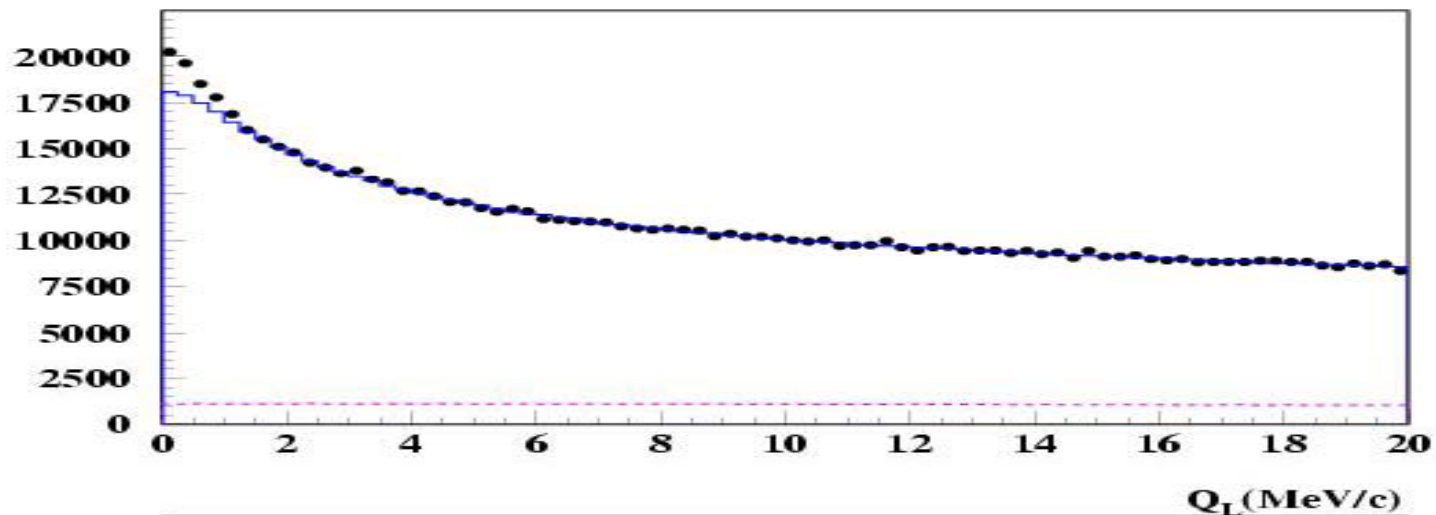
$Q_L < 2 \text{ MeV}/c$



$Q_L > 2 \text{ MeV}/c$



# Pionium Longitudinal Signal



# DETERMINATION OF BREAK-UP PROBABILITY

Coulomb-pair background  $N_{CC}$  determined from fit  $\alpha_1$  parameter:

$$P_{Br} = \frac{n_A}{N_A} = \frac{1}{K^{th}} \frac{n_A}{N_C}$$

$$P_{Br} = \frac{N_{AT}(\Omega)}{N_{CC}(\Omega)} \frac{1}{K^{exp}(\Omega)}$$

$$K^{exp} = \frac{\varepsilon_{CC}(\Omega)}{\varepsilon_{AT}(\Omega)} K^{th}(\Omega)$$

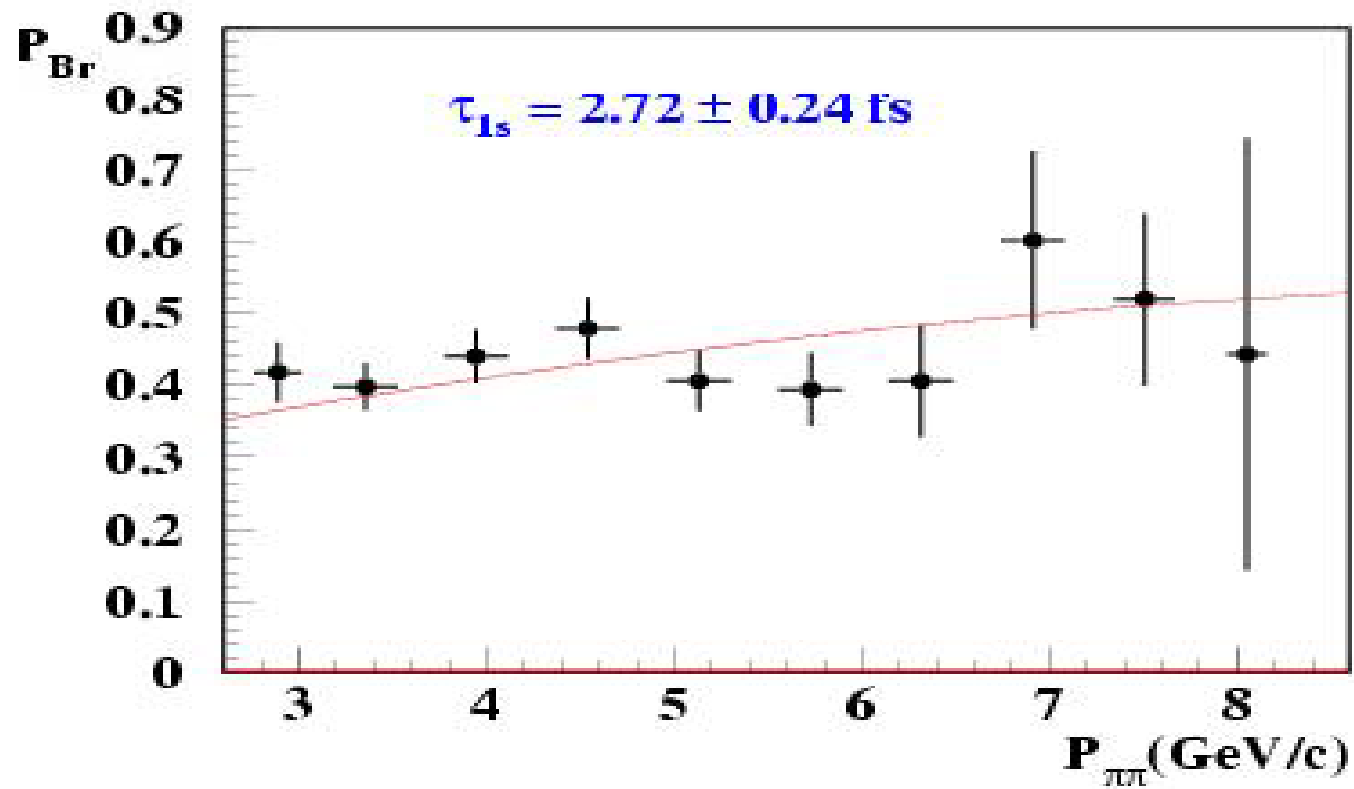
QM analytical factor: 
$$K^{th}(\Omega) = \frac{(2\pi\alpha M_\pi)^3}{\pi} \frac{\sum 1/n^3}{\int_\Omega A_C(Q) d^2Q}$$

Acceptance factors  $\varepsilon_i$  determined by Monte Carlo simulation

Different extrapolation domains:  $\Omega = (0, Q_T^C) \times (0, Q_L^C)$

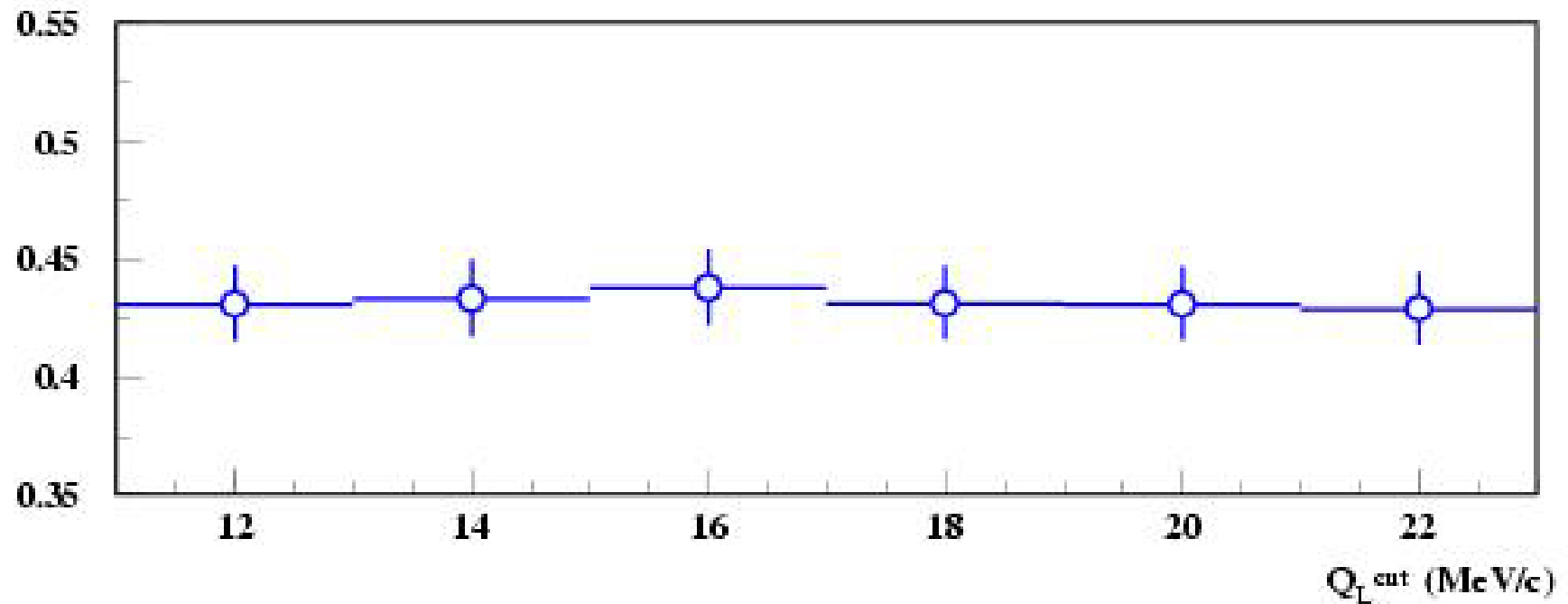
Standard choice is  $Q_L^C = 2 \text{ MeV}/c$  and  $Q_T^C = 5 \text{ MeV}/c$

## Break-up probability as function of pionium momentum

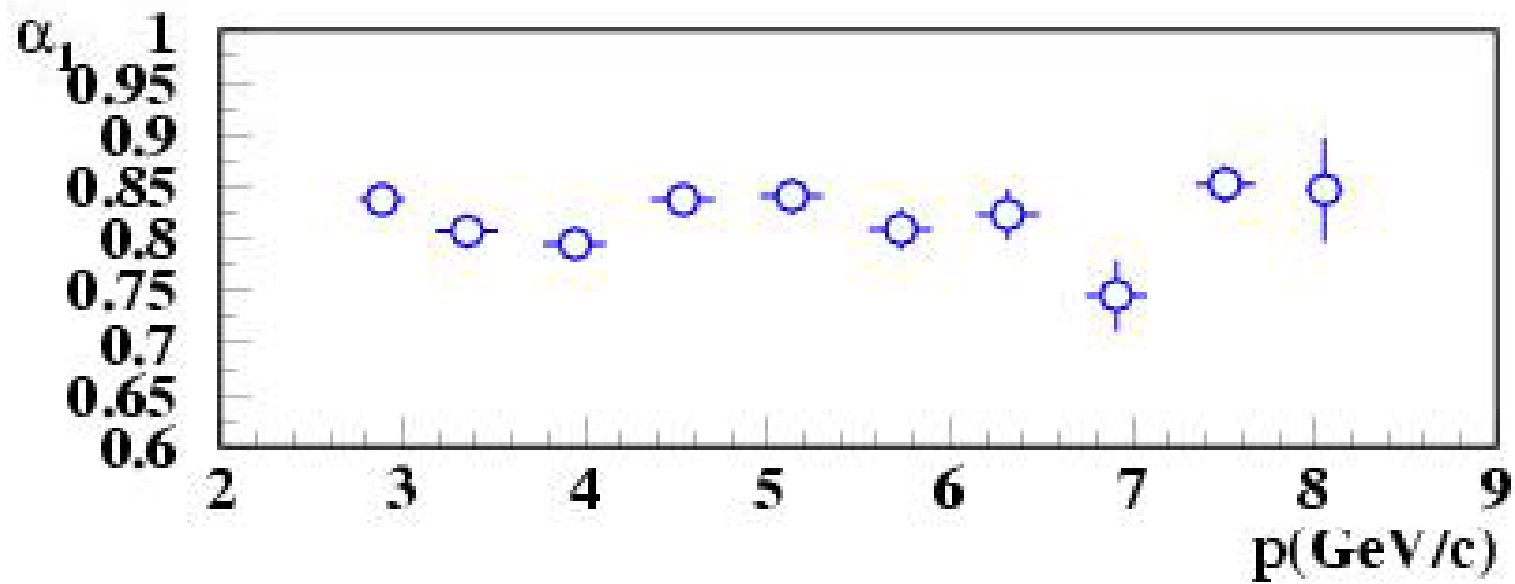


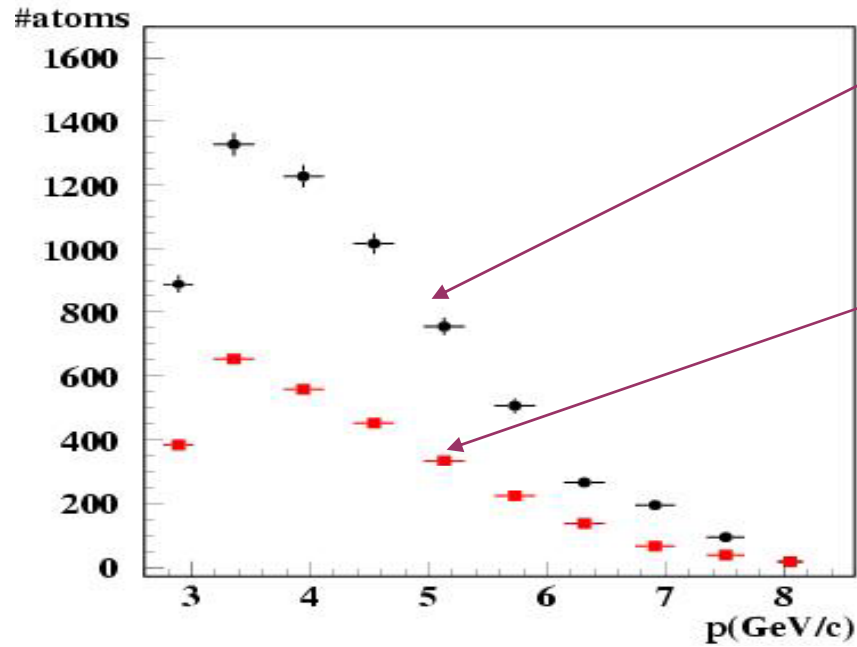


## $P_{Br}$ as function of $Q_L$ upper cut



## Fraction of Coulomb pairs as function of momentum

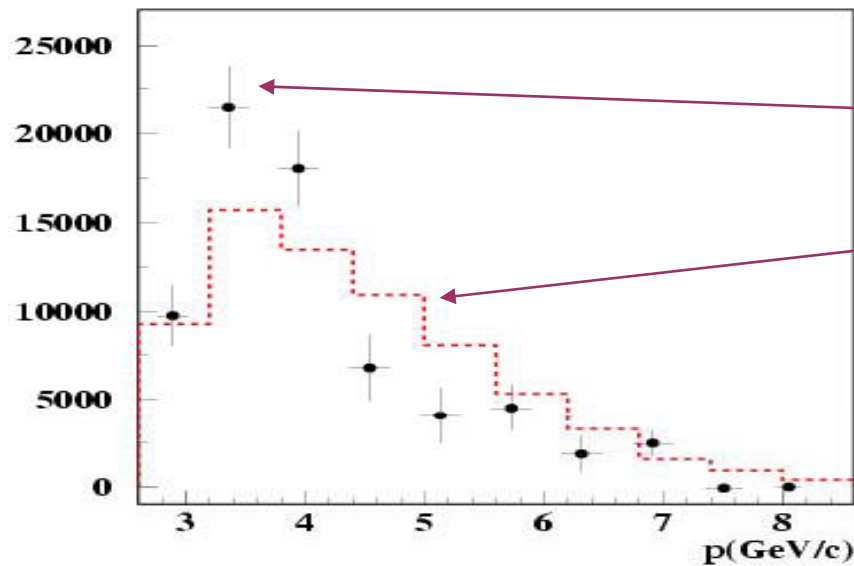




Atom Pairs

Coulomb Pairs x 1/40

Spectrum consistent with  $\pi^+\pi^-$  bound state formation



Long-lived pairs ( $\alpha_2$ )

Coulomb Pairs

Softer spectrum ( $\eta, \omega$  ..) expected from Monte Carlo

# Breakup probability

$$P_{\text{Br}}=0.435\pm 0.016 \text{ (stat)} \pm 0.008 \text{ (syst)} = 0.435 \pm 0.018$$

## Summary of systematic uncertainties:

Source	$\sigma$
$Q_L$ trigger acceptance	$\pm 0.004$
MSGC+SFD background	$\pm 0.006$
Double Ionization cut	$\pm 0.003$
Double-track resolution	$\pm 0.003$
Target Impurity	$\pm 0.003$
KK contamination	$\pm 0.003$
<b>Total</b>	<b><math>\pm 0.008</math></b>

# Results from DIRAC

- *DIRAC collaboration has built up a double arm spectrometer which provides a pair relative momentum ( $Q$ ) resolution of 0.4 MeV/c for  $Q < 30$  MeV/c*
- *More than 6000 of  $\pi^+ \pi^-$  pairs from ponium break-up were observed*
- *The analysis of Ni 2001 data provides a lifetime measurement which translates into an  $S$ -wave amplitude measurement at rest :*

$$\tau_{1S} = 2.63^{+0.266}_{-0.255} (stat)^{+0.117}_{-0.111} (syst) fs$$

$$\tau_{1S} = 2.63^{+0.290}_{-0.278} fs$$

$$|a_2 - a_0| = 0.277^{+0.0153}_{-0.0146} M_\pi^{-1} = (0.277 \pm 0.015) M_\pi^{-1}$$

$$a_0 - a_2 = 0.265 \pm 0.004 \quad (\text{ChPT})$$